# Fast Imaging Trajectories: Non-Cartesian Sampling (1)

M229 Advanced Topics in MRI Holden H. Wu, Ph.D. 2021.04.29



Department of Radiological Sciences

David Geffen School of Medicine at UCLA

#### Class Business

- Homework 2 due 5/7
- Project proposal due 5/10
  - Can send a draft and we'll provide feedback
- Office hours

#### Outline

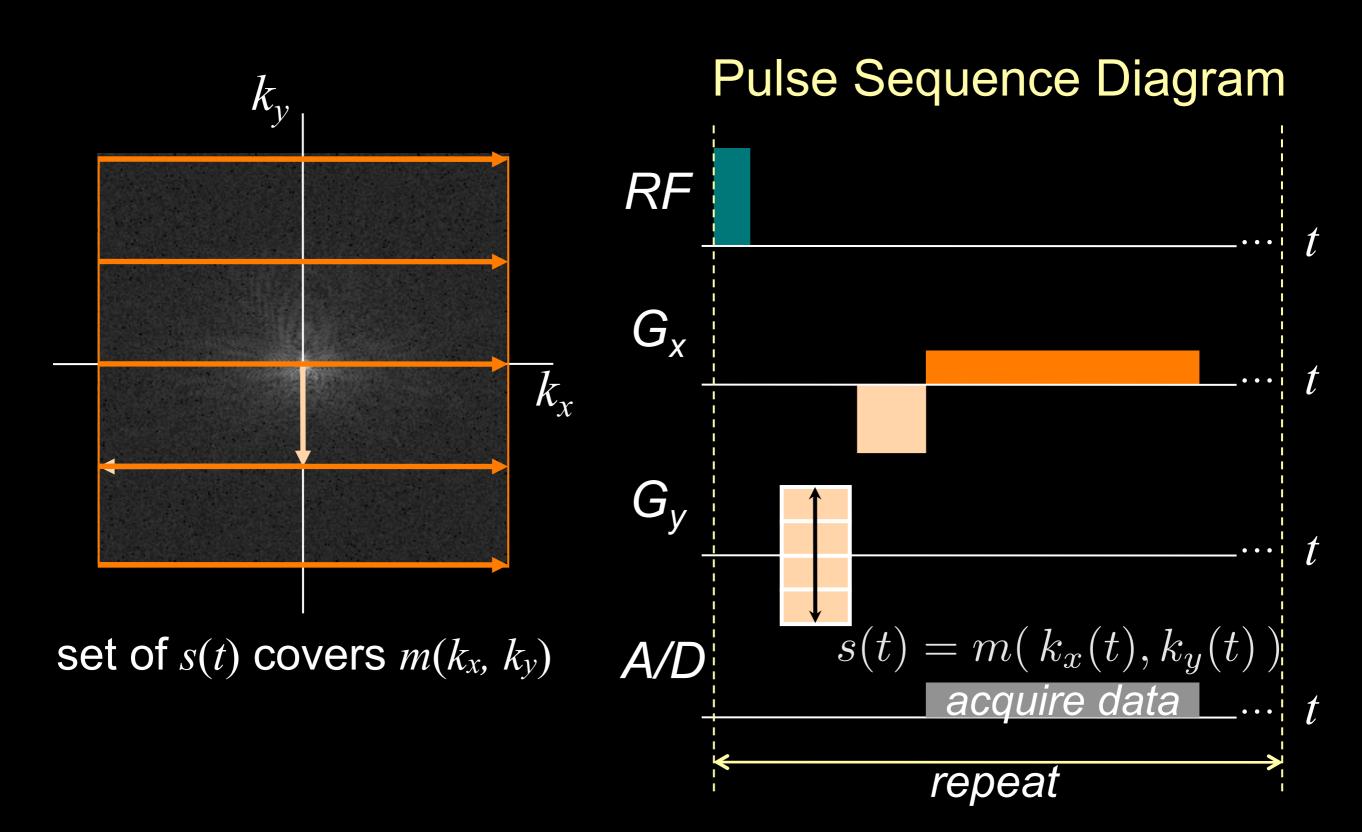
- Review of k-space sampling (2DFT)
- Radial
- Concentric rings

# MR Signal Equation

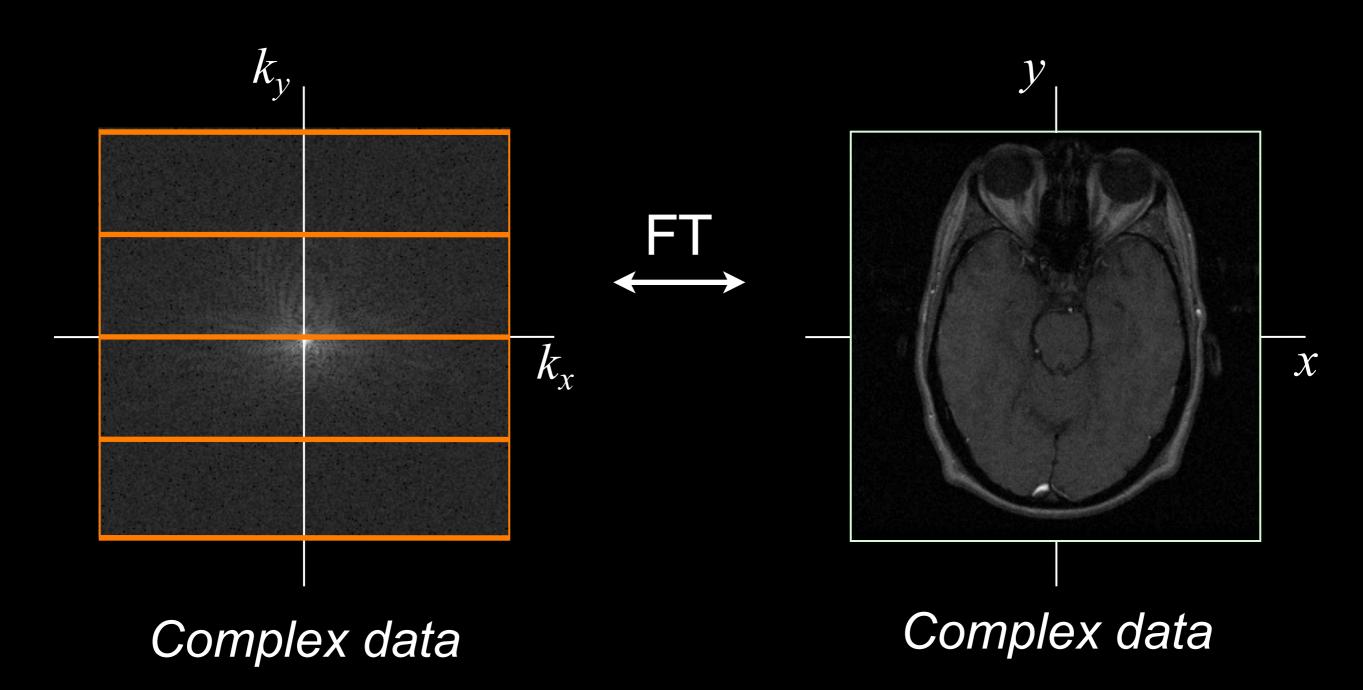
$$s(t) = \iint_{X,Y} M(x,y) \cdot \exp(-i2\pi \cdot [k_x(t) x + k_y(t) y]) dx dy$$
$$= m(k_x(t), k_y(t)) \qquad k_x(t) = \frac{\gamma}{2\pi} G_x t, k_y(t) = \frac{\gamma}{2\pi} G_y t$$

$$m = \mathcal{FT}(M(x, y))$$

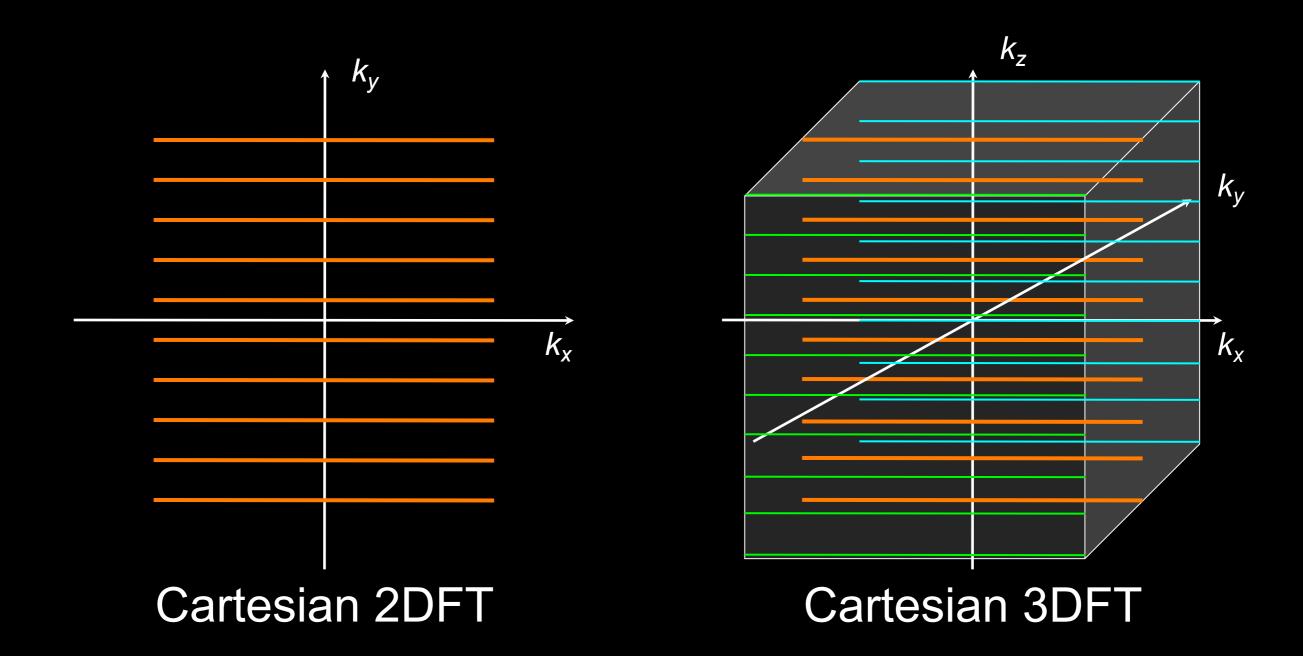
# k-Space Sampling



# Image Reconstruction



# Cartesian Sampling



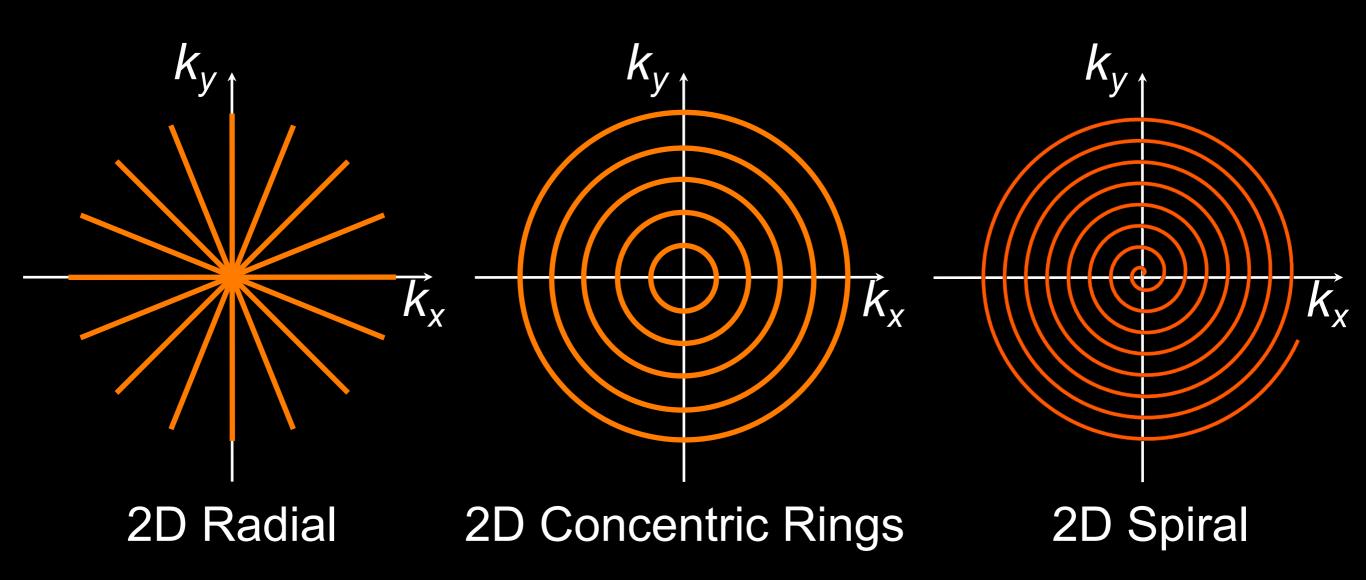
# MR Signal Equation

$$s(t) = \iint_{X,Y} M(x,y) \cdot \exp(-i2\pi \cdot [k_x(t) x + k_y(t) y]) dx dy$$
$$= m(k_x(t), k_y(t)) \qquad k_x(t) = \frac{\gamma}{2\pi} G_x t, k_y(t) = \frac{\gamma}{2\pi} G_y t$$

$$m = \mathcal{FT}(M(x, y))$$

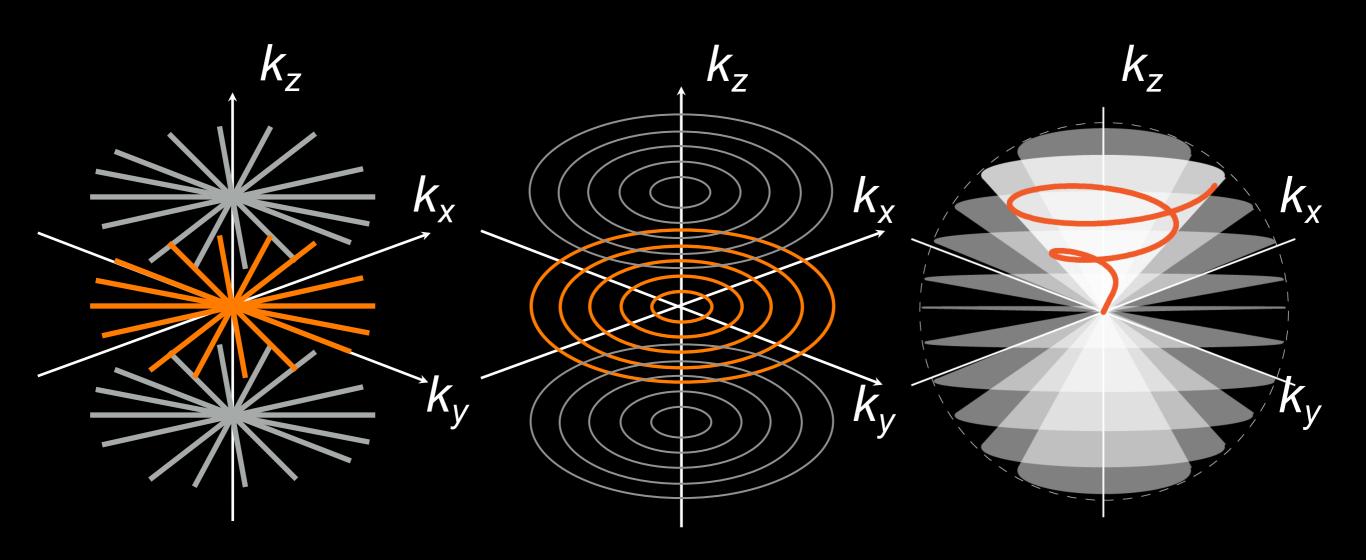
$$k_x(t) = \frac{\gamma}{2\pi} \int_0^t G_x(\tau) d\tau, \ k_y(t) = \frac{\gamma}{2\pi} \int_0^t G_y(\tau) d\tau$$

# Non-Cartesian Sampling



and much more ...

# Non-Cartesian Sampling



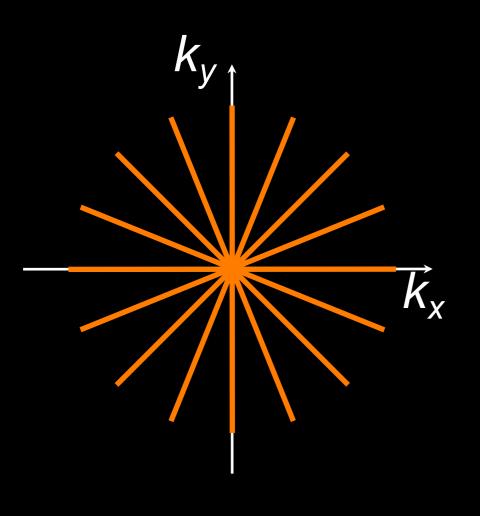
3D Stack of Stars

3D Stack of Rings

3D Cones

and much more ...

#### Radial

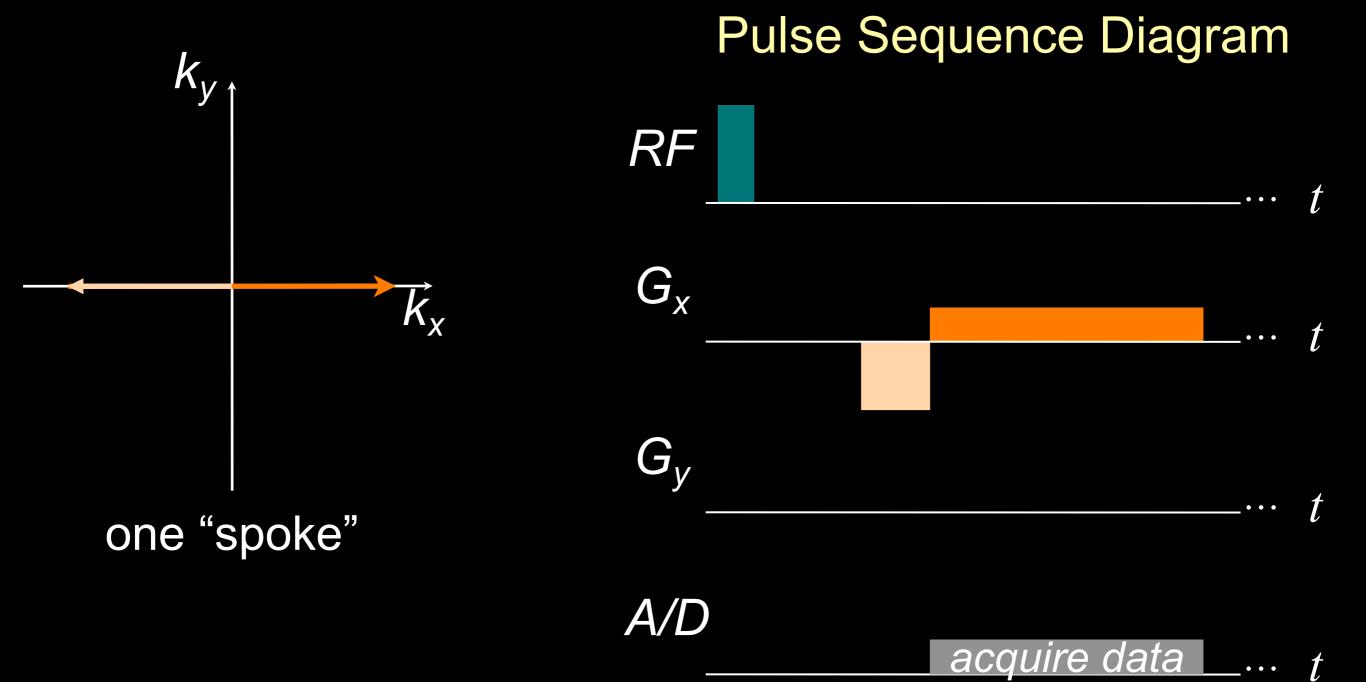


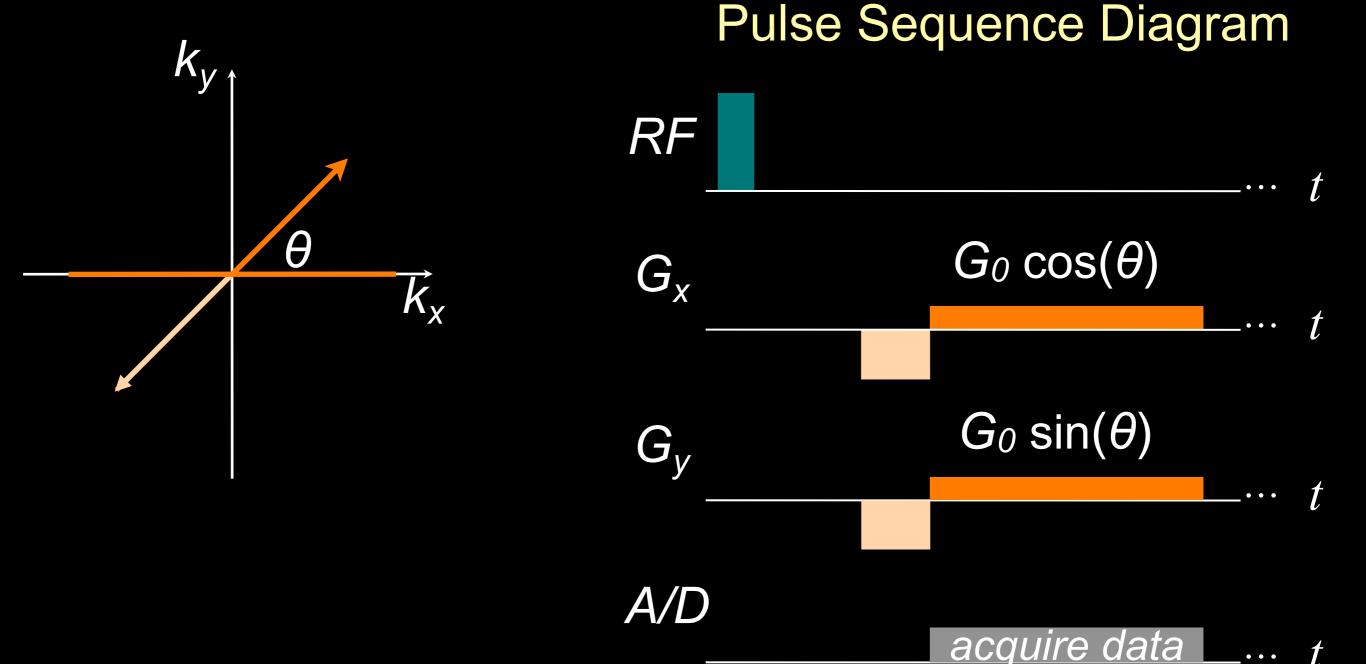
#### The original MRI trajectory!

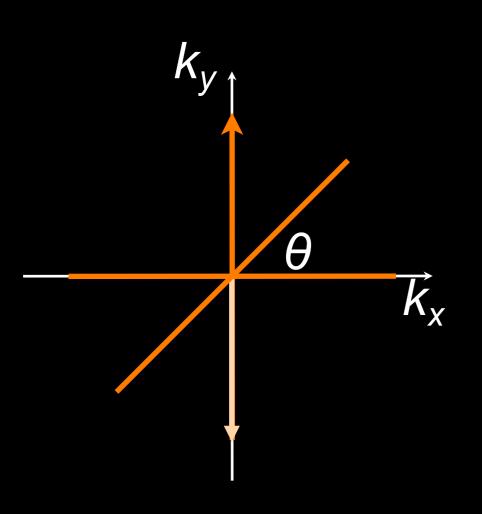
- Lauterbur, Nature 1973

#### Samples k-space on a polar grid

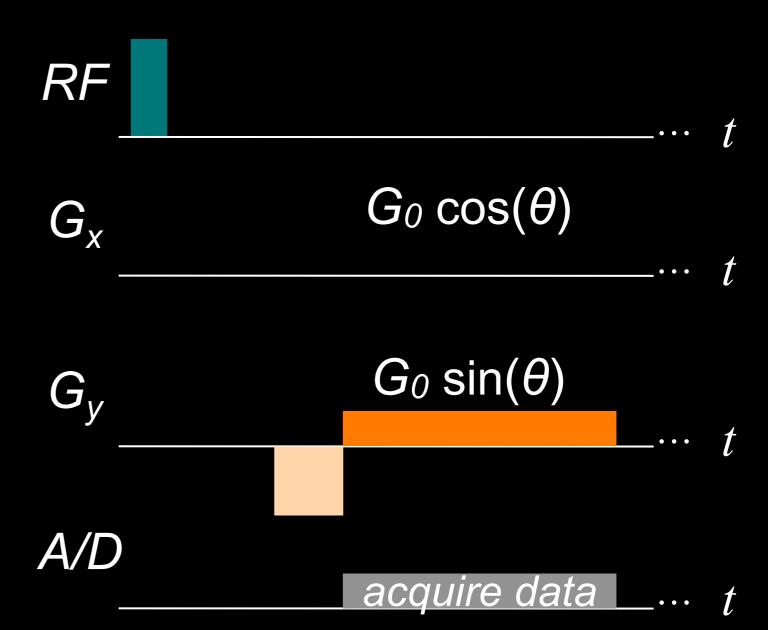
- "Spokes" correspond to projections
- Projection reconstruction (2DPR)

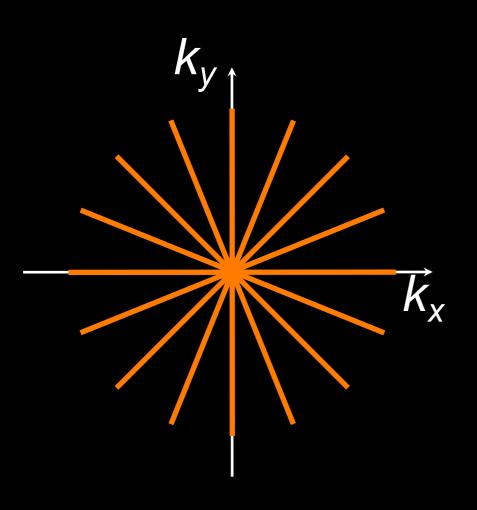


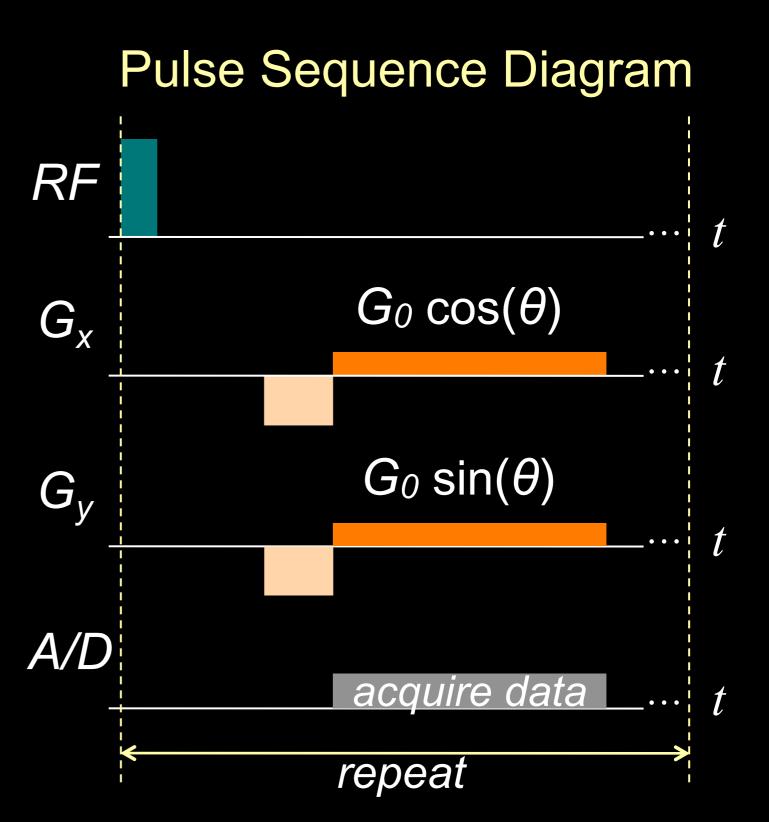


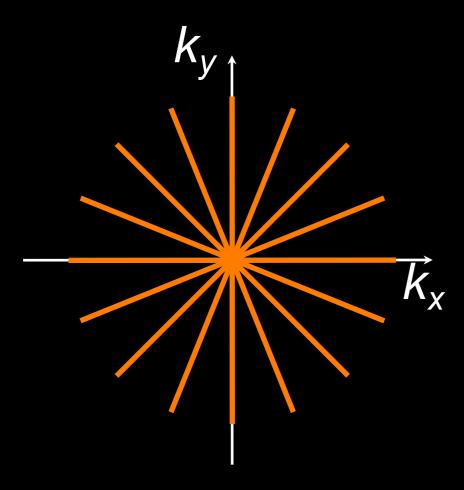


Pulse Sequence Diagram

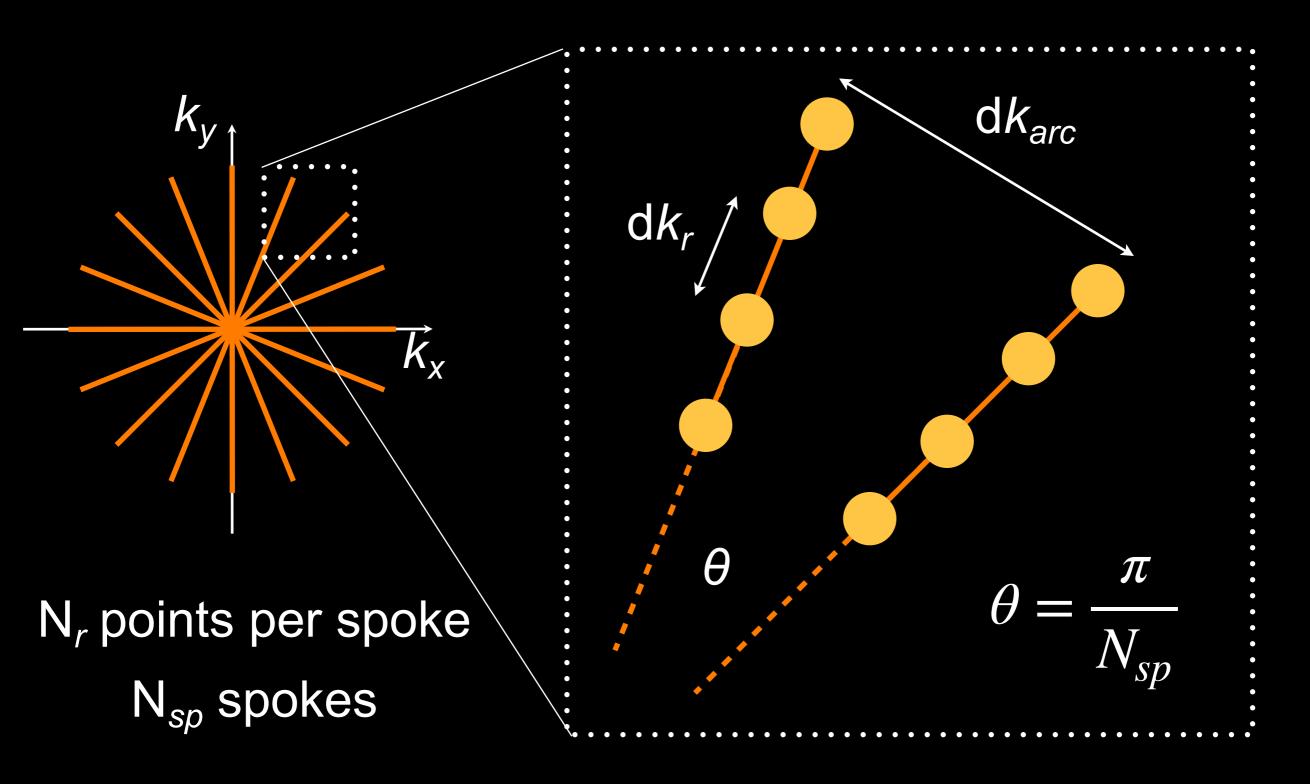


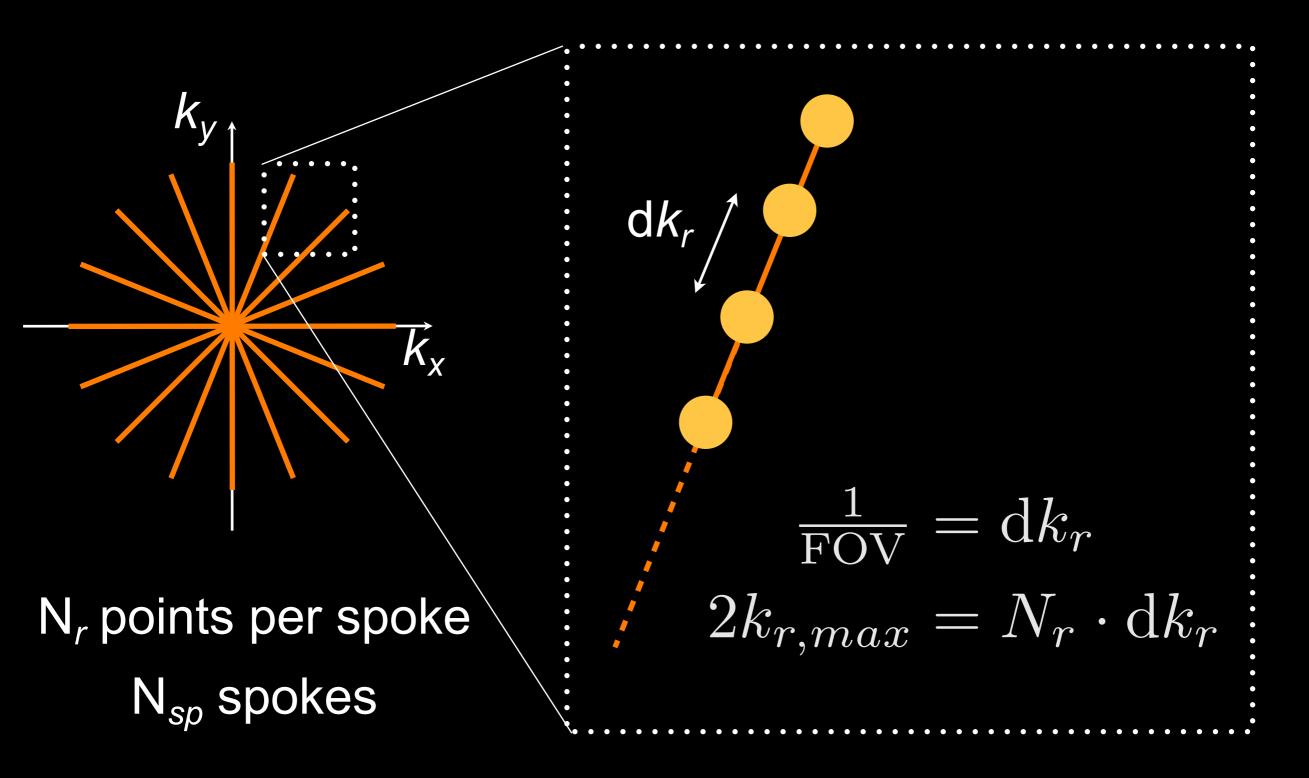


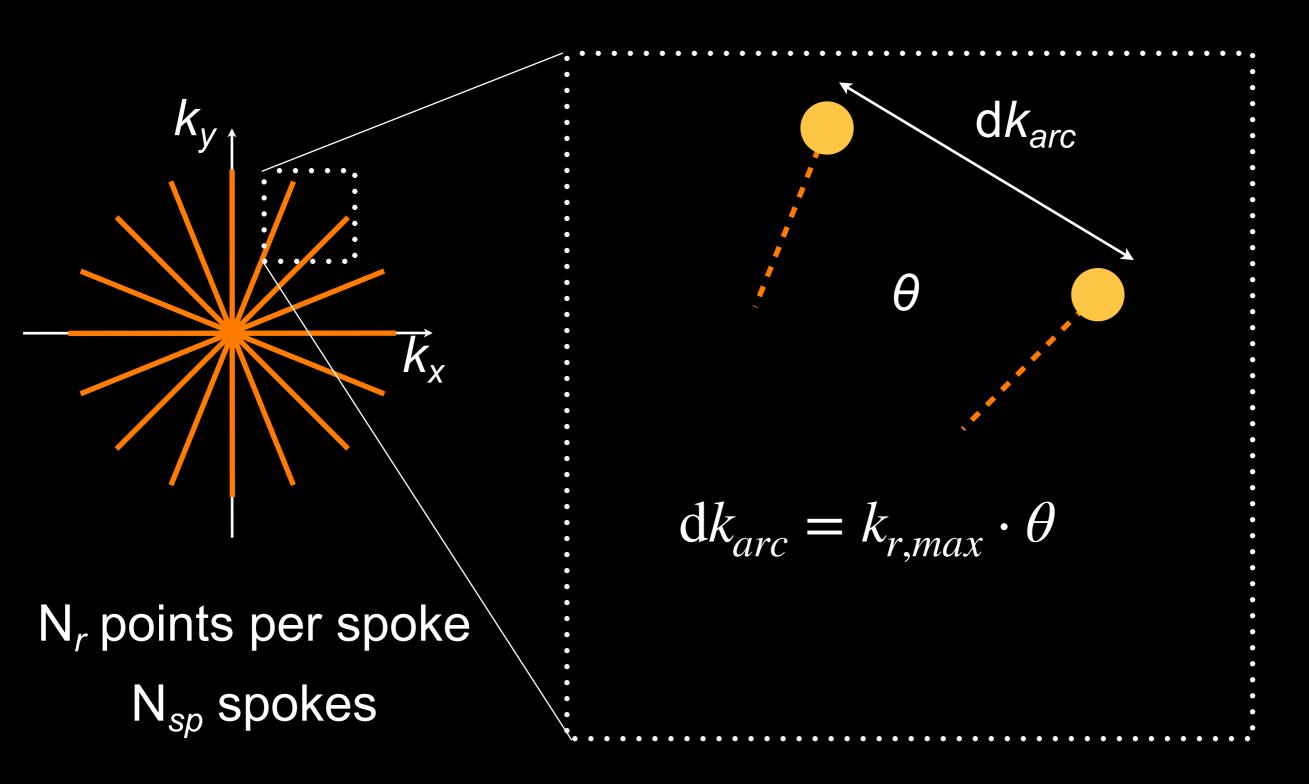


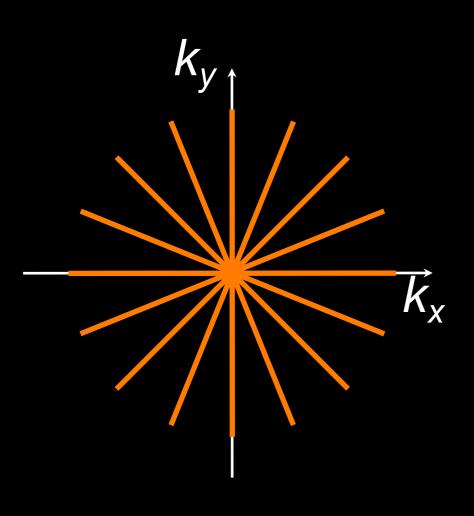


 $N_r$  points per spoke  $N_{sp}$  spokes









To satisfy Nyquist at edges of k-space:

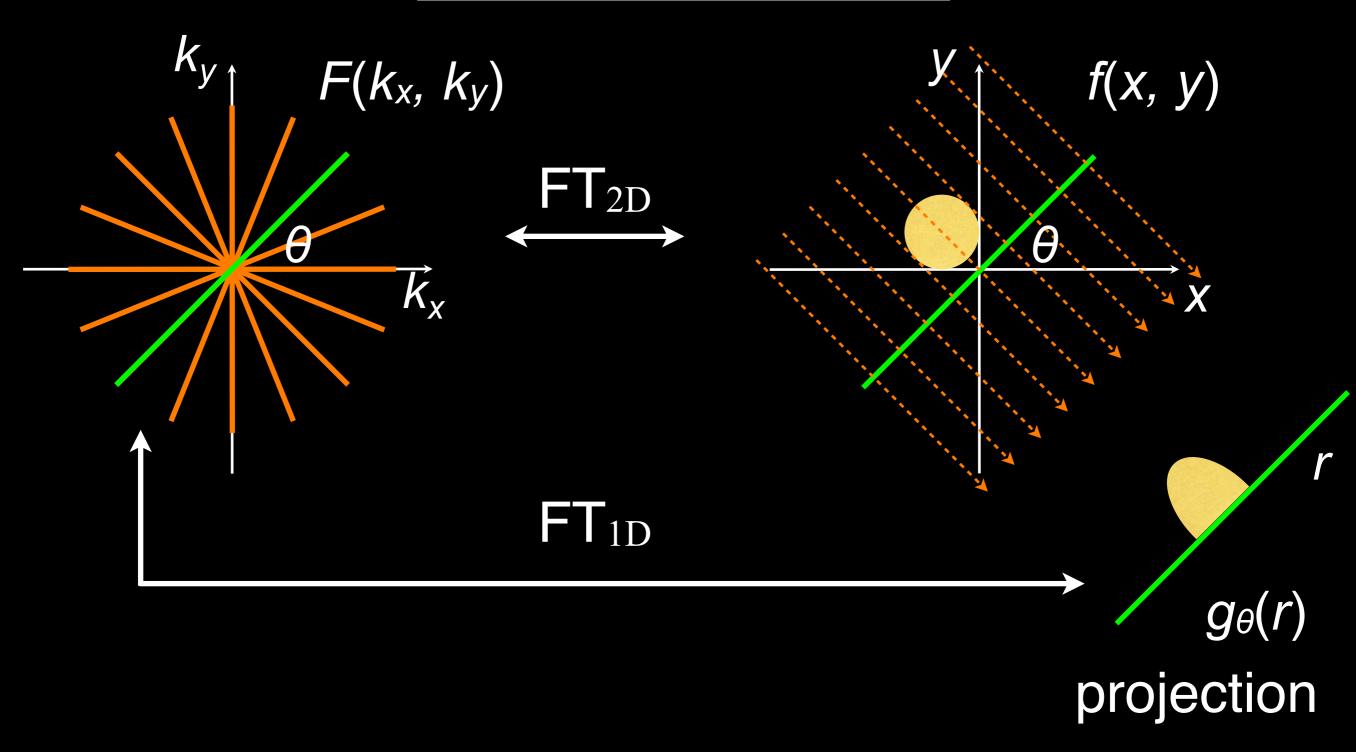
$$dk_{arc} = \left(\frac{N_r}{2} \cdot dk_r\right) \cdot \frac{\pi}{N_{sp}} \le dk_r$$

$$N_{sp} \ge \frac{\pi}{2} \cdot N_r$$

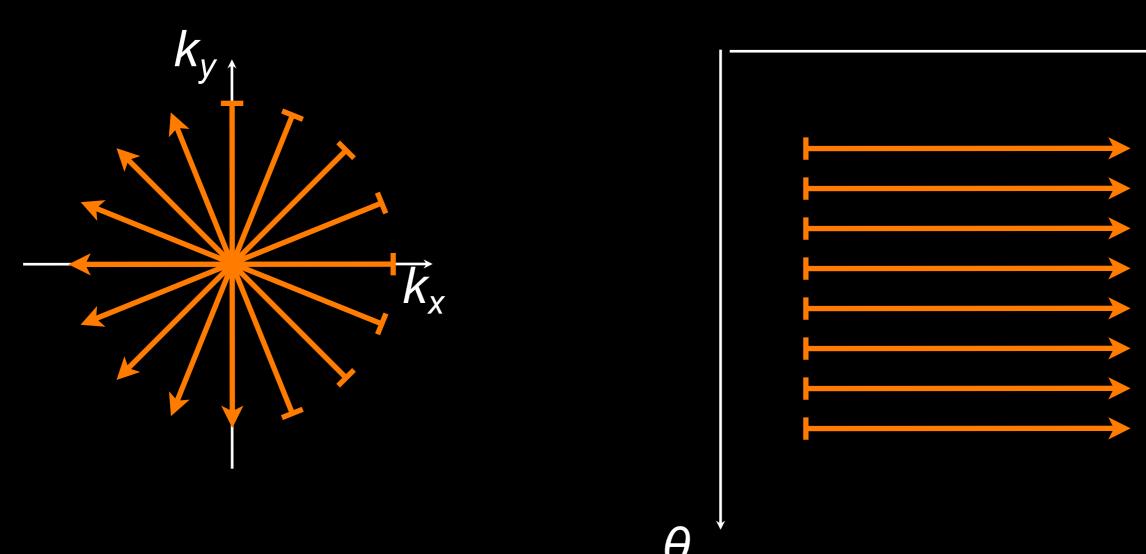
Example:  $N_r = 256$ ,  $N_{sp} = 403$ 

 $N_r$  points per spoke  $N_{sp}$  spokes

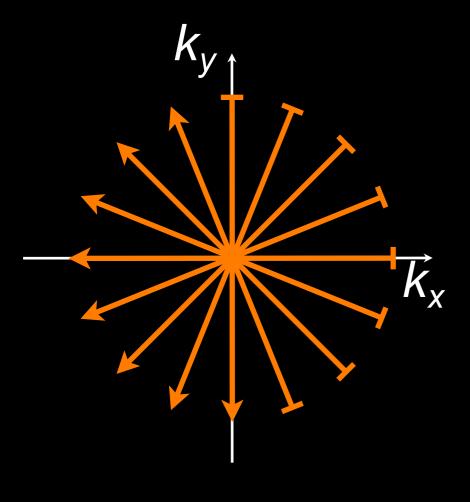
Central Section Theorem

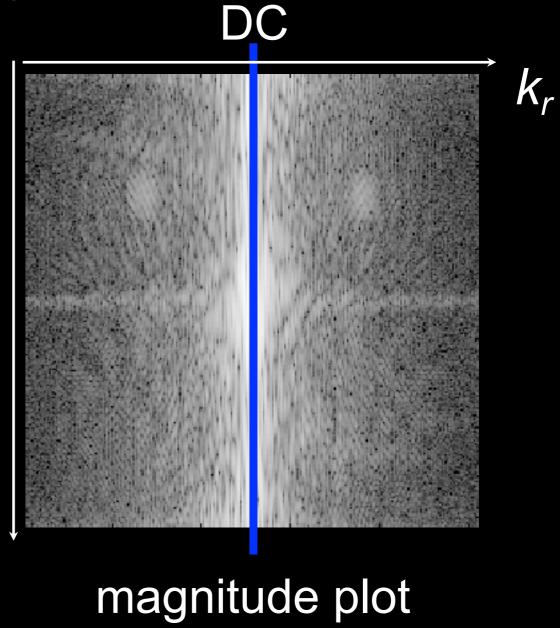


Collect spokes into  $(k_r, \theta)$  matrix  $\rightarrow$ 

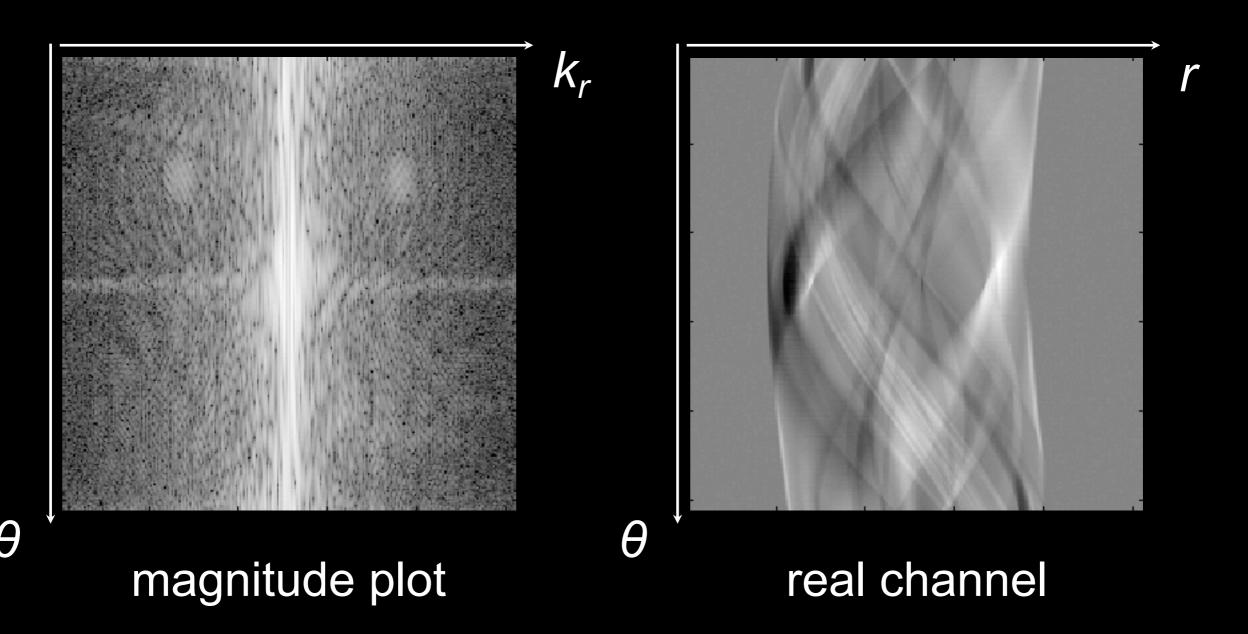


Collect spokes into  $(k_r, \theta)$  matrix  $\rightarrow$ 



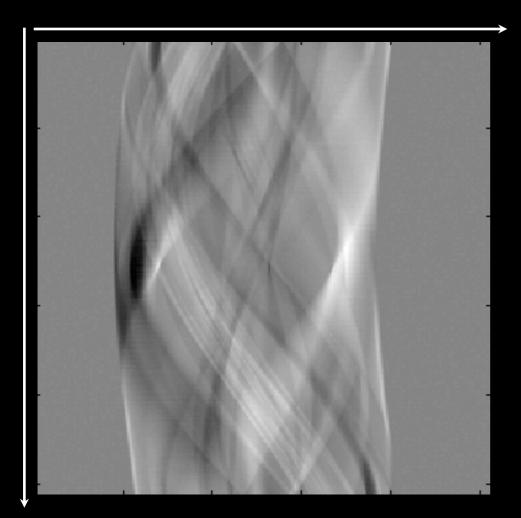


1DFT of each spoke along  $k_r \rightarrow$  "Sinogram"

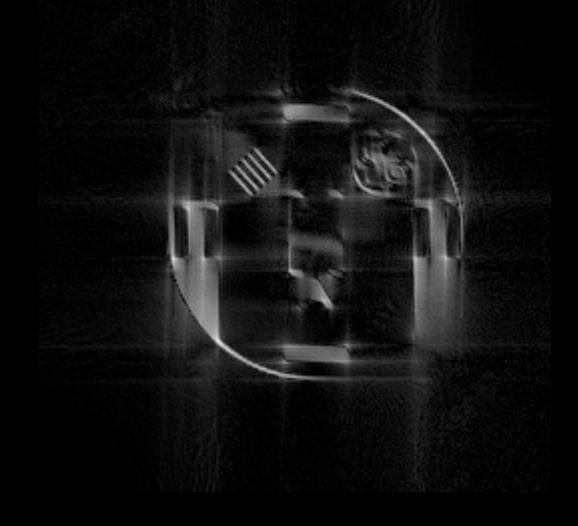


Filtered back projection →

Image



r

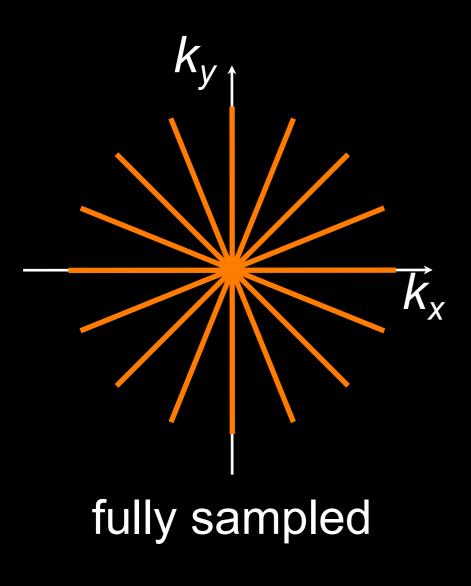


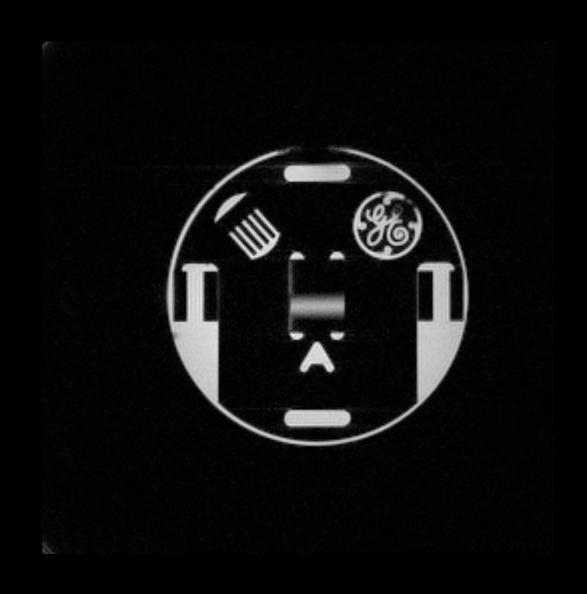
real channel

magnitude

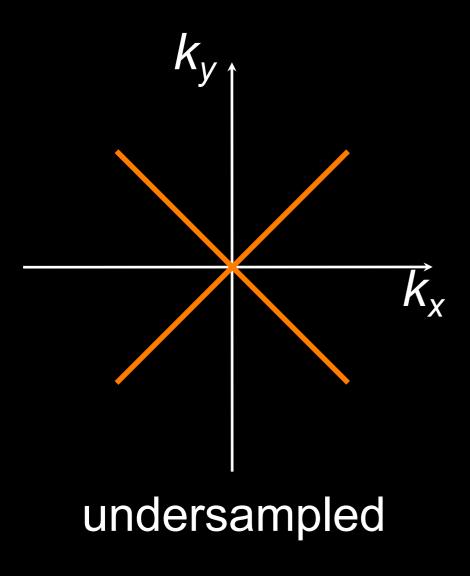
alternatively, can use "gridding" reconstruction

## Radial: Undersampling





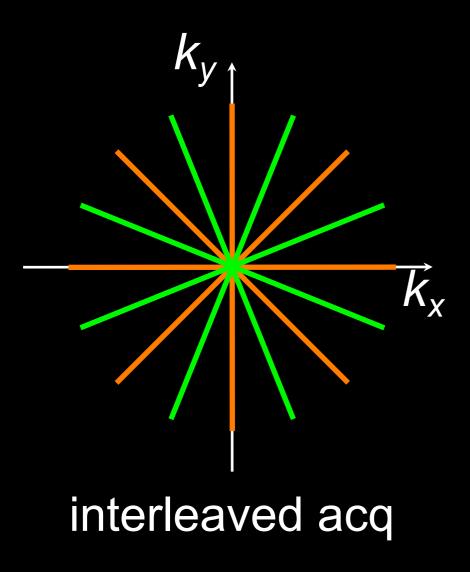
## Radial: Undersampling





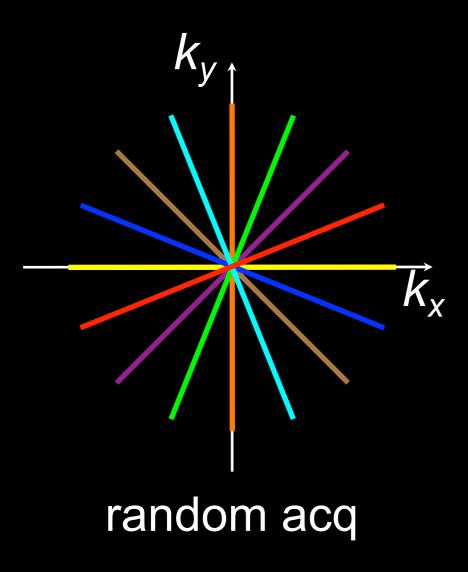
streaking artifacts

## Radial: Acq Ordering



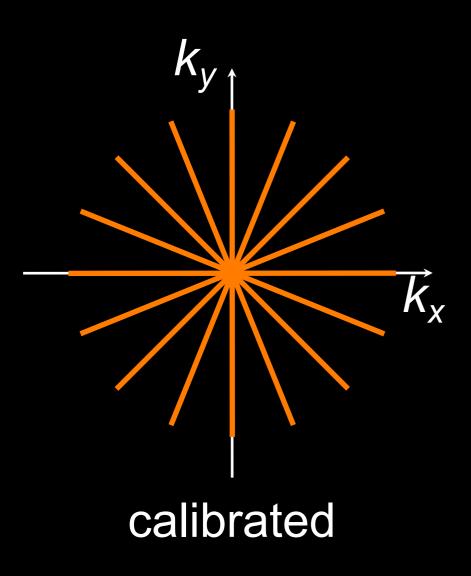


## Radial: Acq Ordering



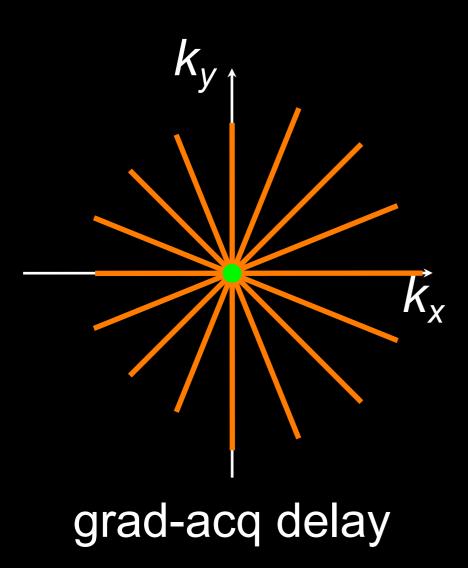


## Radial: Gradient Delays

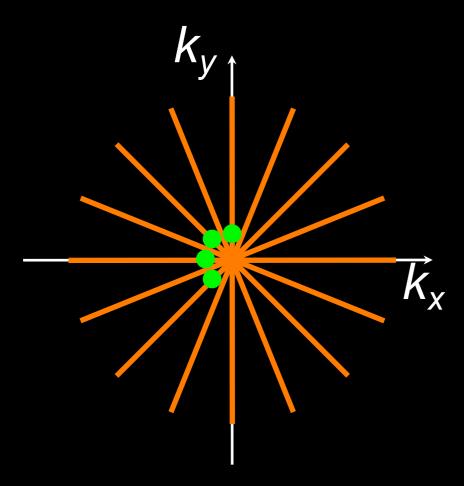




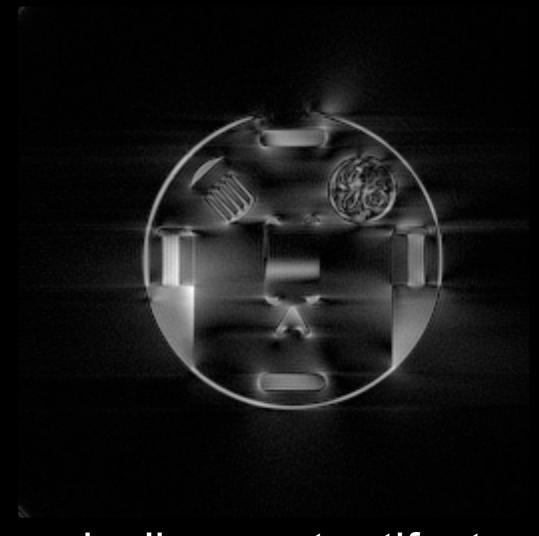
## Radial: Gradient Delays



## Radial: Gradient Delays

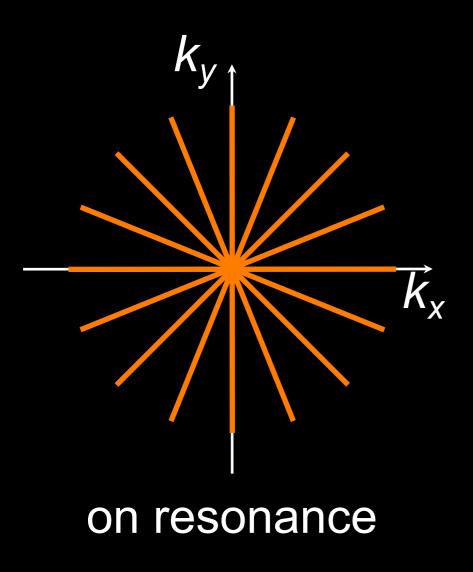


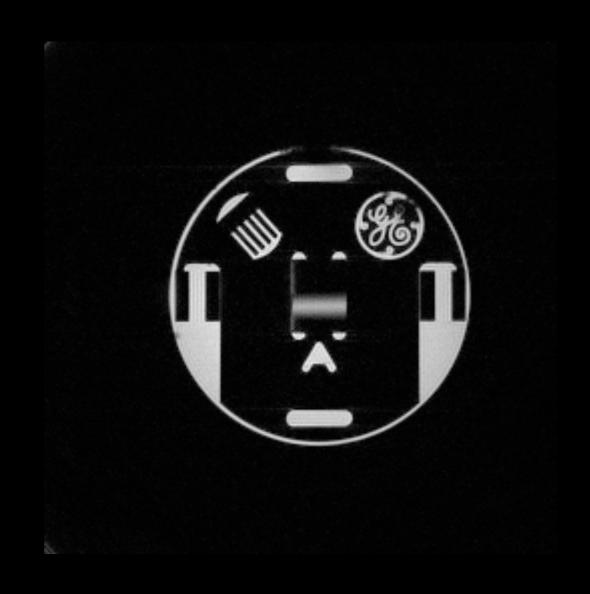
recon unaware of delays mis-aligned DC



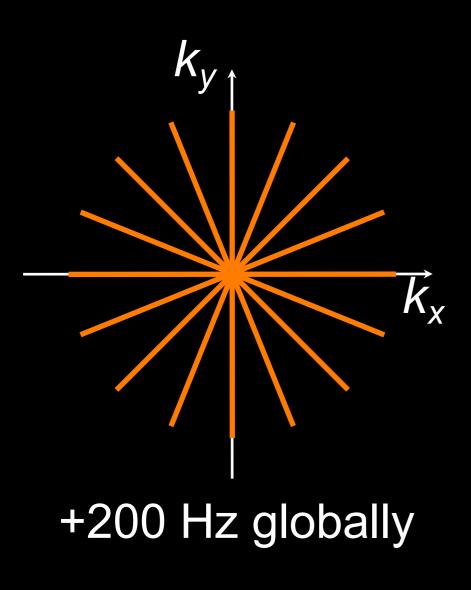
misalignment artifacts

## Radial: Off-resonance Effects





### Radial: Off-resonance Effects

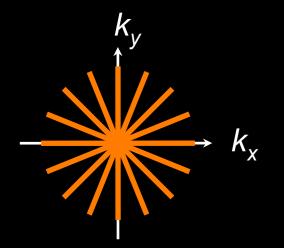




off-res blurring

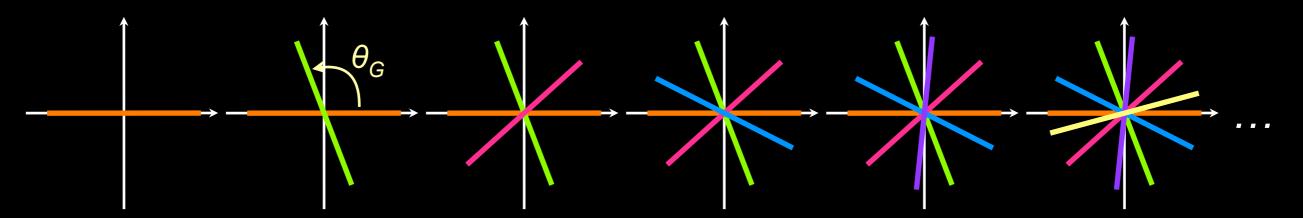
#### Radial: Real-time MRI

#### 2D Radial MRI



- Robust to motion (oversample center of k-space)
- Can tolerate a lot of undersampling

#### Golden Angle Ordering



- Almost uniform sampling of *k-t* space
- Flexible choice of temporal frame location and width

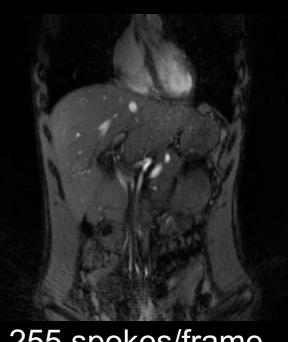
#### Radial: Real-time MRI

#### Radial FLASH

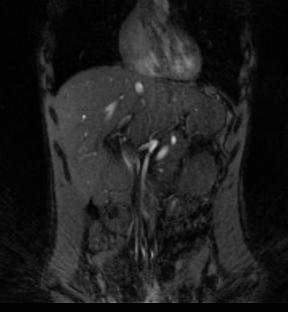
- golden-angle ordering
- 192 x 192 matrix
- TR = 3.1 ms(1 spoke per TR)
- 3.0 T

#### Reconstruction

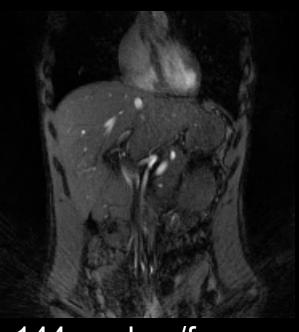
- sliding window of 20 TRs (display at 16 frames/sec)
- parallel imaging (SPIRiT) (300 spokes for Nyquist)



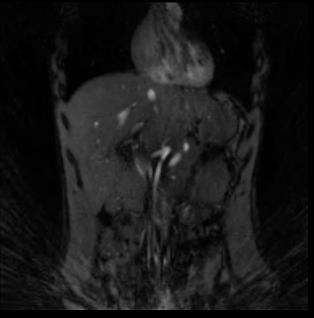
255 spokes/frame (791 ms/frame)



89 spokes/frame (276 ms/frame)



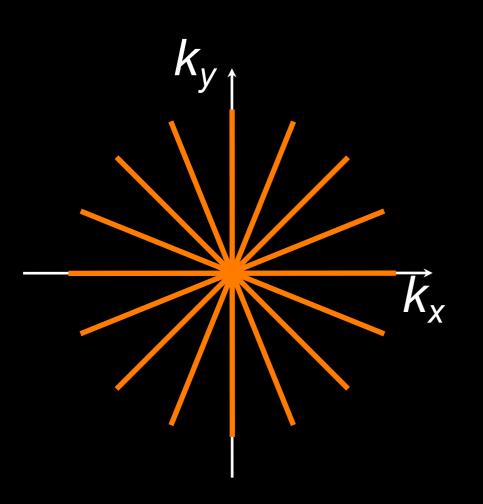
144 spokes/frame (446 ms/frame)



55 spokes/frame (171 ms/frame)

courtesy of Samantha Mikaiel

## Radial: Pros and Cons



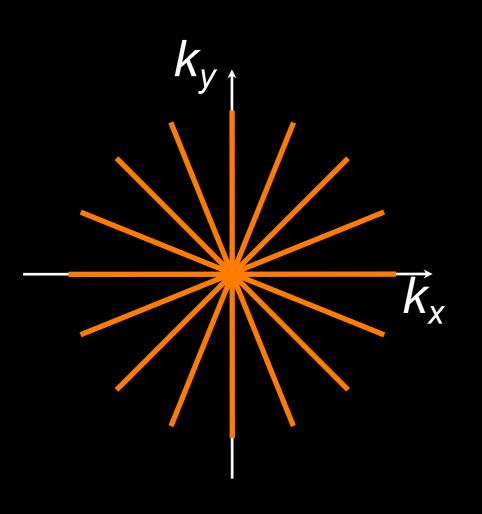
#### <u>Pros</u>

- Robust to motion (get DC every TR)
- Can tolerate a lot of undersampling
- Half-spoke PR has very short TE

#### Cons

- SNR penalty (non-uniform density)
- May have mixed contrast
- Sensitive to gradient delays
- Sensitive to off-resonance effects

## Radial: Extensions



3D stack of stars

3D koosh ball

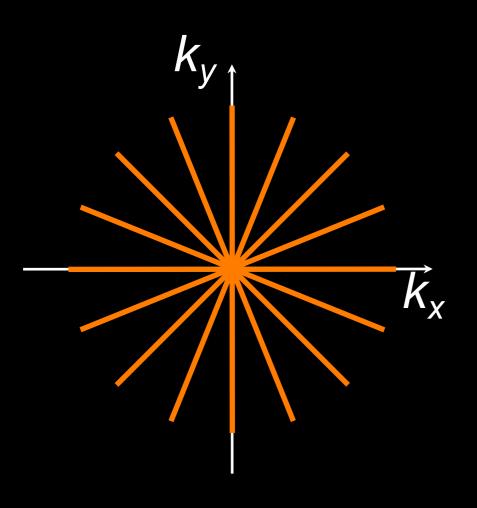
Multiple spokes per TR

Golden angle ordering

Parallel imaging

Partial Fourier

# Radial: Applications



#### Fast imaging

- Cardiac MRI

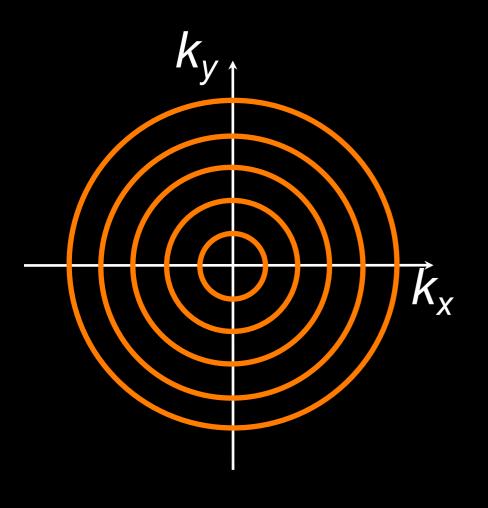
### Improve motion robustness

- Cardiac MRI
- Abdominal MRI

### <u>Ultra-short TE (UTE) imaging</u>

- Musculoskeletal MRI
- Lung MRI

# Concentric Rings

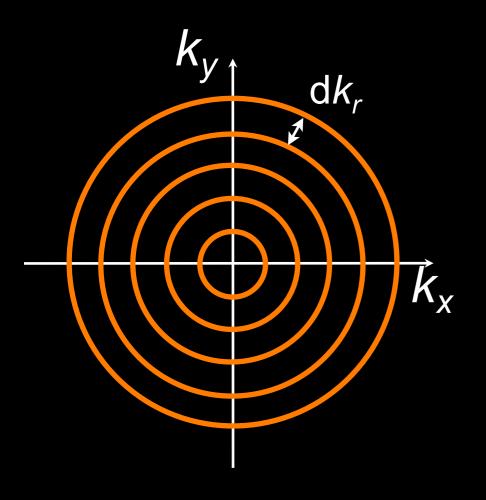


Non-rectilinear sampling!

Samples k-space on a polar grid

- "dual" of radial sampling
- shares some properties of 2DPR
- exhibits distinct characteristics

## Rings: Sampling Requirements



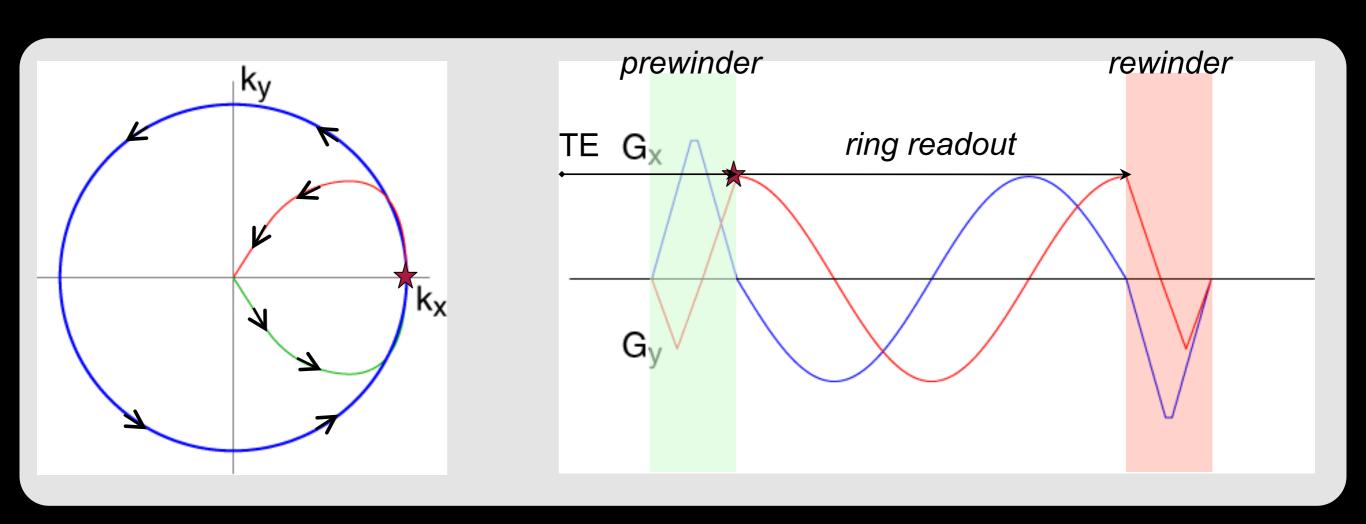
N concentric rings uniform spacing of  $dk_r$ 

$$\frac{1}{\text{FOV}} = dk_r$$

$$k_{r,max} = (N - 1) \cdot dk_r$$

Subject to hardware limits

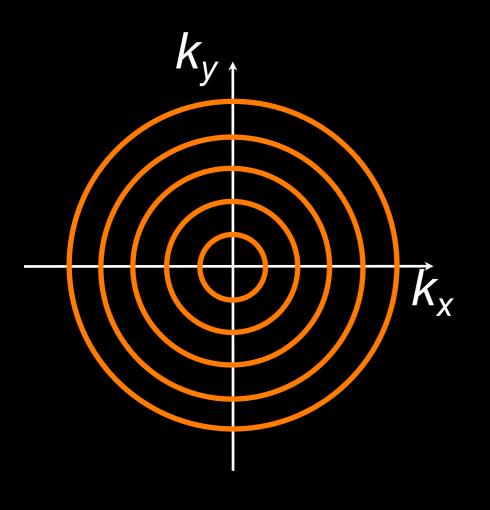
# Rings: Gradient Design



### Scale down gradients for outermost ring

- Sampling density identical to 2DPR
- Robust to gradient delays & timing errors

# Rings: Scan Time



For an  $M \times M$  image,

need N = M/2 rings

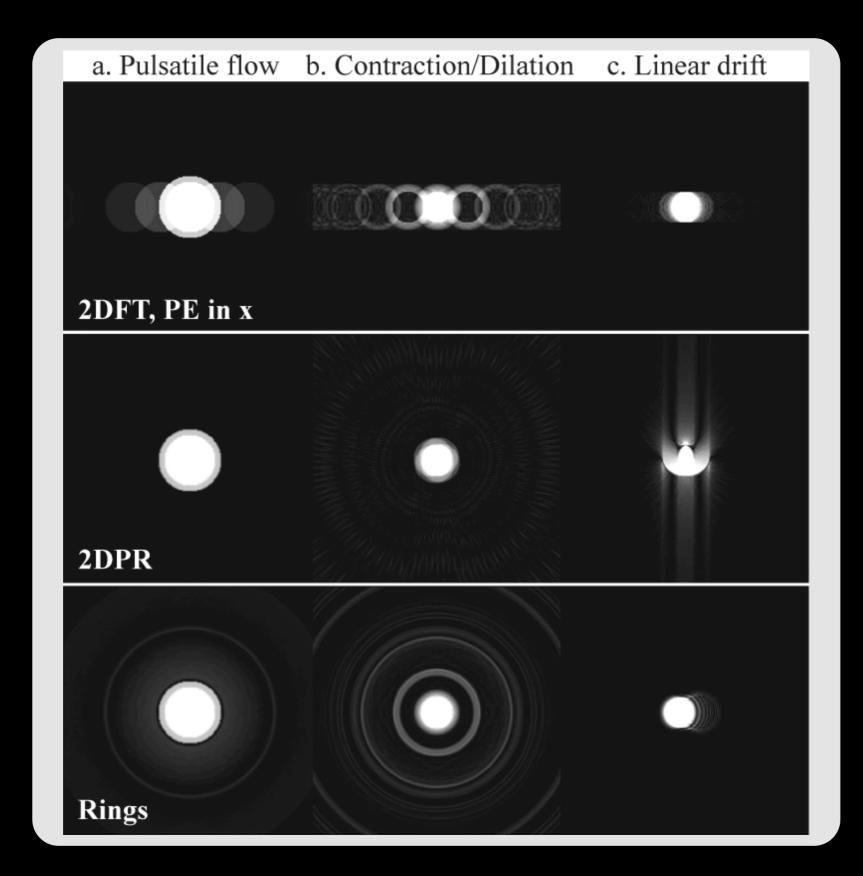
Scan time = (M/2) x TR<sub>ring</sub>

Compare with 2DFT:

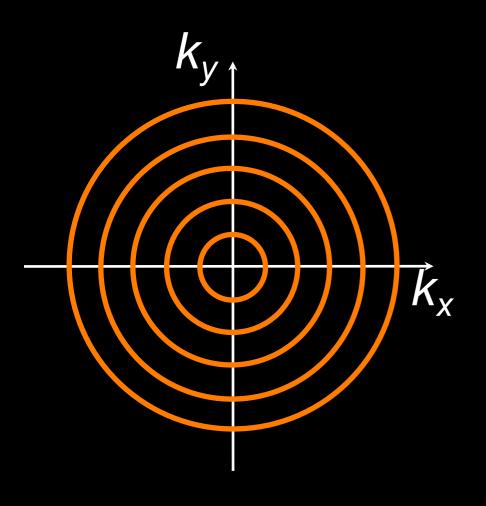
Scan time =  $M \times TR_{line}$ 

Rings offer ~2x acceleration

# Rings: Motion and Flow



# Rings: Image Reconstruction



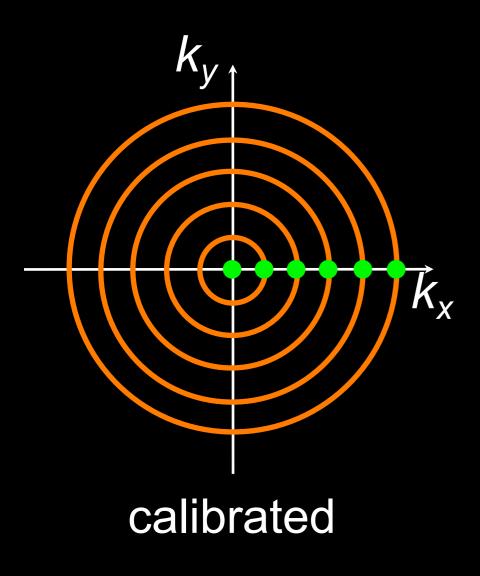
### Reformat into spokes

- filtered back projection

### Resample onto Cartesian grid

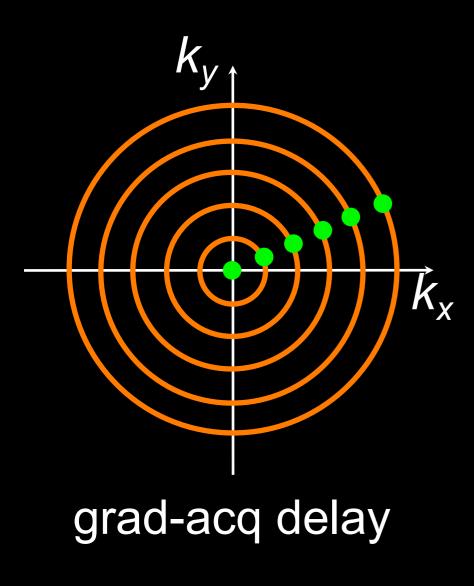
- "gridding" reconstruction

# Rings: Gradient Delays





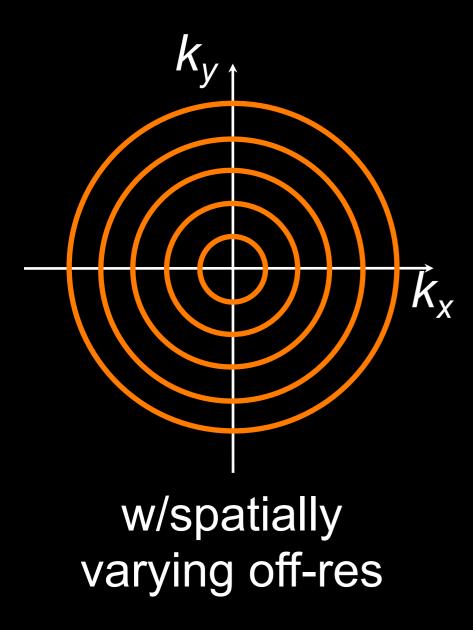
# Rings: Gradient Delays





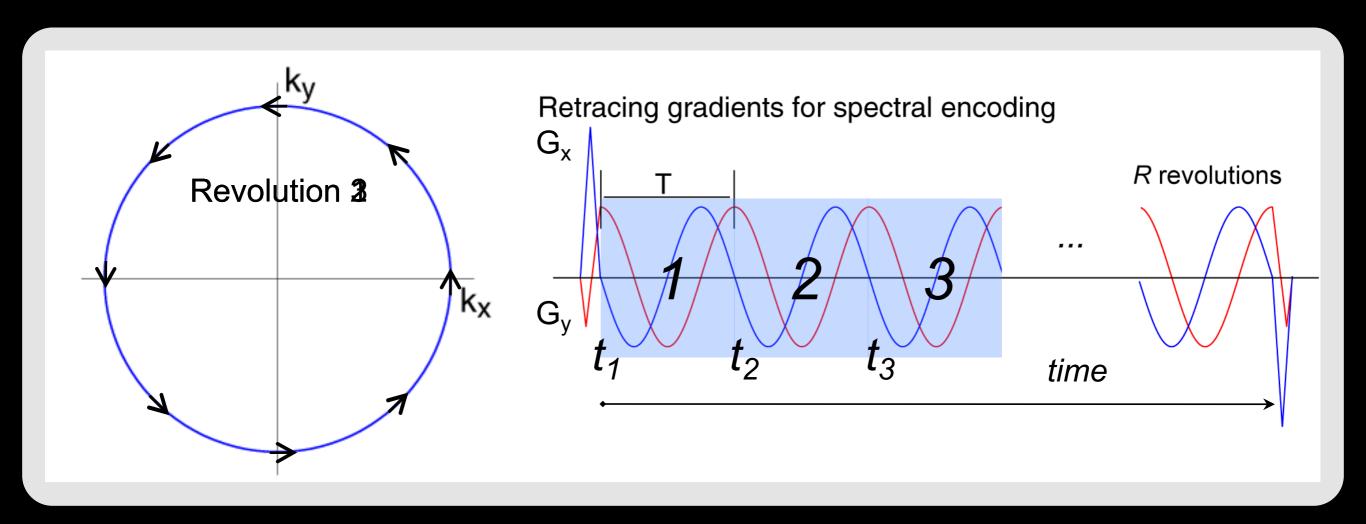
in-plane rotation

# Rings: Off-resonance Effects





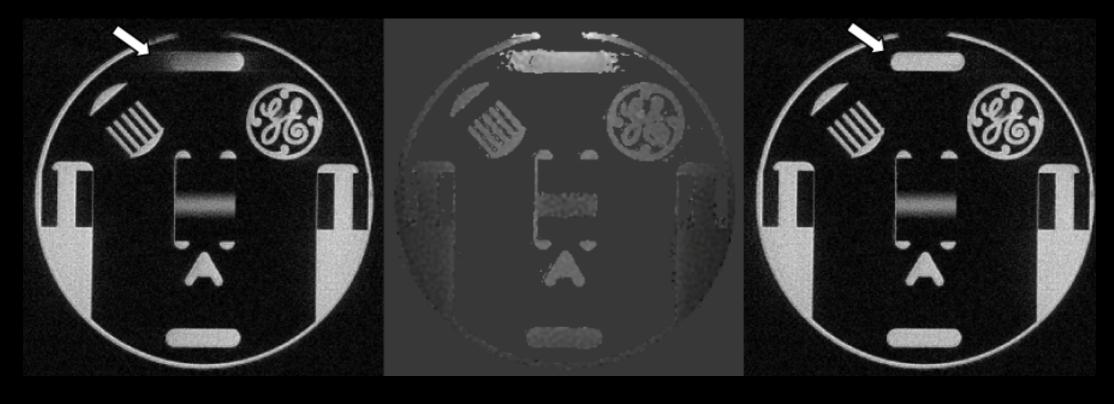
off-res blurring



## Encodes $(k_x, k_y, time)$ simultaneously

- Resolve off-resonance effects
- "Spectral" encoding

## Concentric Rings with 2 Revolutions / TR

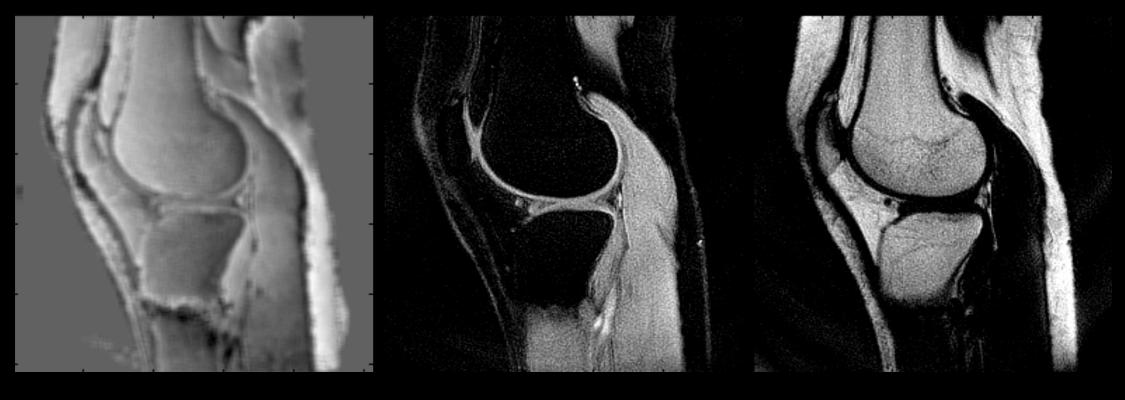


Regular recon

Field map

ORC image

## Concentric Rings with 3 Revolutions / TR



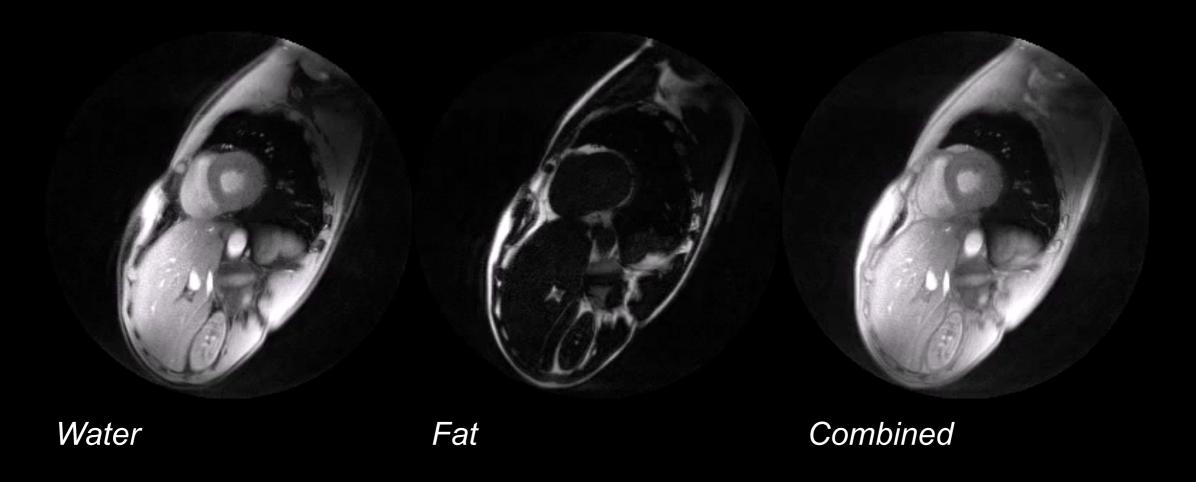
Field map

Water image

Fat image

### 1.5 T, 2D GRE, Cardiac F/W Cine

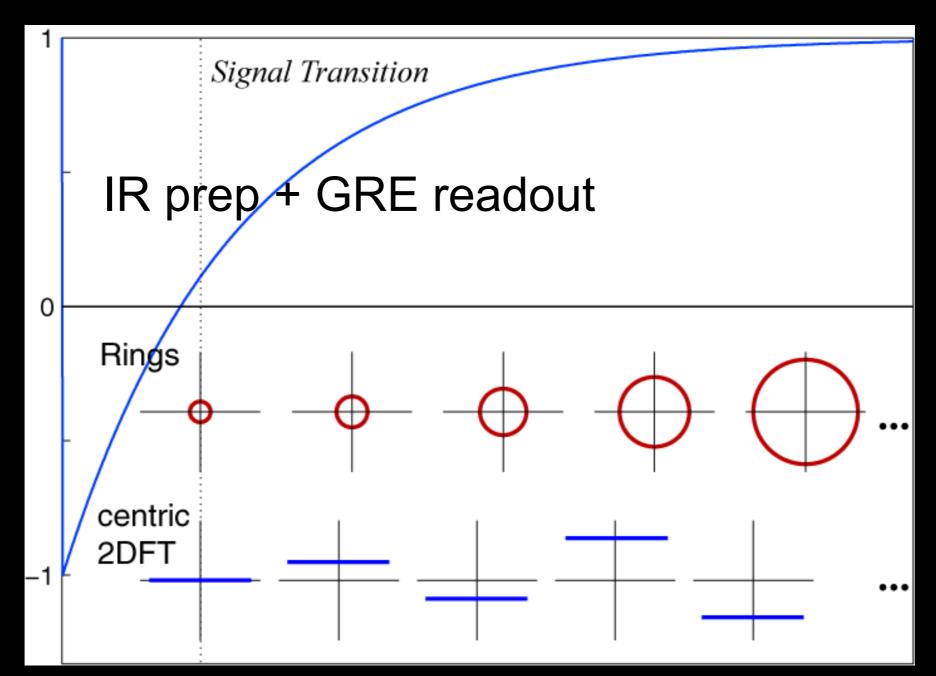
13-HB BH scan (with add'l 3-fold k-t BLAST acceleration)



## Rings: Magnetization-Prepared MRI

### Inherent 2D centric ordering

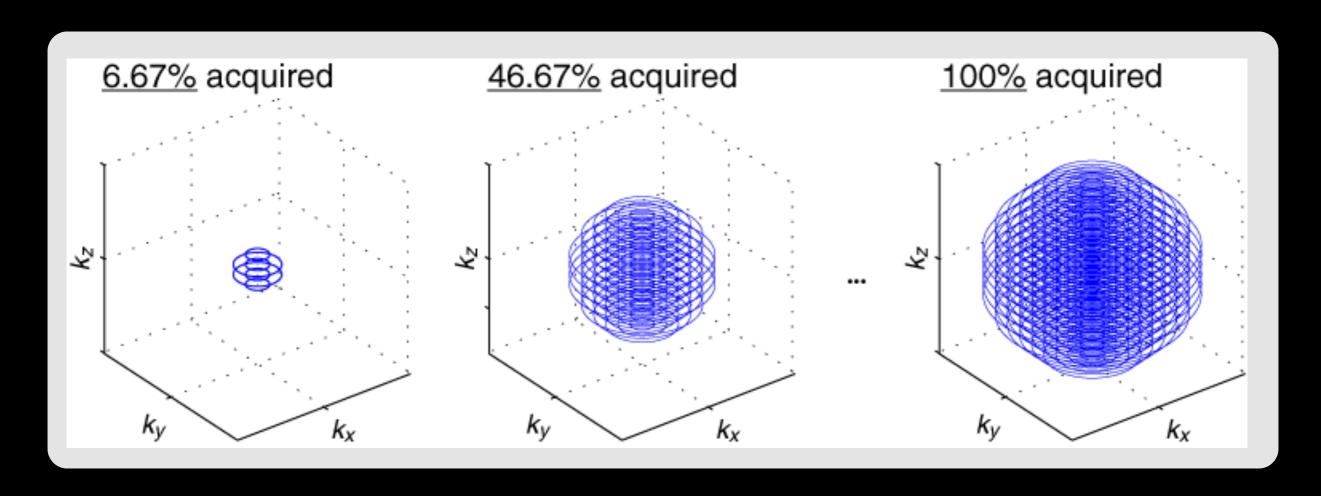
- improved mag-prep contrast and k-space weighting



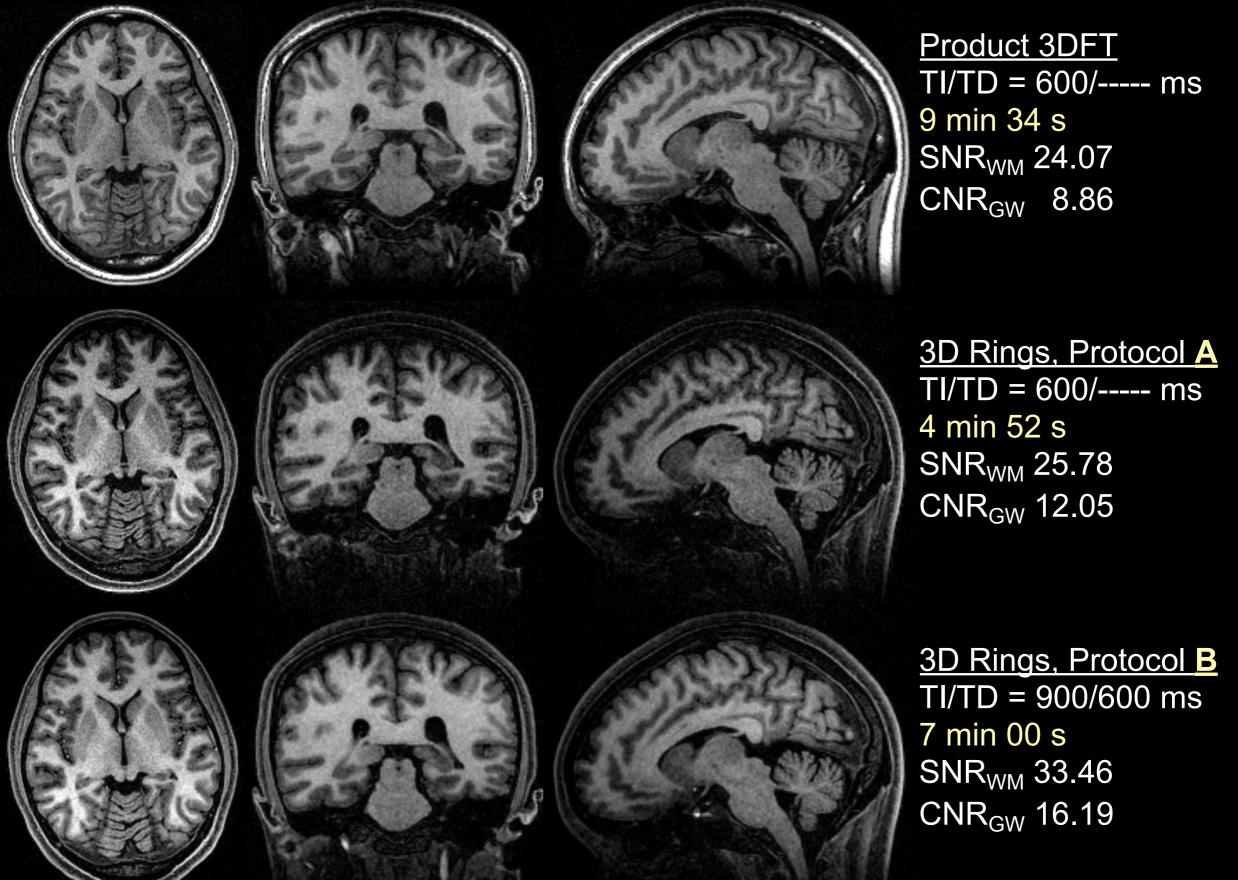
## Rings: 3D Mag-Prep MRI

## Fully 3D centric ordering

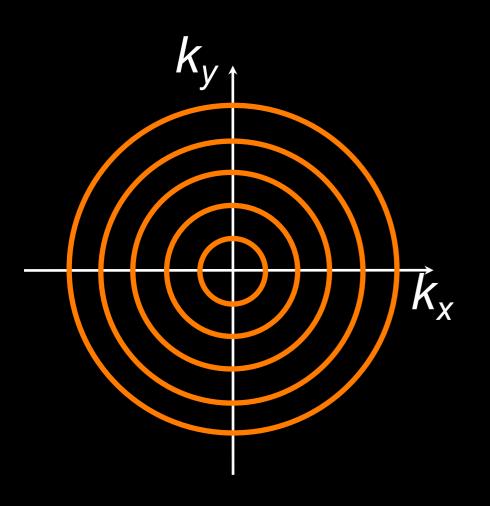
- improved mag-prep contrast and k-space weighting
- spherical k-space coverage saves time



## Rings: 3D Mag-Prep MRI



## Rings: Pros and Cons



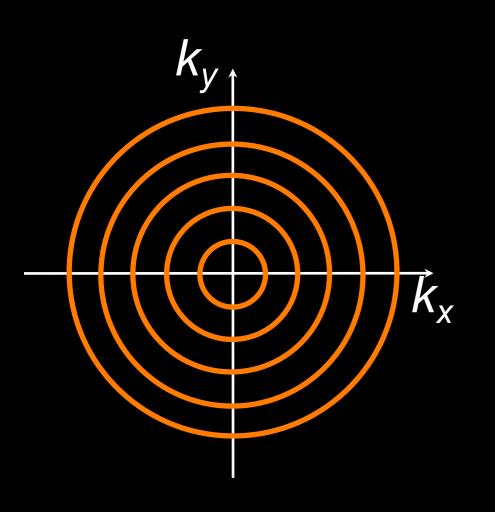
#### **Pros**

- 2x reduction in #TRs (vs. Cartesian)
- Favorable motion/flow properties
- Robust to gradient delays
- Efficient spatial/spectral encoding
- Effective for mag-prep MRI

#### Cons

- SNR penalty (non-uniform density)
- Scale-down design not optimal

## Rings: Extensions



Variable density sampling

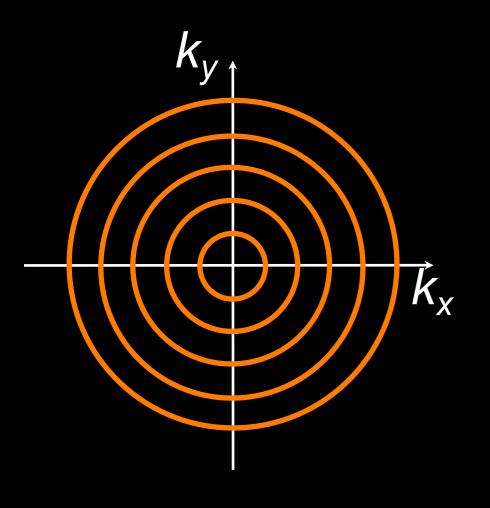
Multiple rings per TR

3D concentric cylinders

Parallel imaging

Partial Fourier

# Rings: Applications



### Fast imaging

- Cardiac MRI

### Chemical shift imaging

- Fat/water separation
- MR spectroscopic imaging

### Mag-prep imaging

- Neuro MRI
- Non-con MR angiography (MRA)
- Contrast-enhanced MRA

# Non-Cartesian Sampling

#### Benefits

- Reduced scan time
- Robustness to motion and flow
- Short echo time

### Applications

- Dynamic MRI
- Real-time MRI
- Cardiovascular MRI
- Short-TE MRI

### Challenges

- Hardware performance
- Gradient fidelity
- Off-resonance effects
- Implementation
- Challenges addressed
- On-going research
- Use judiciously!

## Thanks!

- Further reading
  - Bernstein et al., Handbook of MRI Sequences
- Next week
  - Spiral, 3D Non-Cartesian trajectories
  - Gridding reconstruction
  - Trajectory measurement
  - Off-resonance correction

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http://mrrl.ucla.edu/wulab