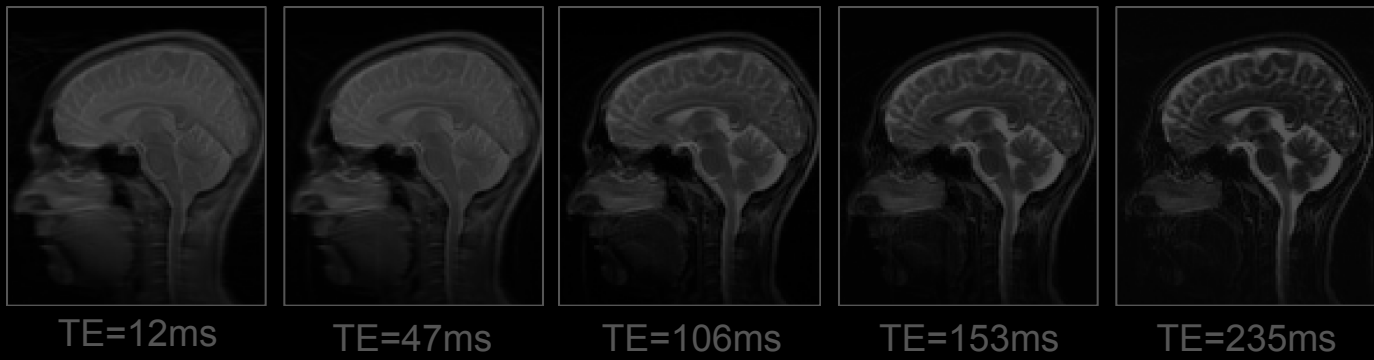


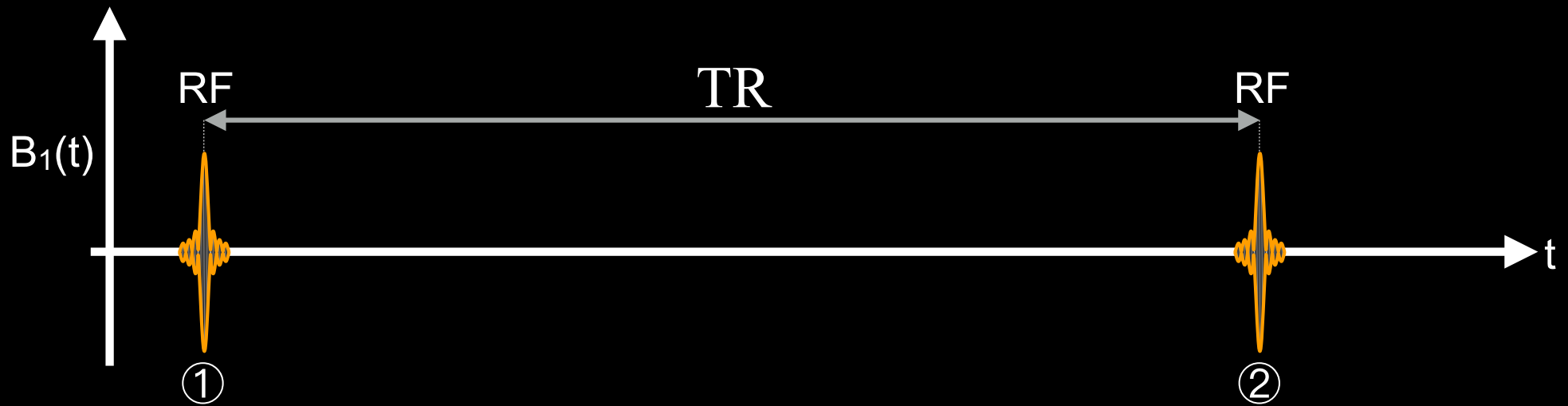
# Basic Pulse Sequences II - Spin Echoes



David Geffen  
School of Medicine

**UCLA**  
Radiology

# Lecture #6 Summary



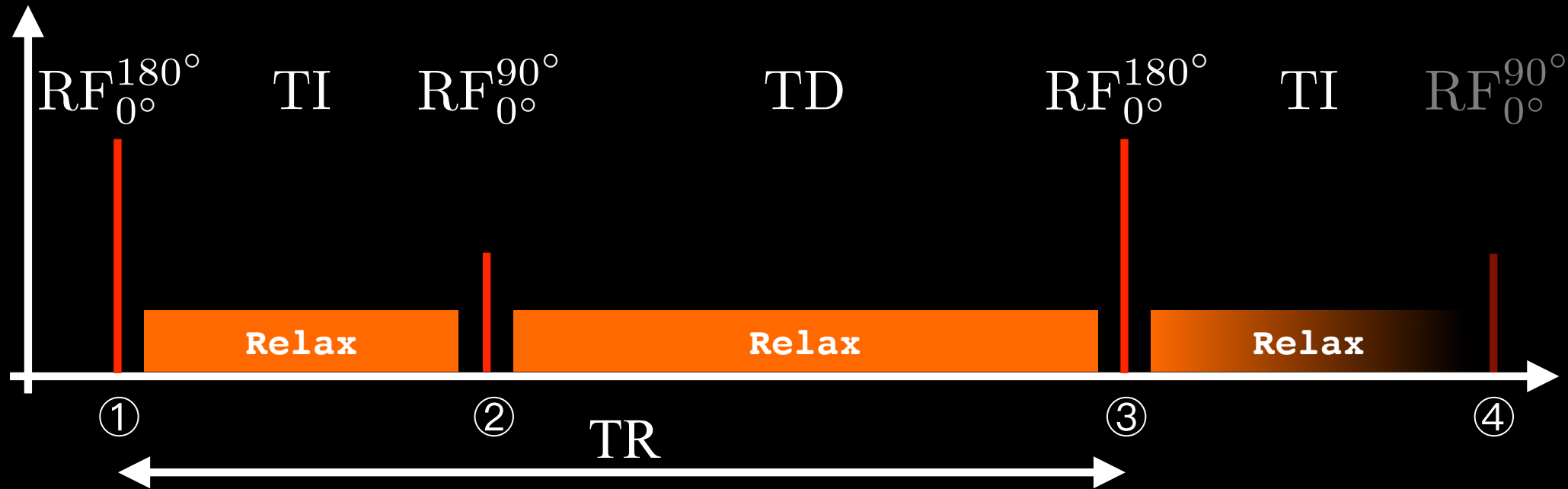
$$\vec{M}^{(1)}(0_-) = \vec{M}_0 = \begin{bmatrix} 0 \\ 0 \\ M_0 \end{bmatrix} \quad \text{Initial Condition}$$

$$\vec{M}^{(1)}(0_+) = RF_\theta^\alpha \vec{M}^{(1)}(0_-) \quad \text{Forced Precession}$$

$$\vec{M}^{(2)}(0_-) = E(T_1, T_2, TR) \vec{M}^{(1)}(0_+) \quad \text{Free Precession}$$

$$\vec{M}^{(2)}(0_+) = RF_\theta^\alpha \vec{M}^{(2)}(0_-)$$

# Inversion Recovery



$$(180^\circ - \text{TI} - 90^\circ - \text{TD})_N$$

# IR Contrast

$$A_{fid} \propto \rho \left( 1 - 2e^{-TI/T_1} + e^{-TR/T_1} \right)$$

$$I(\vec{r}) \propto \rho(\vec{r}) \left( 1 - 2e^{-TI/T_1(\vec{r})} + e^{-TR/T_1(\vec{r})} \right) \text{ Eqn. 7.21}$$

The final image is the product of  $\rho(r)$  and  $f(T_1(r))$ .

The final image contrast is controlled by TI and TR.



# IR Signal Nulling Effect

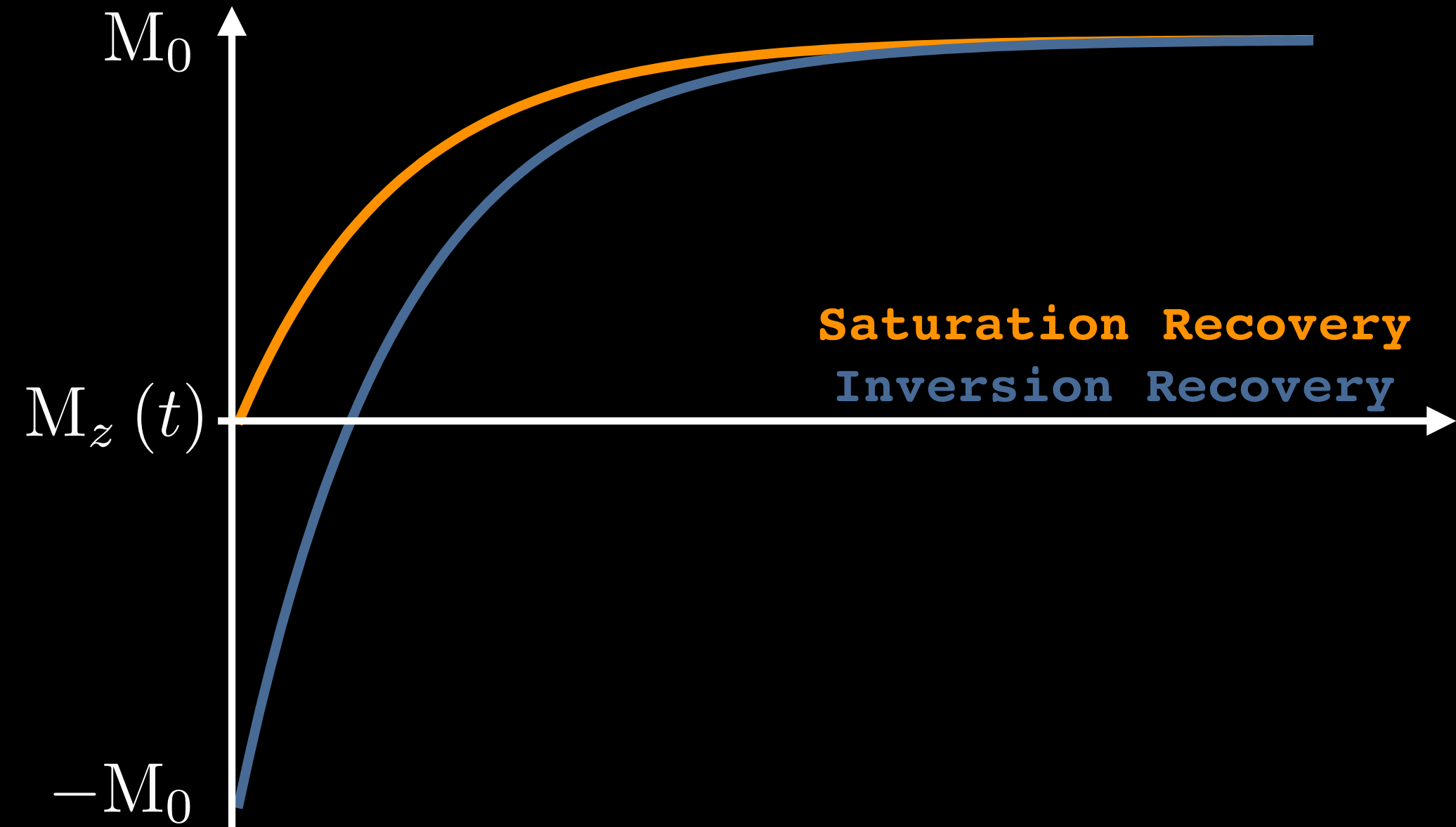
$$TI_{null} = \left[ \ln 2 - \ln \left( 1 + \exp^{-TR/T_1^0} \right) \right] T_1^0$$

Target  $T_1$   
↓

$$TI_{null} = [\ln 2] T_1^0, \text{ if } TR \longrightarrow \infty$$

$$I(\vec{r}) = 0, \text{ if } T_1(\vec{r}) = T_1^0(\vec{r})$$

# SR vs. IR



# Inversion Pulse - Applications

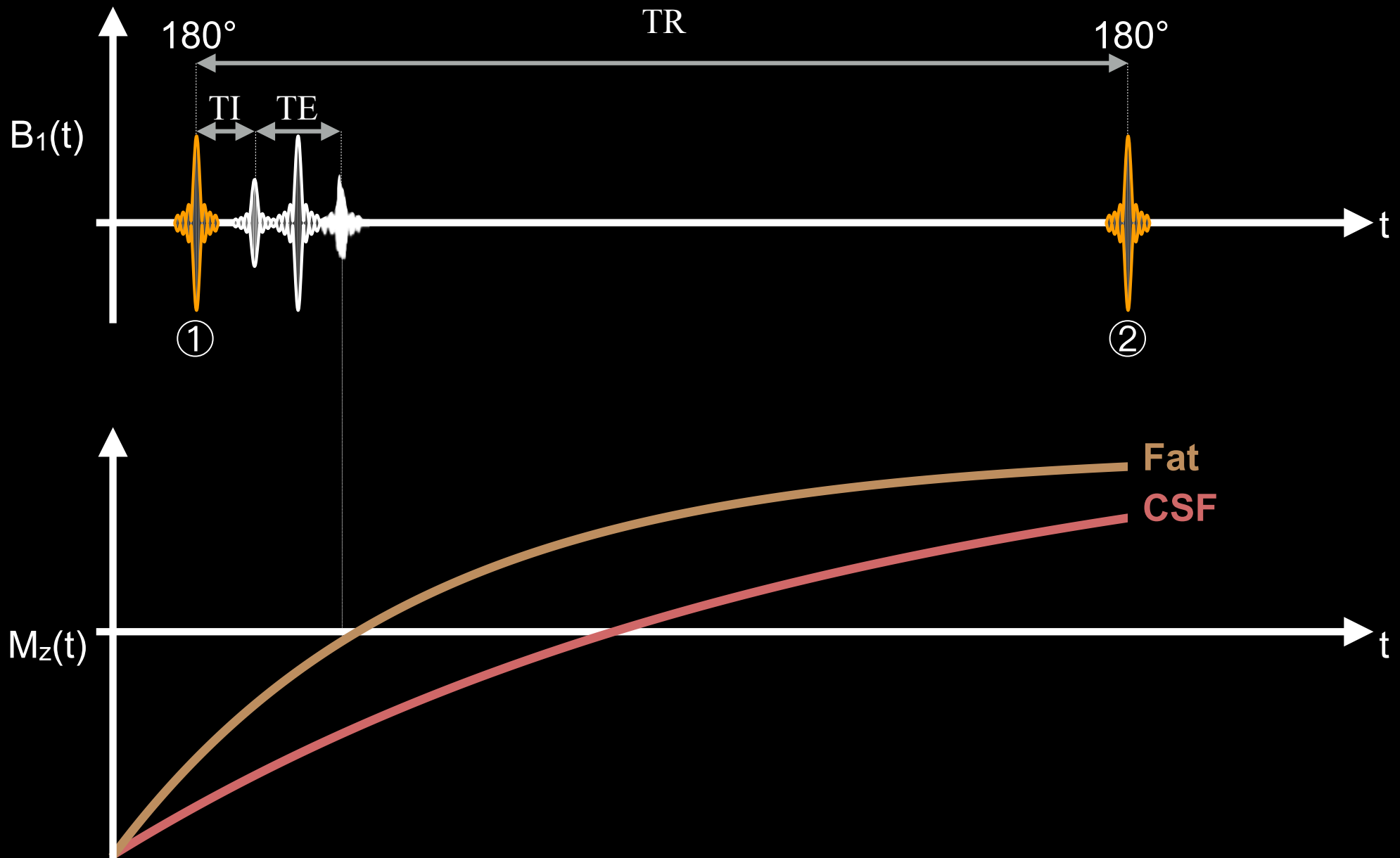
- Greater  $T_1$  contrast than SR
- $T_1$  species nulling/attenuation
  - FLAIR (Fluid Attenuated Inversion Recovery)
  - STIR (Short Tau Inversion Recovery)
- IR is better than SR for generating contrast when:
  - $\rho(A)=\rho(B)$  and  $T_2(A)=T_2(B)$
  - AND
  - $T_1(A)$  and  $T_1(B)$  are slightly different
- Quantitative  $T_1$  mapping

$$I(\vec{r}) \propto \rho(\vec{r}) \left( 1 - 2e^{-TI/T_1(\vec{r})} + e^{-TR/T_1(\vec{r})} \right) \text{Eqn. 7.21}$$

The final image is the product of  $\rho(r)$  and  $f(T_1(r))$ .

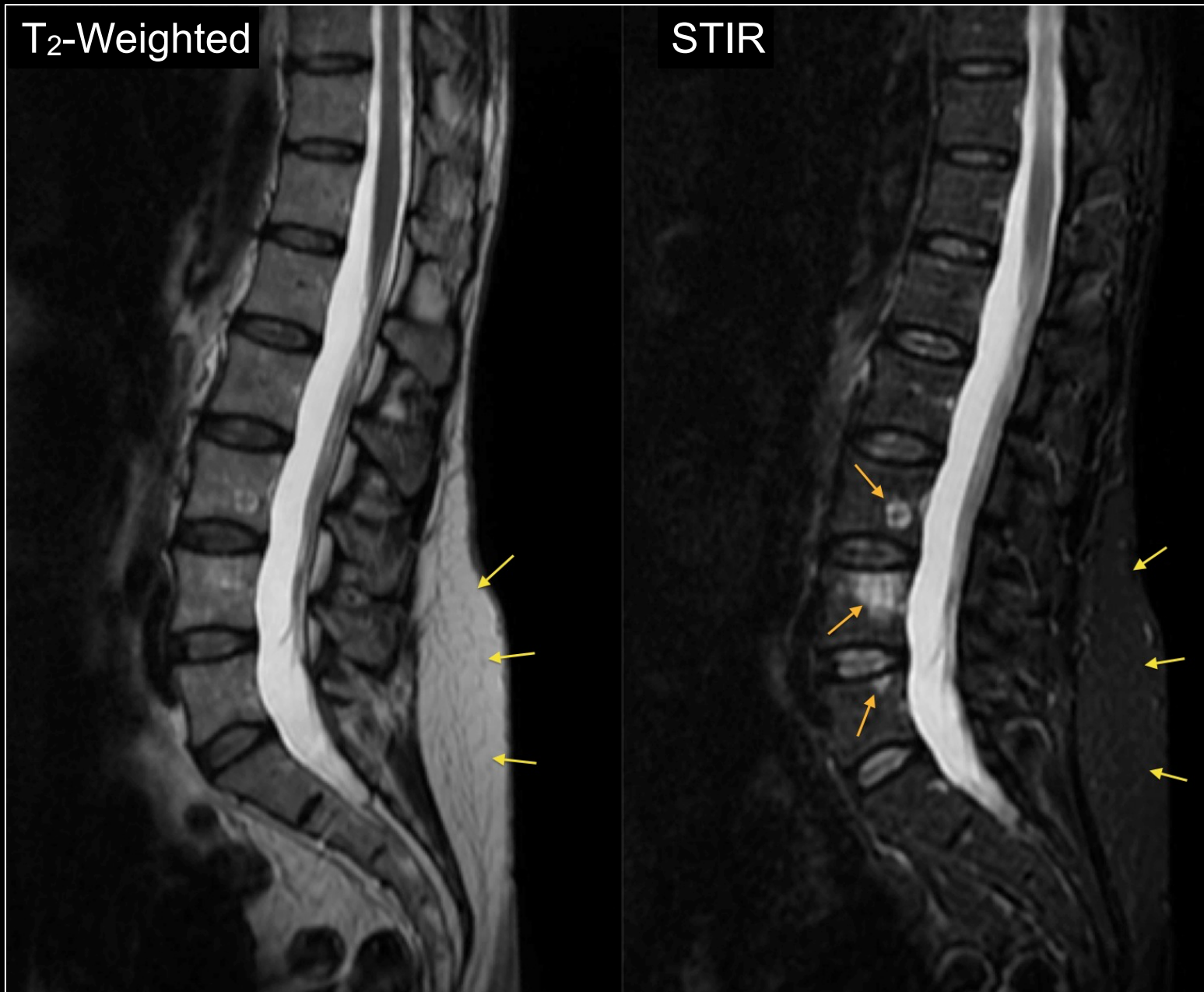
The final image contrast is controlled by TI and TR.

# STIR Pulse Sequence

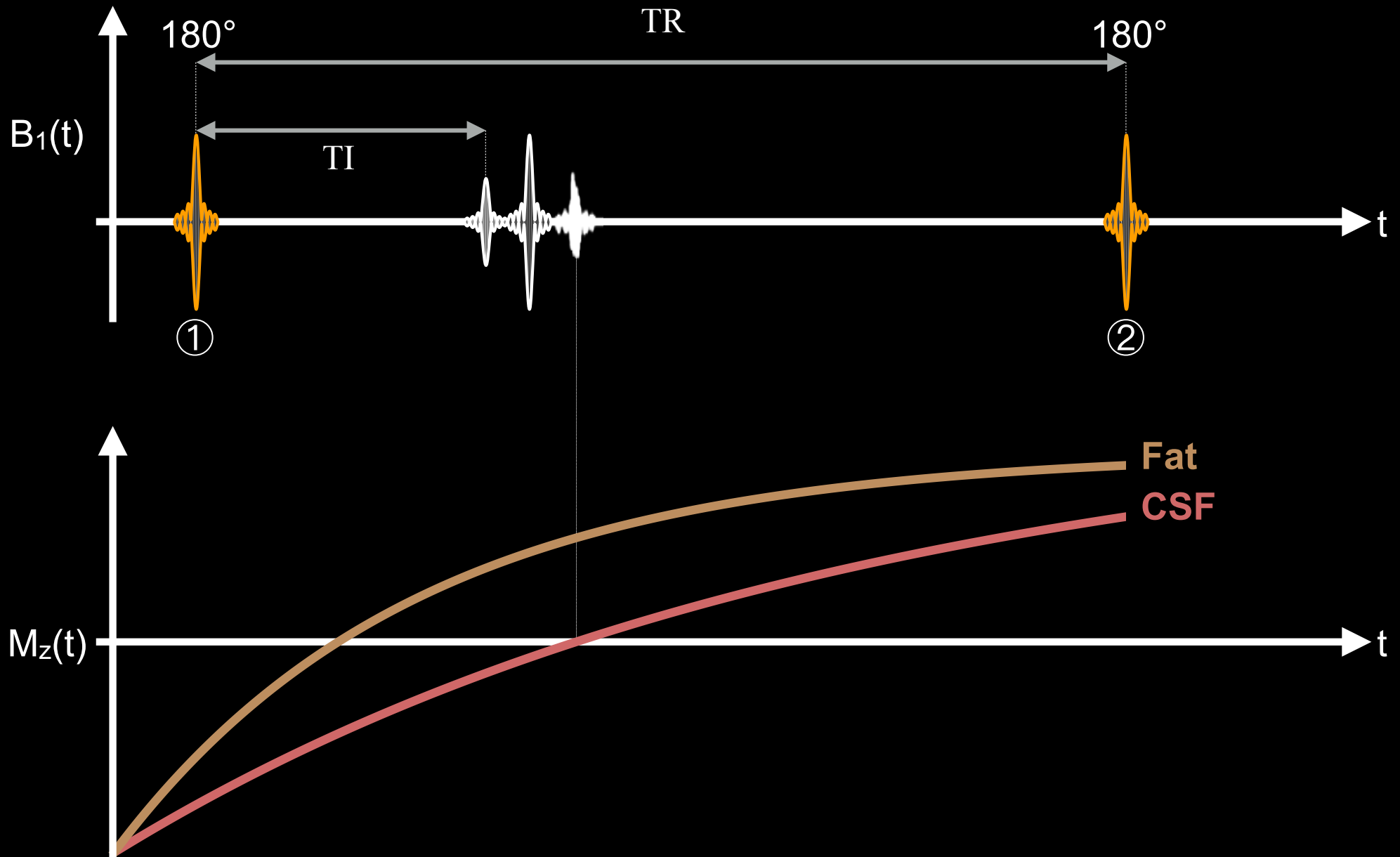


Short Tau Inversion Recovery (STIR) is used to null fat.

# STIR Images



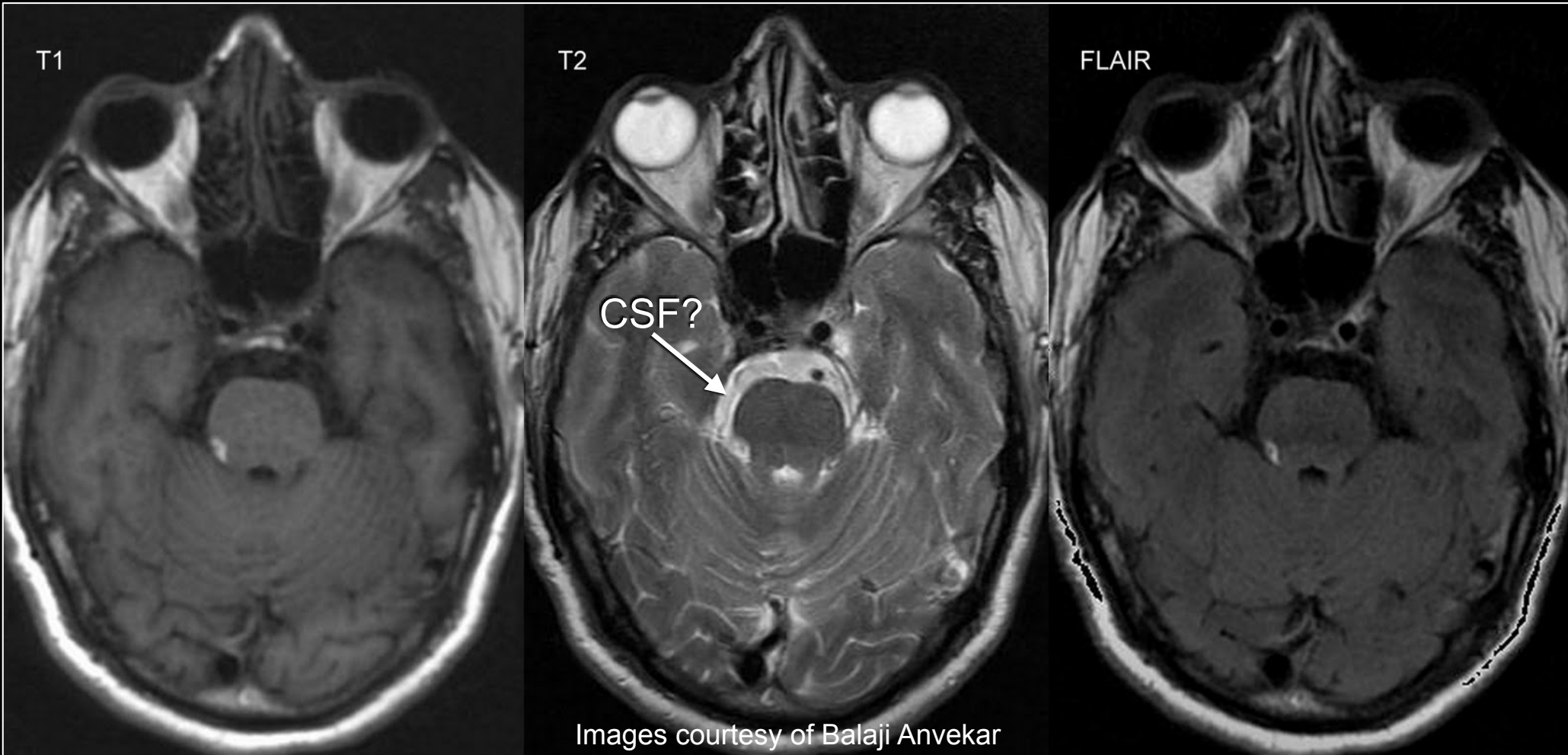
# FLAIR Pulse Sequence



Fluid Attenuated Inversion Recovery (STIR) is used to CSF.

# FLAIR Images

FLAIR can distinguish fat from CSF.



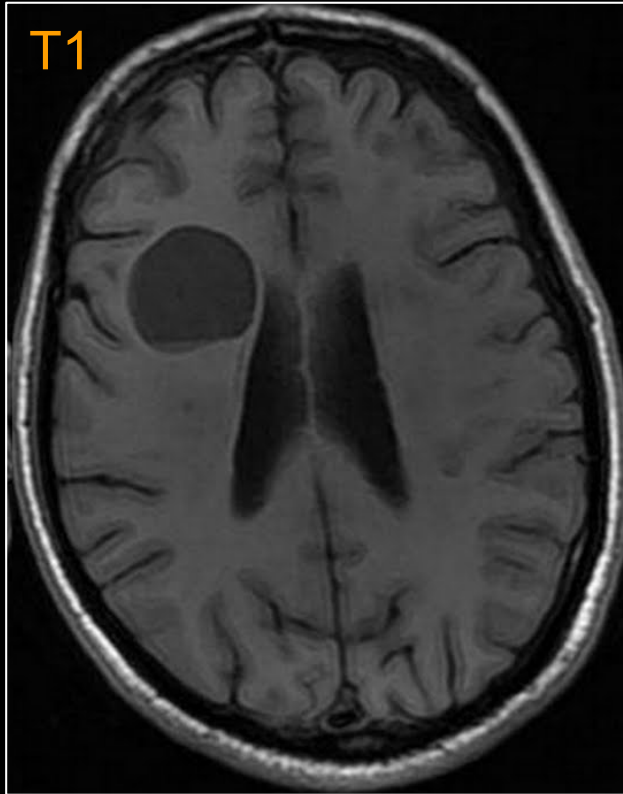


# FLAIR Images

Long T2 is bright on T2w.



Short T1 is bright on T1w.



Long T1 is dark on FLAIR.



Lesion has long T2 and intermediate T1. Not fat. Not CSF. Cerebral hydatid.



# Lecture #6 Learning Objectives

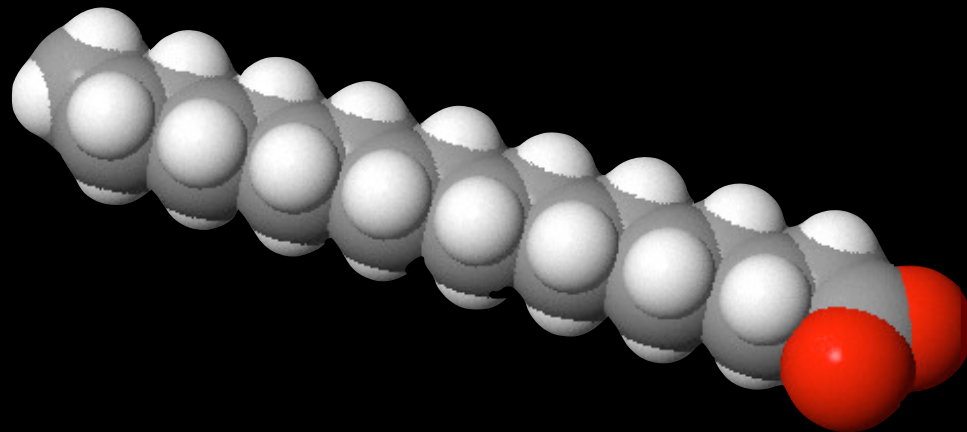
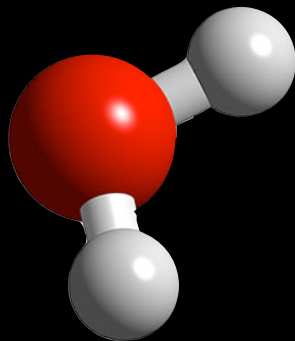
- **Appreciate the definition of image contrast.**
- **Explain what a T1 or T2-weighted image is.**
- **Describe what a pulse sequence is.**
- **Understand the saturation recovery pulse sequence and the saturation condition.**
- **Describe the inversion recovery sequence.**
- **Distinguish between STIR and FLAIR.**

Off-Resonance

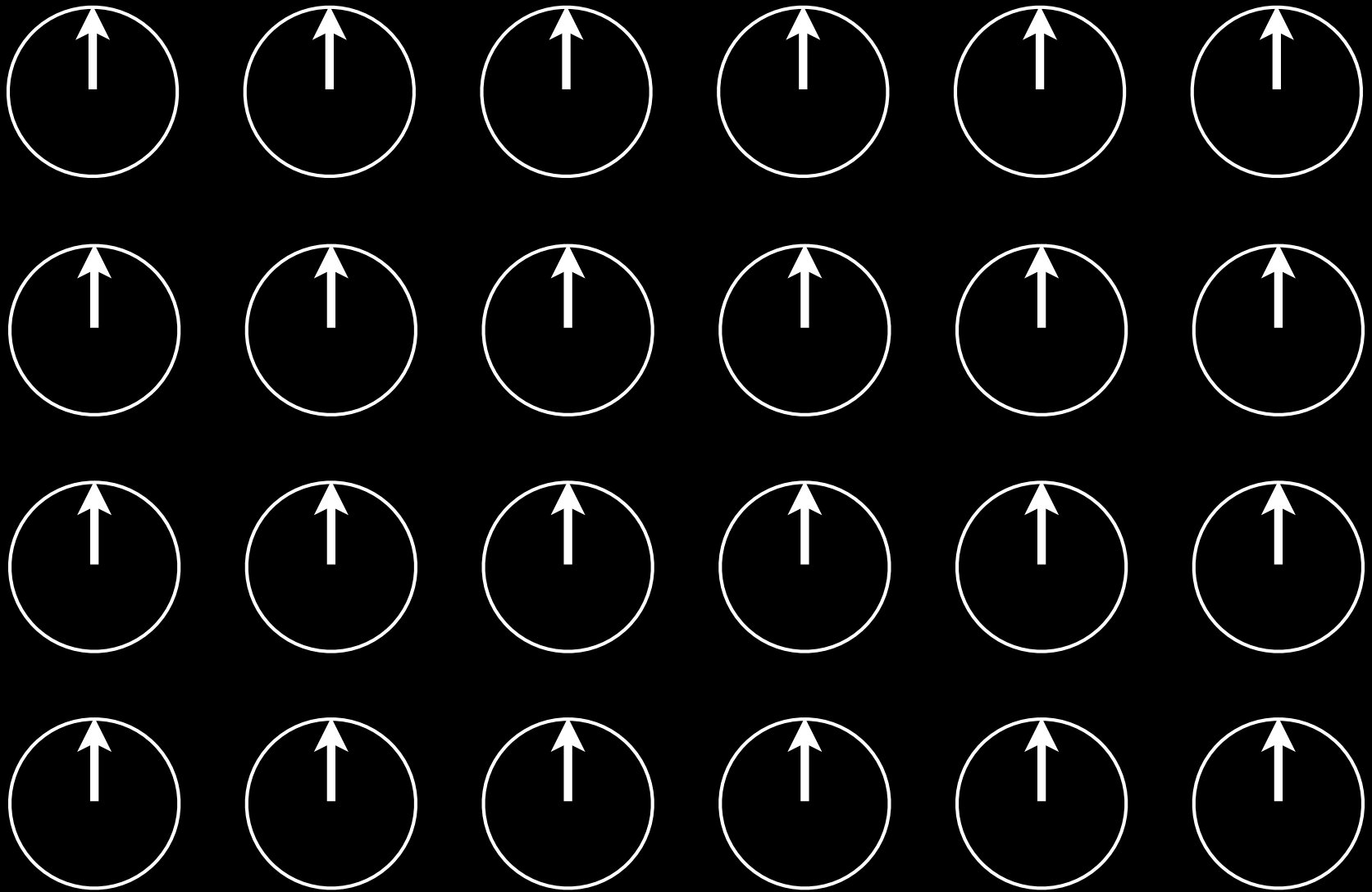
# Isochromats

- ***Isochromat*** - Group of nuclear spins with the same resonant frequency
- Ideally all spins in a “system” have the same resonance frequency
- Multiple isochromats arise from:
  - $B_0$  inhomogeneity (heterogeneity!)
  - Chemical shift effects
  - Magnetic susceptibility differences
  - Gradients

Sources of  
Off-resonance



# Isochromats



# Isochromats



# $B_0$ Inhomogeneity

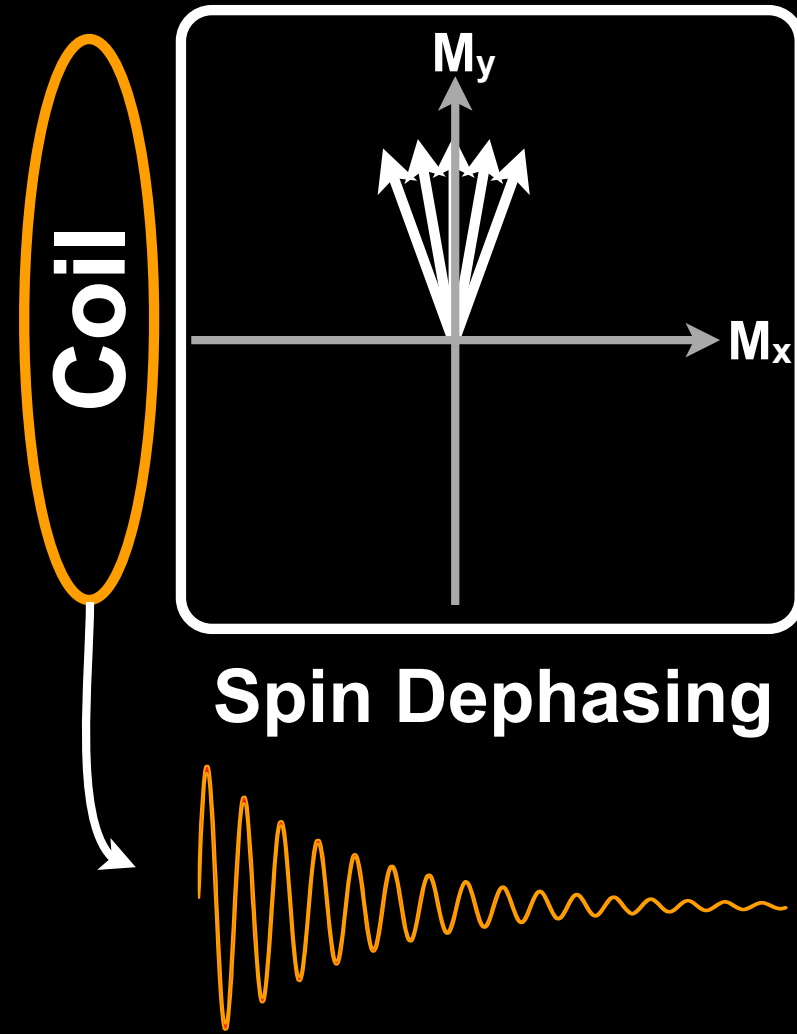
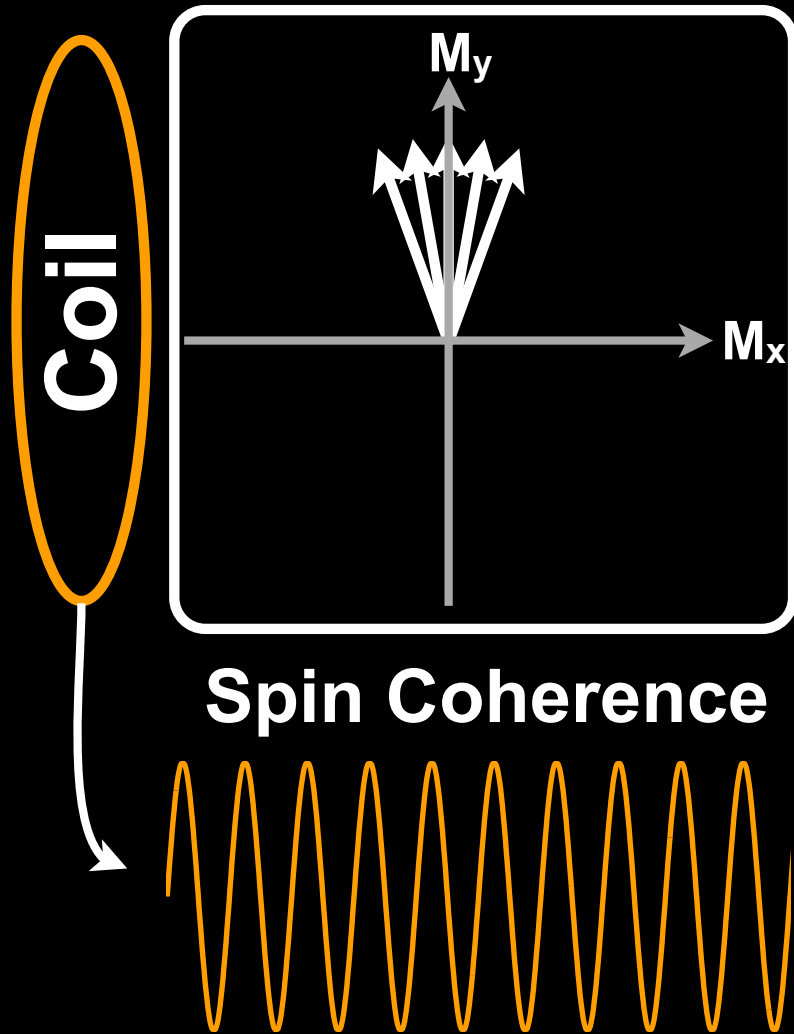
# Spin Dephasing

- Intravoxel spin dephasing from:
  - **Off-resonance**
    - $B_0$  inhomogeneity
    - Chemical shift effects
    - Susceptibility differences (macro and micro)
      - Blood products (**iron**)
      - Blood oxygenation levels
  - Applied gradients
    - Strong gradients produce more spin dephasing
- ... leads to:
  - Loss of spin phase coherence
  - Usually within a voxel
  - Leads to a decreased echo amplitude.
- Minimized by:
  - Field shimming
  - Susceptibility manipulation
  - Refocusing pulses

# Intravoxel Spin Dephasing

*Homogenous* Intravoxel Field

*Inhomogenous* Intravoxel Field



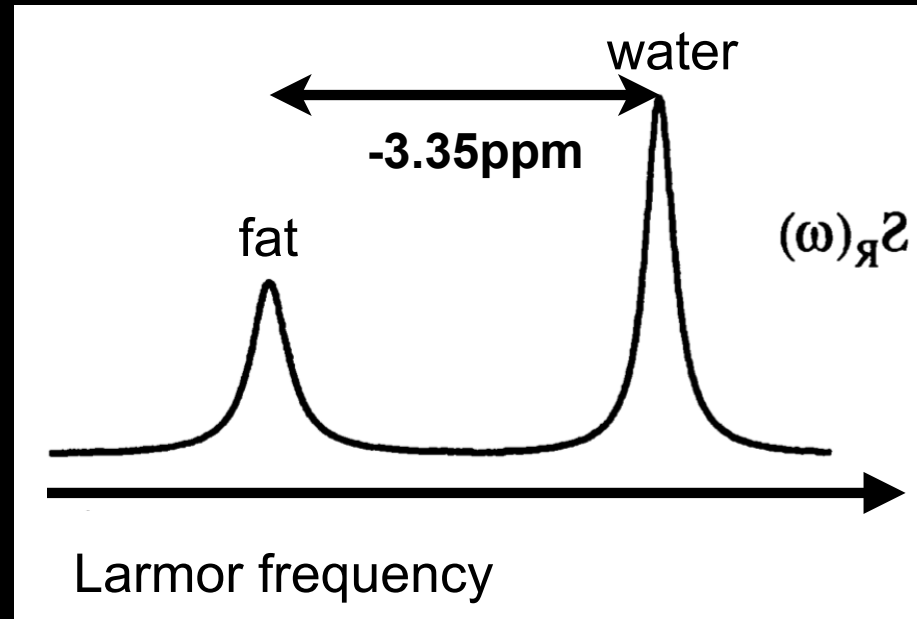
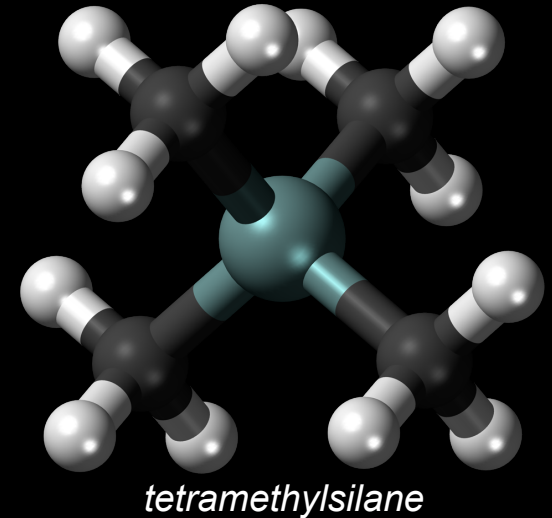
**Signal loss from spin dephasing and  $T_2^*$ .**



# Chemical Shift

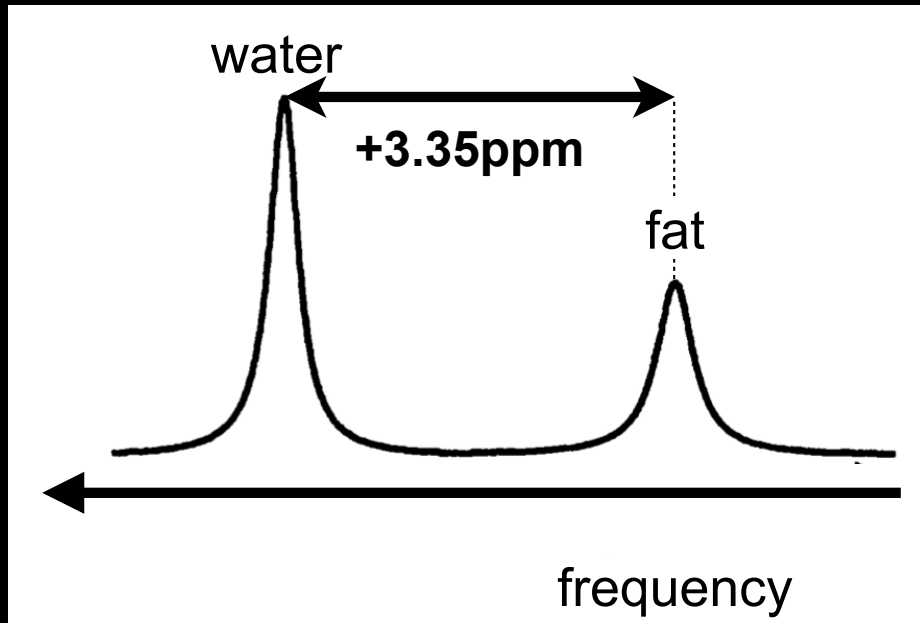
# Chemical Shift

- Nuclear (eg  $^1\text{H}$ ) spins surrounded by different chemical environments
- Orbiting electrons shield the nucleus
- Referenced against tetramethylsilane
  - Assigned a chemical shift of zero

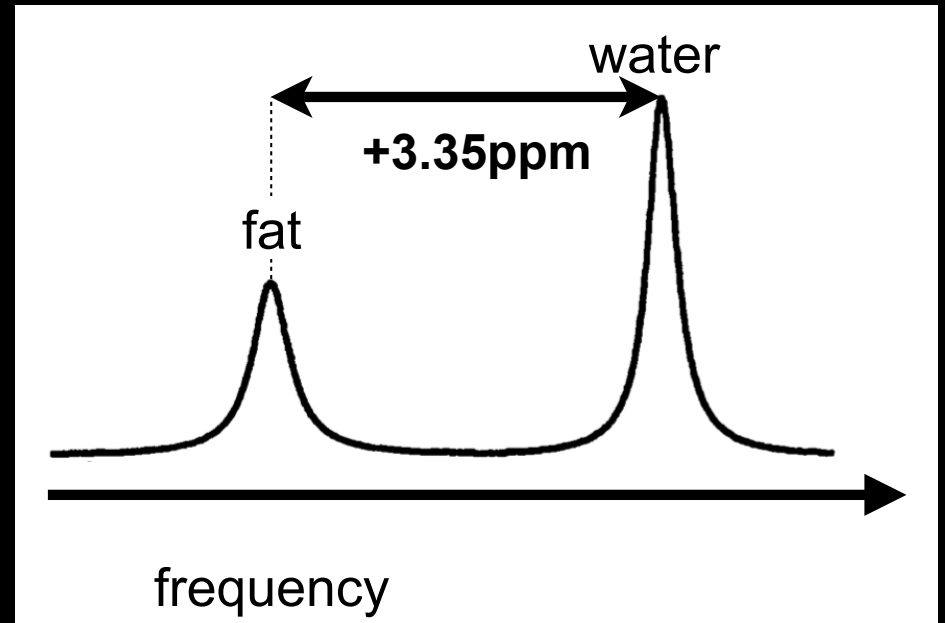


$-\text{CH}_2$  is 214Hz lower at 1.5T

# Chemical Shift



Chemists



Physicists

$$B = B_0 (1 - \delta)$$

$$\delta_{-\text{CH}_2} = 3.35\text{ppm}$$

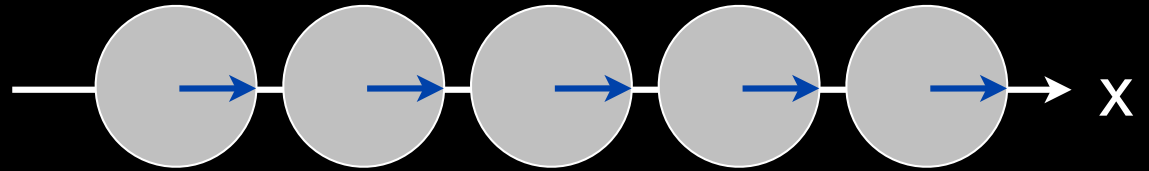
$-\text{CH}_2$  is 214Hz *lower* at 1.5T

# Chemical Shift

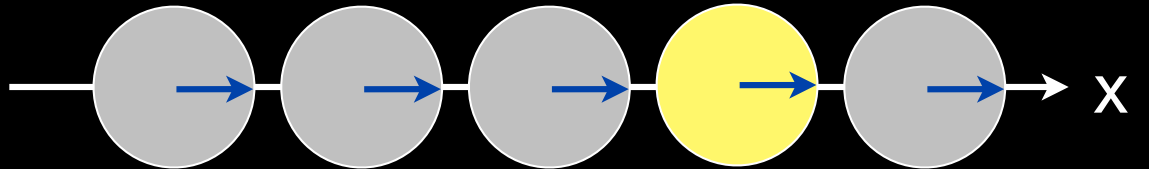
Type of Proton	Structure	Chemical Shift, ppm
Cyclopropane	$C_3H_6$	0.2
Primary	$R-CH_3$	0.9
Secondary	$R_2-CH_2$	1.3
Tertiary	$R_3-C-H$	1.5
Vinylic	$C=C-H$	4.6-5.9
Acetylenic	triple bond, $CC-H$	2-3
Aromatic	$Ar-H$	6-8.5
Benzylic	$Ar-C-H$	2.2-3

# Chemical Shift Artifact

Normal Spins



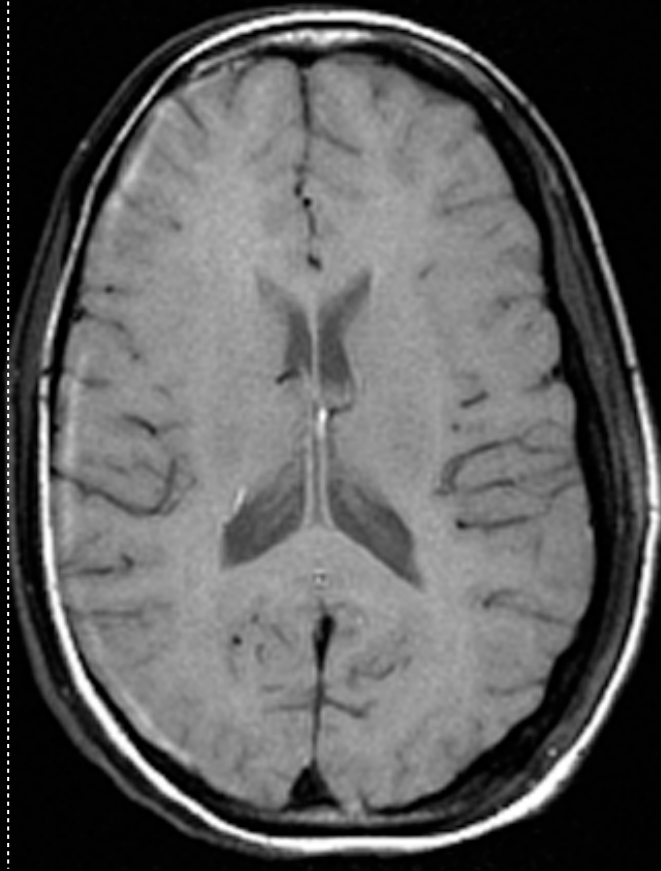
Off-Resonant Spin



Frequency is linearly related to spatial position.

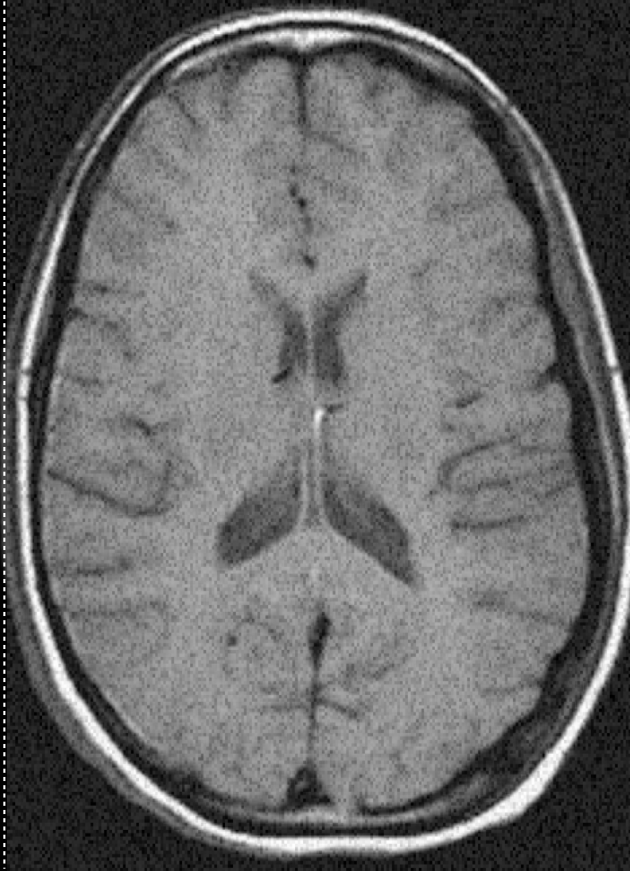
# Chemical Shift Artifact

Readout →

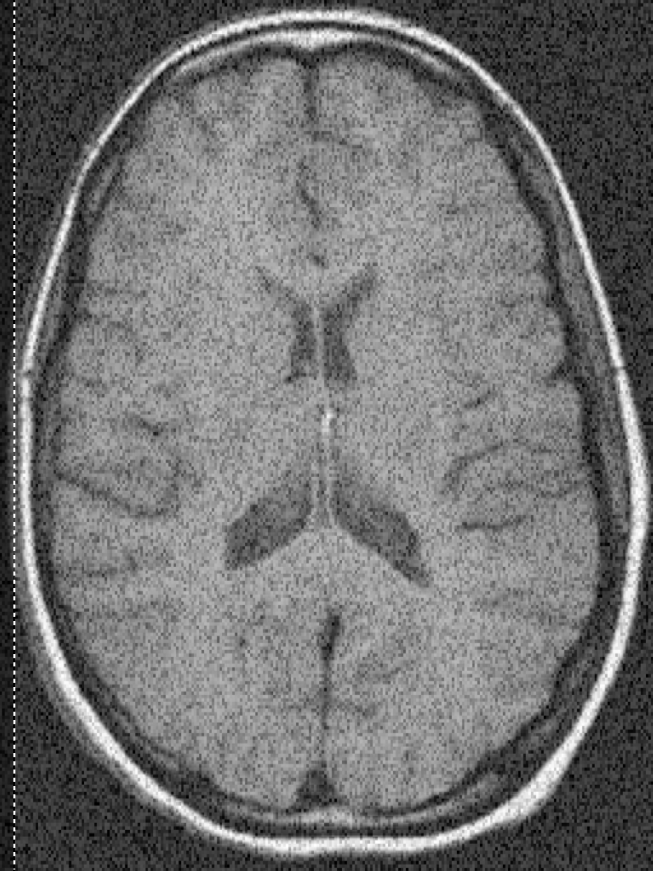


$\text{BW} = \pm 4\text{kHz}$

**Low Bandwidth  
Large Fat-Water Shift  
High SNR**



$\text{BW} = \pm 8\text{kHz}$



$\text{BW} = \pm 16\text{kHz}$

**High Bandwidth  
Small Fat-Water Shift  
Low SNR**

# Magnetic Susceptibility

# Magnetic Susceptibility ( $\chi$ )

- Ability of a substance to become magnetized
  - (–) Susceptibility - slightly decreases the magnetic field
    - Its magnetization is oppositely directed
  - (+) Susceptibility - slightly increases the magnetic field
    - Its magnetization is parallel with the main field

$$B = (1 + \chi) B_0$$

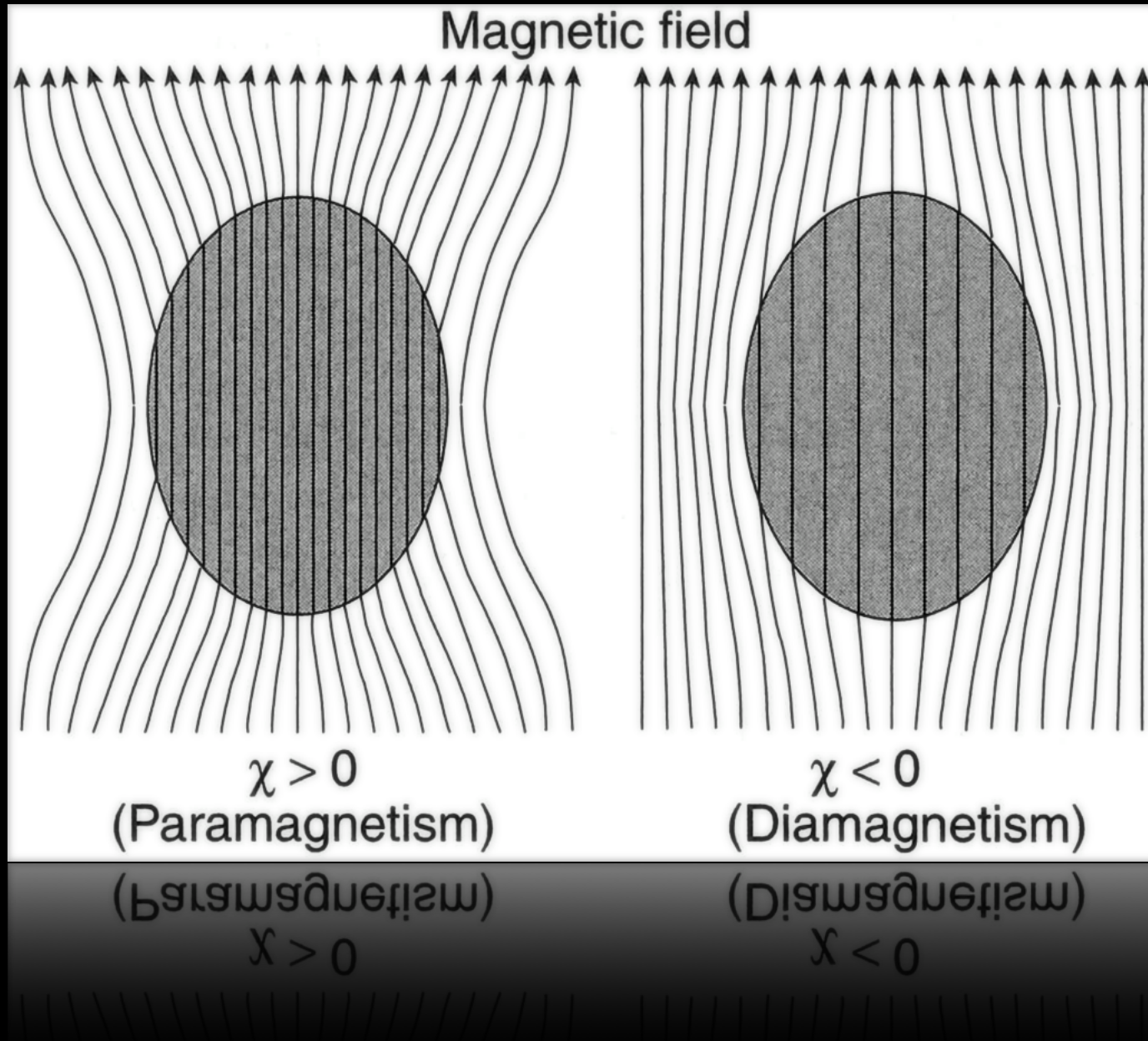
	Temperature [°C]	Pressure [atm]	$\chi$ [m <sup>3</sup> ·kg <sup>-1</sup> ]
Vacuum	Any	0	0
Water	20	1	$-9.04 \times 10^{-6}$
O <sub>2</sub>	20	0.209	$3.73 \times 10^{-7}$
N <sub>2</sub>	20	0.781	$-5.06 \times 10^{-9}$



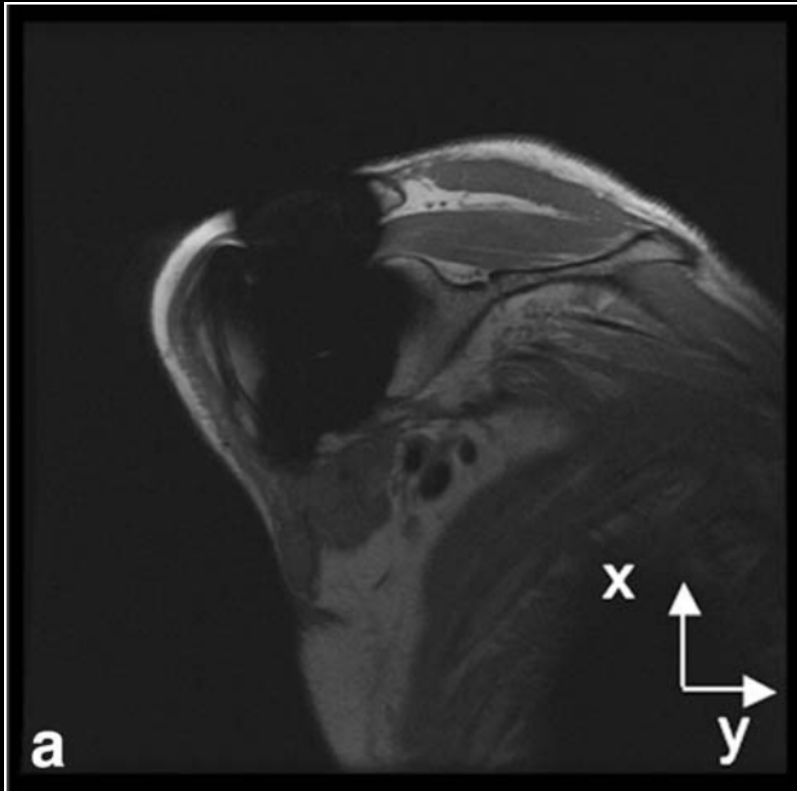
# Magnetic Susceptibility

- Diamagnetic - A substance with a small negative magnetic susceptibility
  - Oxyhemoglobin has a diamagnetism similar to tissue
- Paramagnetic - A substance with a small but positive magnetic susceptibility.
  - Deoxyhemoglobin more paramagnetic than tissue
- Ferromagnetic - A substance that has a large positive magnetic susceptibility.
  - Iron particles
- Large susceptibility gradients at:
  - Tissue-Air interfaces
  - Around metallic implants
  - Can cause large image artifacts

# Magnetic Susceptibility



# Metal Artifacts



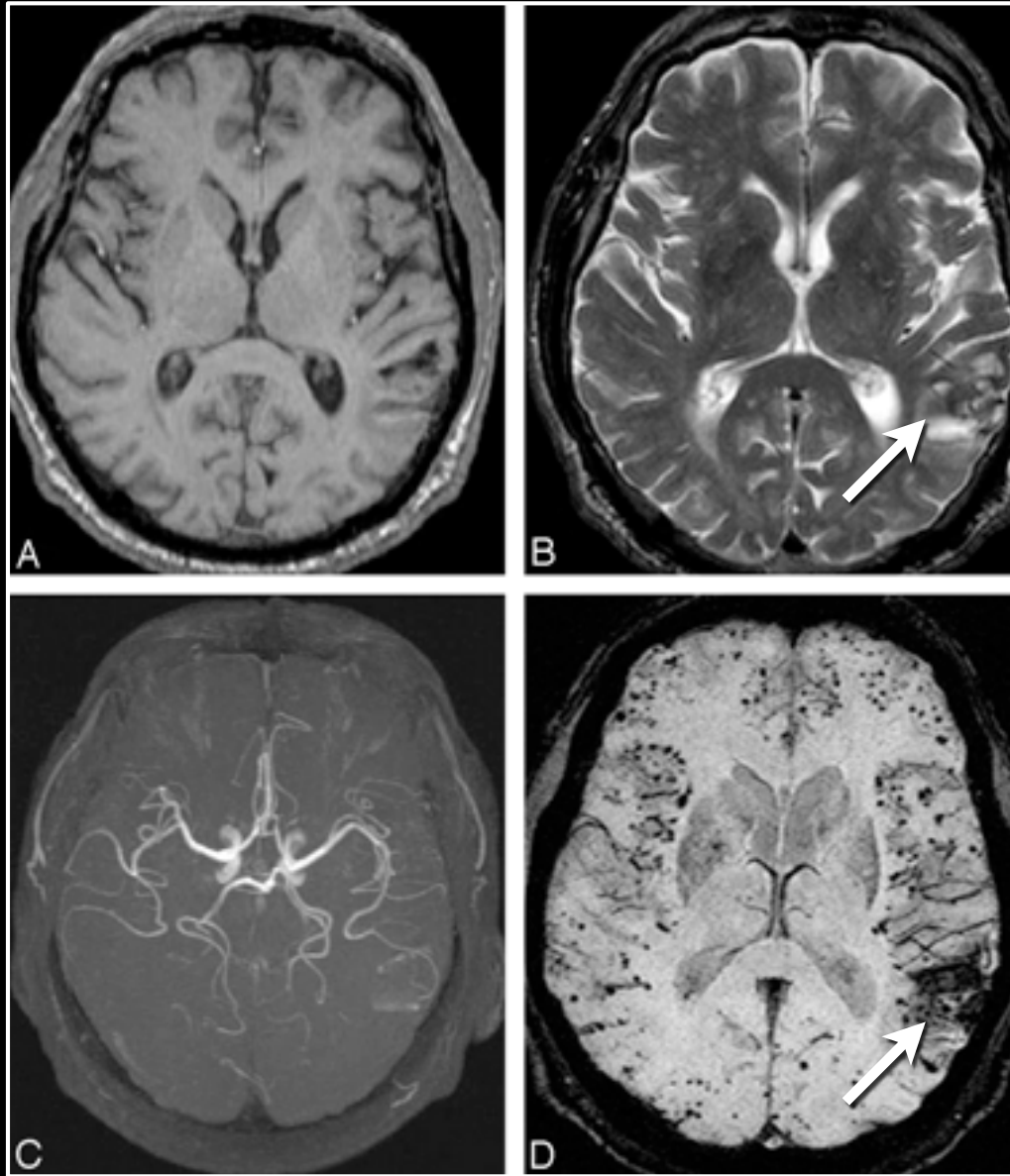
2D FSE of a shoulder.



3D FSE of a knee.

Koch KM et al. Imaging near metal with a MAVRIC-SEMAC hybrid. Magn Reson Med 2011;65(1):71-82 [PMID 20981709].

# Susceptibility Weighted Imaging (SWI)



Multiple microbleeds in cerebral amyloid angiopathy (CAA). A and B, T1-weighted (A) and T2-weighted (B) images do not reveal significant abnormalities except for the lesion in the left temporoparietal area. C, MRA shows normal brain vascular structure. D, SWI demonstrates, in addition to hemorrhage in the left temporoparietal region, **multiple microbleeds** distributed along the gray/white matter interface in the whole brain, strongly suggesting CAA.

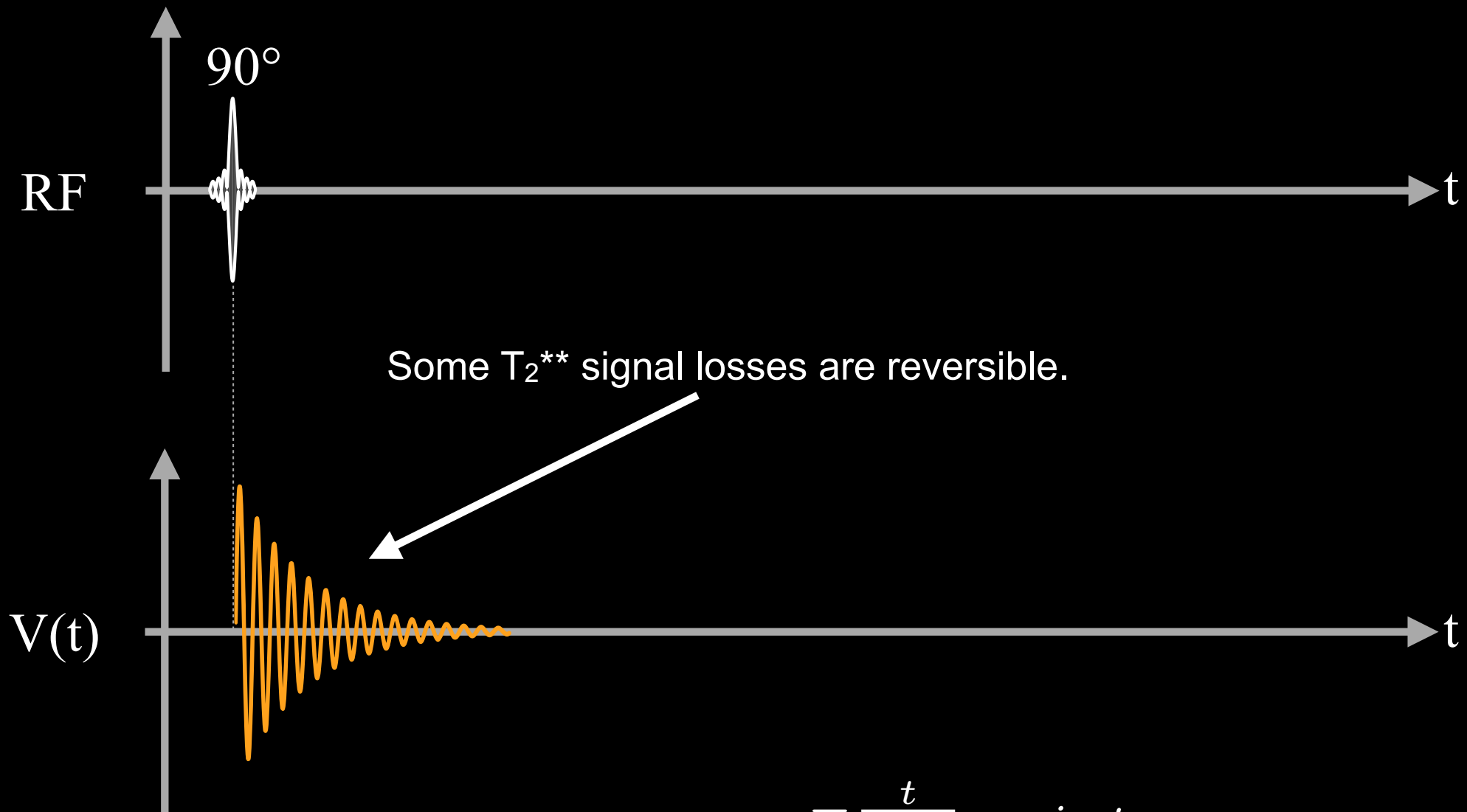
# Free Induction Decay

# Free Induction Decay (FID)

- **Free**
  - Signal arises from precession of bulk magnetization about  $B_0$  after perturbation
- **Induction**
  - Signal is induced in a coil (Faraday's Law)
- **Decay**
  - Decreases in amplitude over time
- **Characteristics:**
  - Amplitude maximum at  $t=0$
  - Decay rate depends on:
    - $T_2$ ,  $T_2^*$ , and spectral distribution ( $T_2^{**}$ )
      - ↑ Spin-level sources of off-resonance
      - ↑ Pixel-level sources of off-resonance

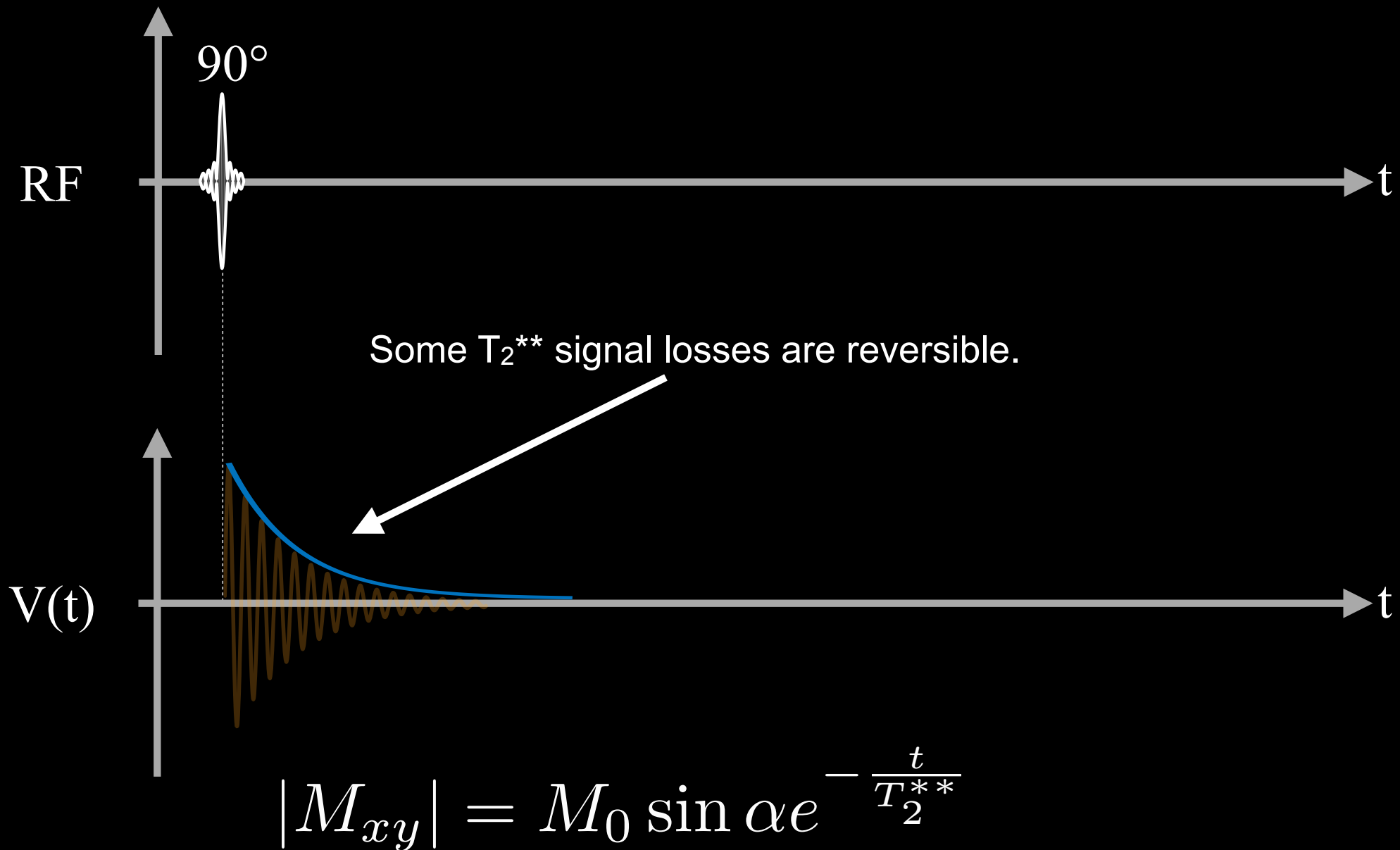


# Free Induction Decay (FID)



$$M_x = M_0 \sin \alpha e^{-\frac{t}{T_2^{**}}} e^{-i\omega t}$$

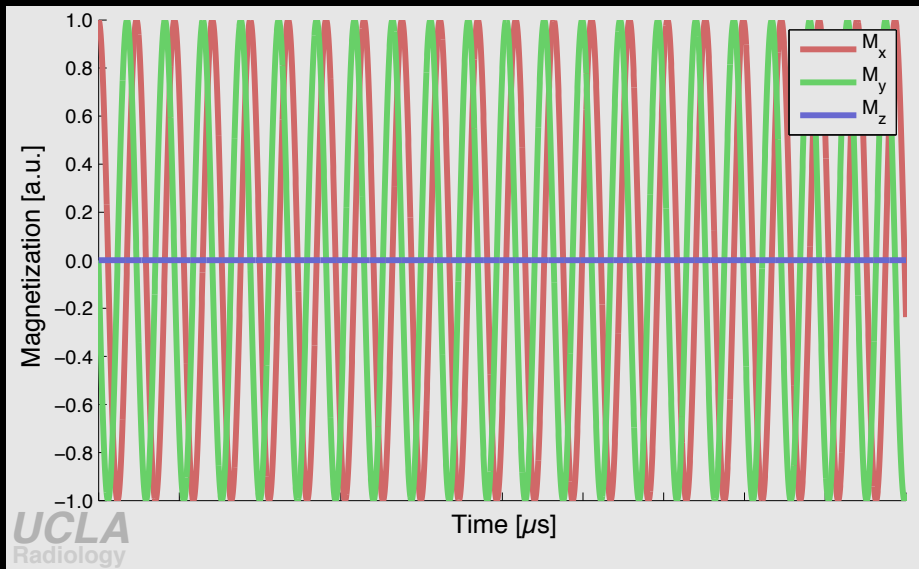
# Free Induction Decay (FID)



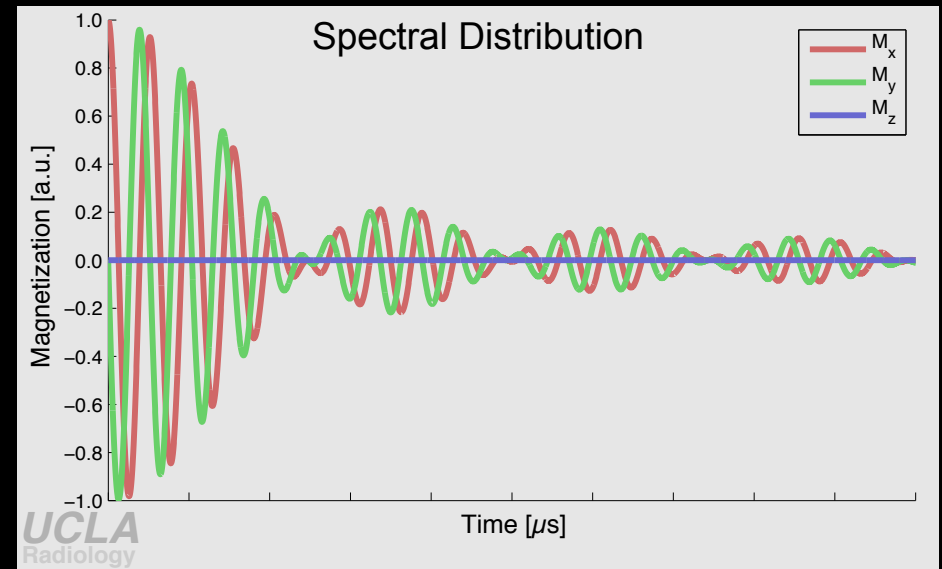


# Off-resonance Without Relaxation

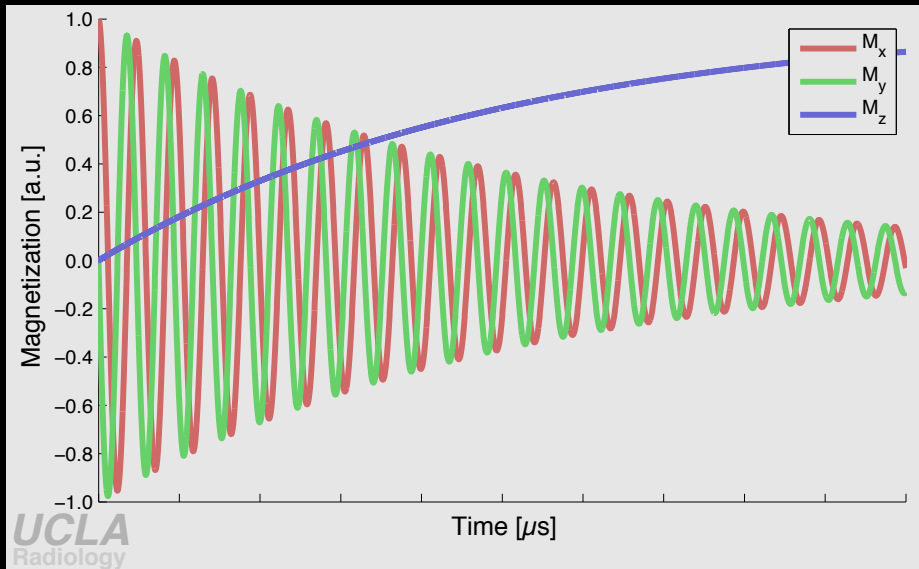
## Single Isochromat without Relaxation



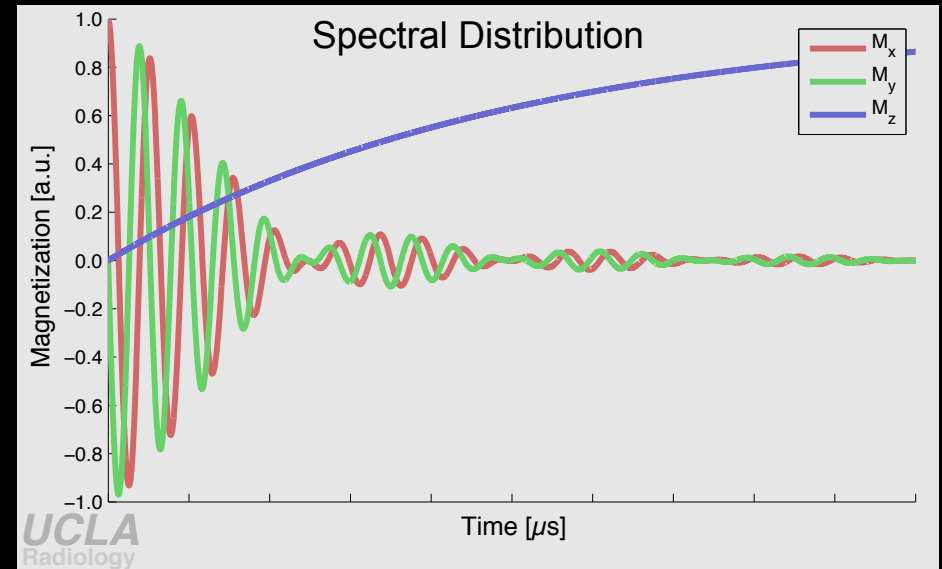
## 100 Isochromats without Relaxation



## Single Isochromat with Relaxation



## 100 Isochromats with Relaxation



# Signal Decay

- $T_2$ 
  - Irreversible spin-spin interactions
- $T_2^*$ 
  - $T_2$  plus...
  - Spin de-phasing due to spin-level off-resonance
  - Reversible
- $T_2^{**}$ 
  - $T_2^*$  plus...
  - Spin de-phasing due to voxel-level off-resonance
    - External field imperfections
  - Reversible

# $T_2^*$ Relaxation

- Intravoxel Spin Dephasing
  - Spin-spin ( $T_2$ ) dephasing combined with...
  - Off-resonance
    - $B_0$  inhomogeneity
      - Typically a few PPM over 30-50cm
        - » 1PPM = 640Hz = 1.5 $\mu$ T
    - Susceptibility differences (macro and micro)
      - Induce small field perturbations, therefore dephasing
    - Chemical shift effects
- Off-resonance can be rephased with a spin echo
  - Not with a gradient echo!
- $T_2^* < T_2$

# $T_2^*$ Relaxation

$$\frac{1}{T_2^*} = \frac{1}{T_2} + \gamma \delta B_0$$

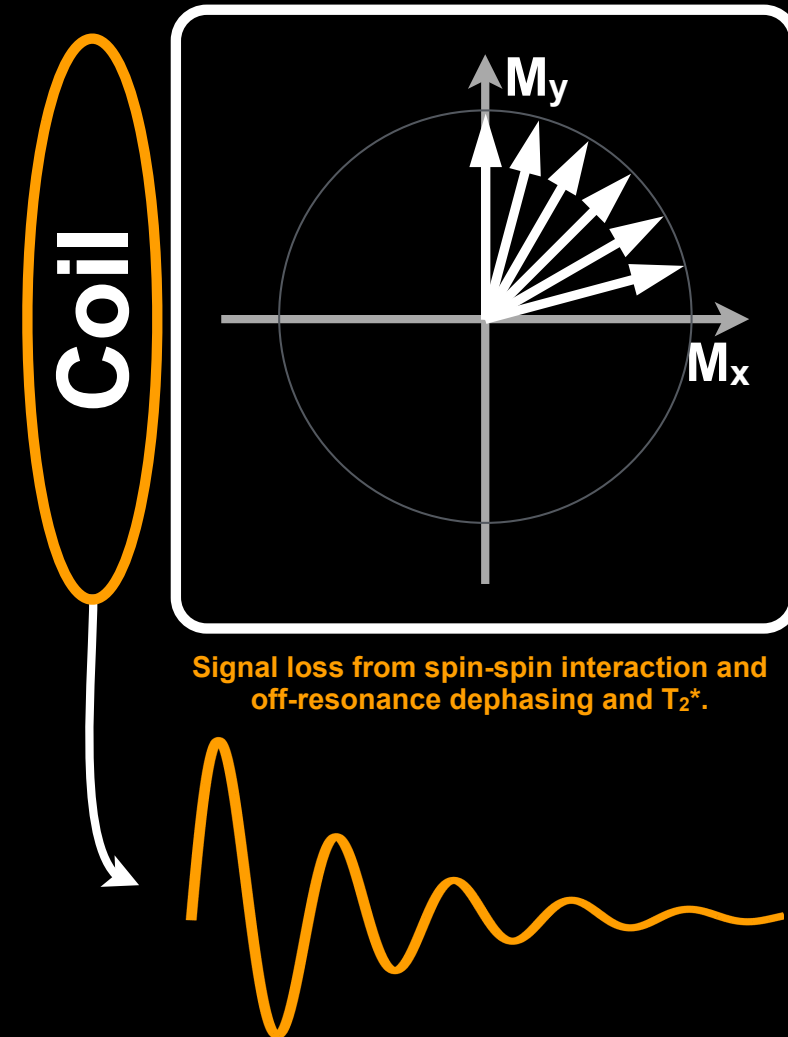
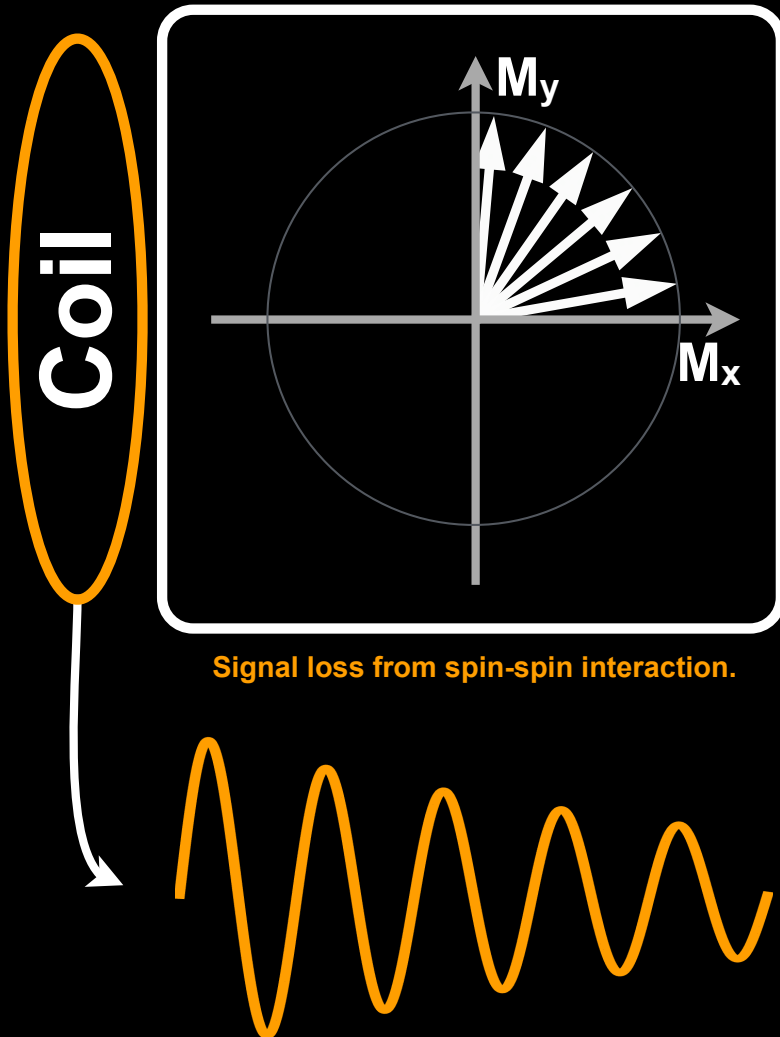
↑  
Irreversible  
Losses

↑  
Reversible  
Losses

# $T_2$ versus $T_2^*$

$T_2$  Decay

$T_2^*$  Decay



**Signal loss from spin dephasing and  $T_2^*$ .**

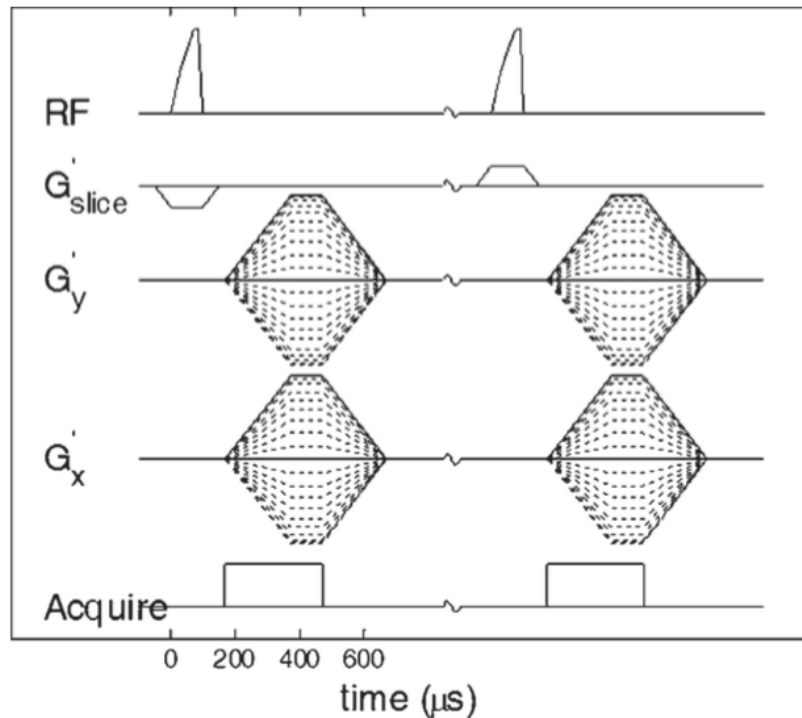
# Range of Off-Resonances

- **B<sub>0</sub>**
  - <4ppm over 50cm DSV
    - ~0.008ppm within a 1mm voxel
    - ~0.5Hz for <sup>1</sup>H at 1.5T within a 1mm voxel
- **Susceptibility**
  - -5.06ppb for N<sub>2</sub> and 0.37ppm for O<sub>2</sub>
  - ~70.5ppb for air (0.8\*(-5.06e-9)+0.2\*(3.73e-7))
    - ~4.5Hz for *air* at 1.5T
- **Chemical shift**
  - ~3.4ppm for fat
    - ~217 Hz for <sup>1</sup>H at 1.5T within a voxel
- **Gradients**
  - 5G/cm or 0.5G/mm
    - 2128Hz for <sup>1</sup>H across a 1mm voxel

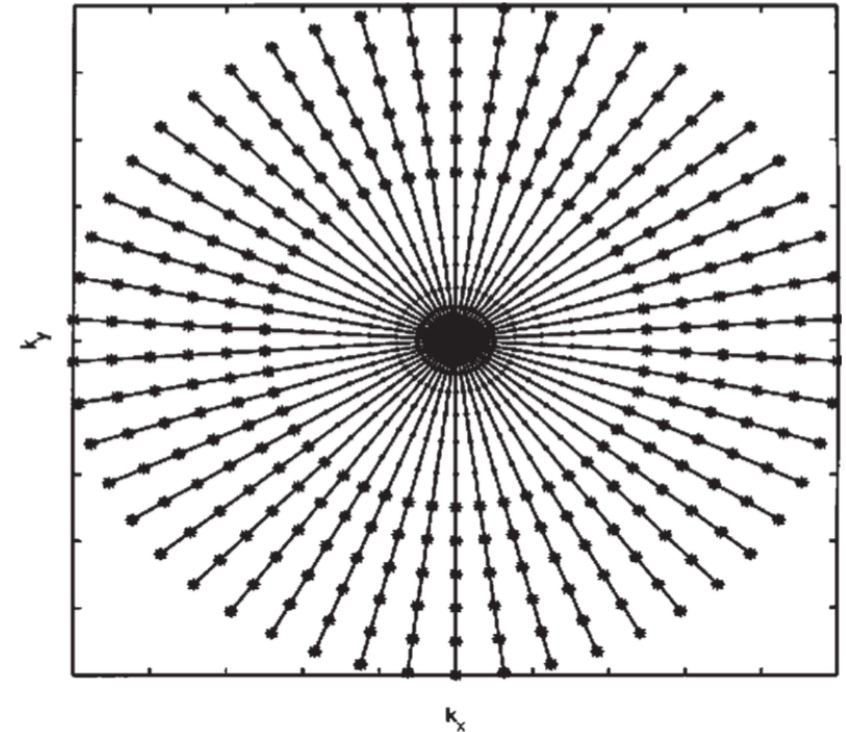
# Free Induction Decay

- Used for ultrashort echo time imaging of very short  $T_2$  species
  - Positive contrast for bone, ligament, tendon, cartilage, meniscus, etc.
- Spin echoes and gradient echoes are methods that extend the usability of the FID signal

# UTE Pulse Sequence



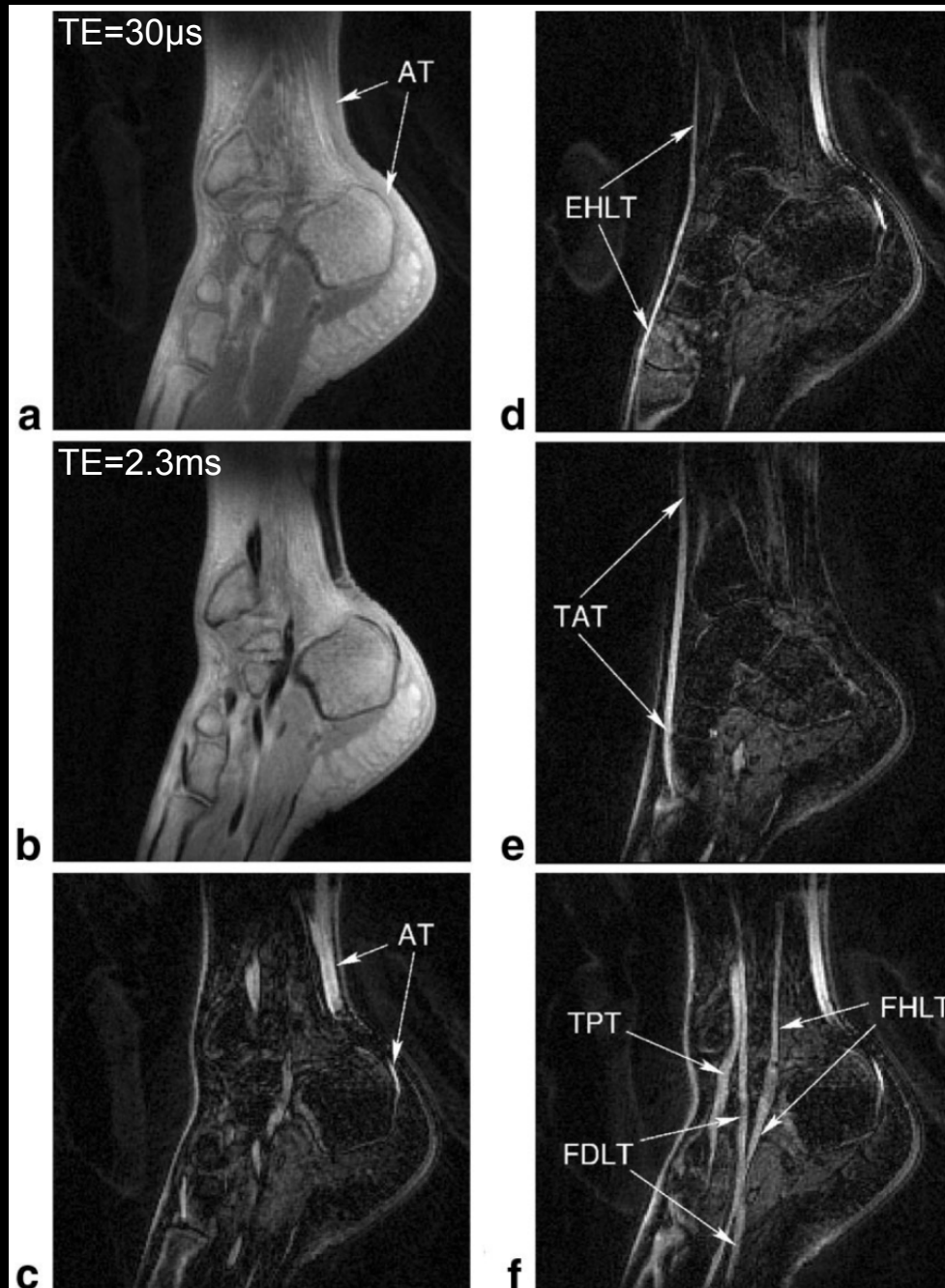
**Figure 4.** Pulse sequence diagram for a basic UTE sequence. The half rf pulses are applied with the slice selection gradient  $G_z$  negative in the first half and with this gradient positive in the second half. The rf pulse is truncated and followed rapidly by the acquisition during which  $G_x$  and  $G_y$  are applied to give the radial gradient. These gradients ramp up to a plateau during data acquisition



**Figure 5.**  $k$ -Space trajectories for the above imaging sequence. Each 'spoke' represents the  $k$ -space trajectory due to the readout gradients. The dots represent the central points which are sampled on the gradient ramps, and the stars the peripheral points which are sampled on the gradient plateau. Practical acquisitions typically include 128–512 spokes and 256–512 points on each spoke. The data points are regridded onto a Cartesian grid prior to 2D Fourier transformation



# Ultra Short TE (UTE) Images



Tendons have a very short  $T_2$ .

FIG. 7. 3D UTE dual-echo data of the right ankle. (a) FID image at TE 30µs showing high signal from almost all tissues. The arrows indicate the Achilles tendon (AT). (b) Echo acquired at TE 2.3 ms. (c) Difference image highlighting short- $T_2$  components. (d-f) Curved (nonplanar) reformatted views of the 3D difference image data set. The course of several tendons can be followed through the complex anatomy of the ankle. (d) Extensor hallucis longus tendon (EHLT). (e) Tibialis anterior tendon (TAT). (f) Flexor digitorum longus tendon (FDLT) crossing the flexor hallucis longus tendon (FHLT); the tibialis posterior tendon (TPT) is also visible.

Rahmer J, Bornert P, Groen J, Bos C. Magn Reson Med 2006;55(5): 1075-1082 [PMID 16538604].



Echoes

# Why echoes?

- **Free Induction Decay**
  - **Signal decays rapidly**
    - $T_2$ 
      - Spin-spin interaction
    - **Spectral (frequency) distribution**
      - Micro-scale B-field heterogeneity ( $T_2^*$ )
      - Macro-scale B-field heterogeneity ( $T_2^{**}$ )
  - **Imaging requires certain “delays”**
    - **Slice-selective rephasing**
    - **Phase encoding**
    - **Read-out pre-phasing**
  - **Echoes let us buy some time**

# What are echoes?

- **Two-sided NMR signals**
  - First half from re-focusing
  - Second half from de-phasing
- **Radiofrequency Echoes**
  - Arise from multiple RF-pulses
- **Gradient Echoes**
  - Arise from magnetic field gradient reversal

“it is easier to generate an echo than to ignore it in multiple-pulse MR experiments”

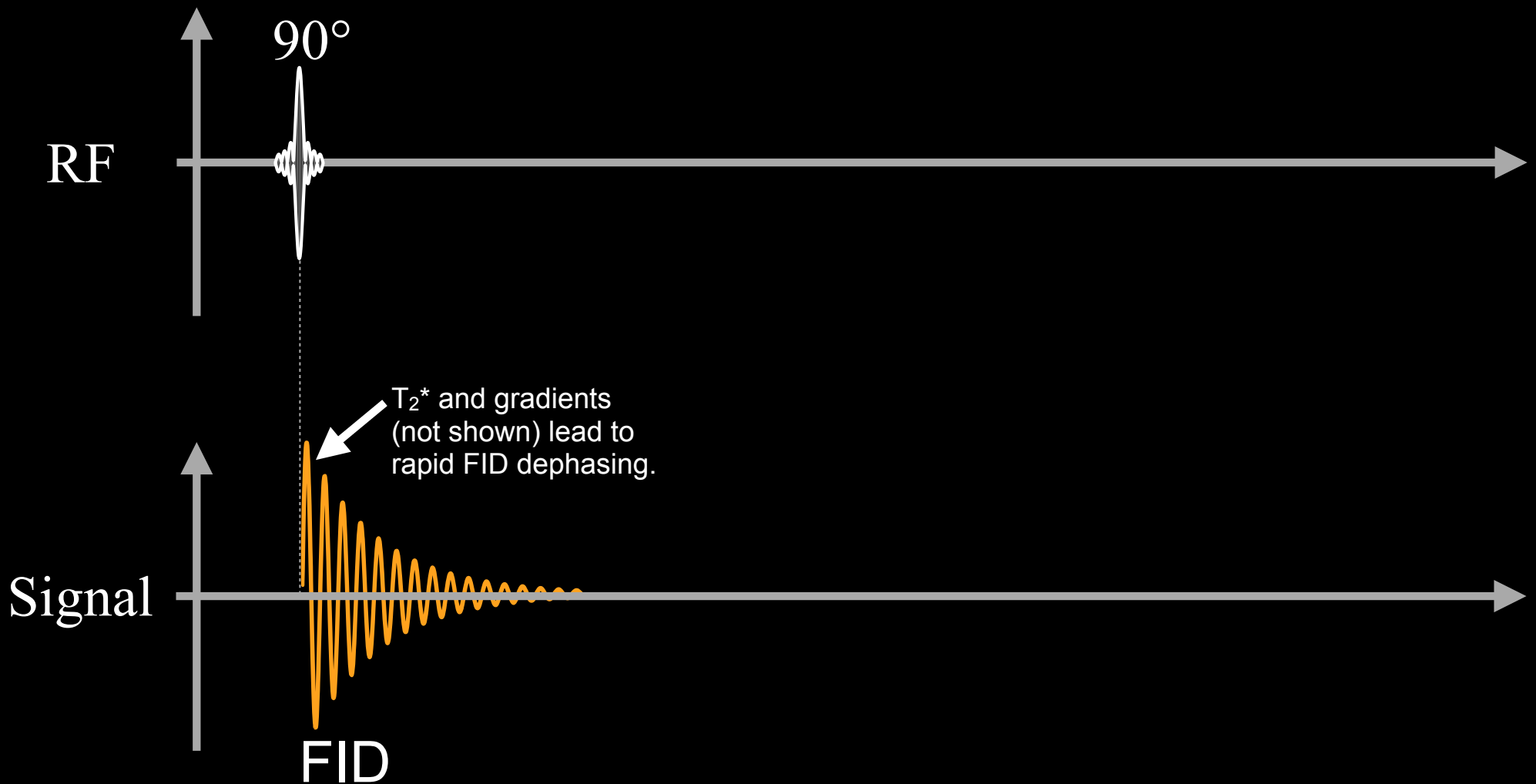
--Liang & Lauterbur, Page 114

# Spin Echo Imaging

# Spin Echo

- **Advantages**
  - **Insensitive to off-resonance**
    - **All spins within voxel rephased**
    - **$B_0$  inhomogeneity**
    - **Intravoxel Chemical shift signal loss**
    - **Susceptibility**
  - **Great for  $T_1$ ,  $T_2$ ,  $\rho$  contrast**
    - **Not  $T_2^*$**
  - **High SNR**
- **Disadvantages**
  - **TR can be long**
    - **Leads to long scan time**
  - **SAR can be high**
    - **Lots of 90s and 180s**
    - **Leads to patient heating**

# Free Induction Decay



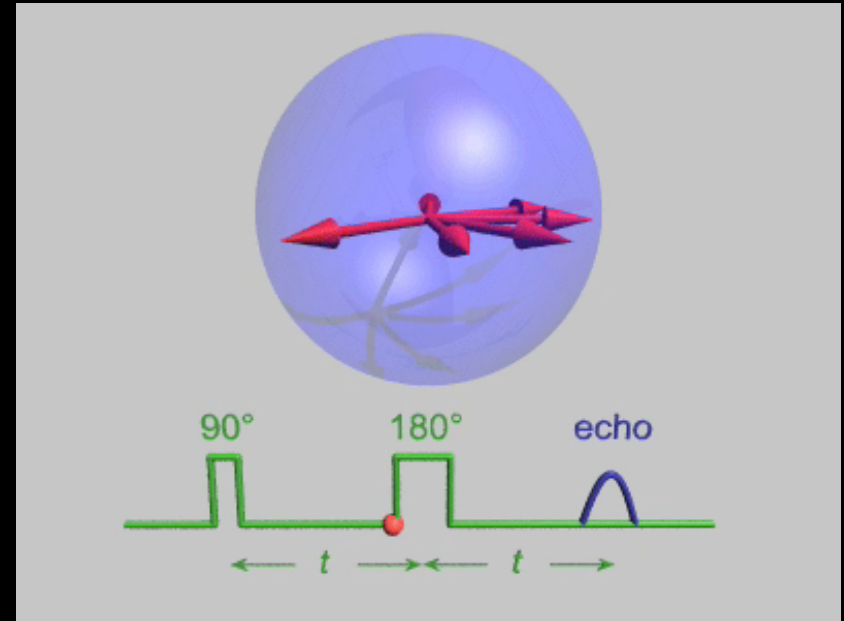
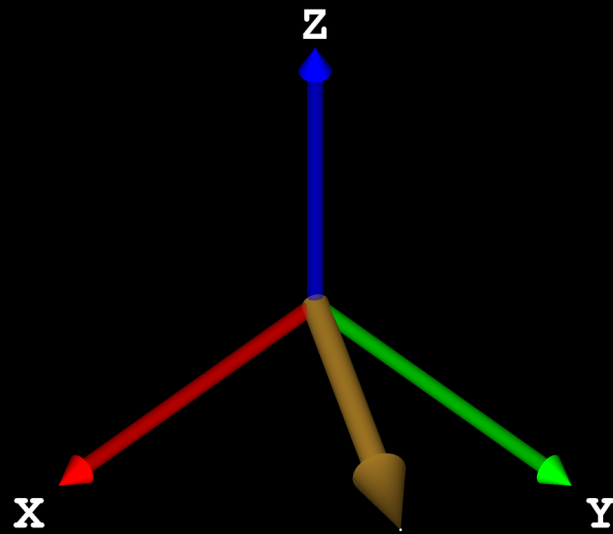
We can “refocus” the signal with a refocusing RF pulse.

# Refocusing Pulses

- **Typically, 180° RF Pulse**
  - Provides optimally refocused  $M_{xy}$
  - Largest **spin echo** signal
- **Refocus spin dephasing due to**
  - imaging gradients
  - local magnetic field inhomogeneity
  - magnetic susceptibility variation
  - chemical shift



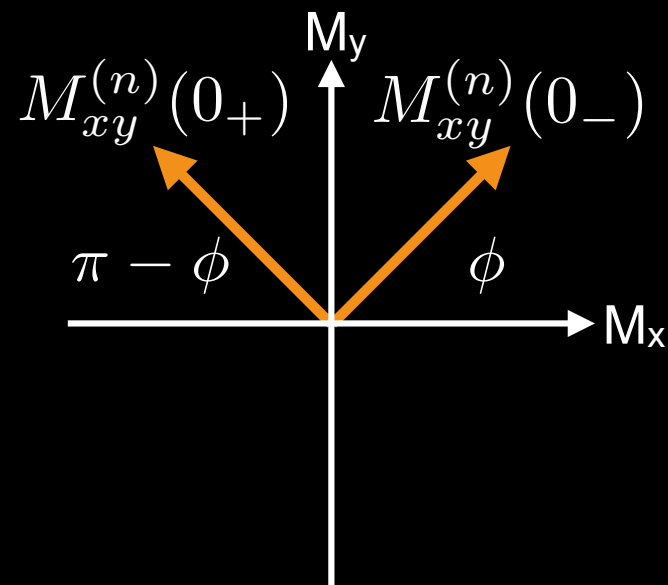
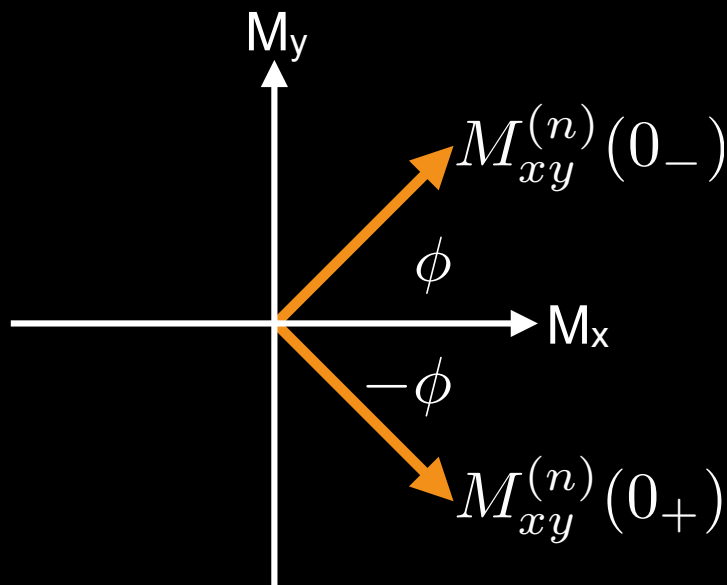
# Refocusing Pulses



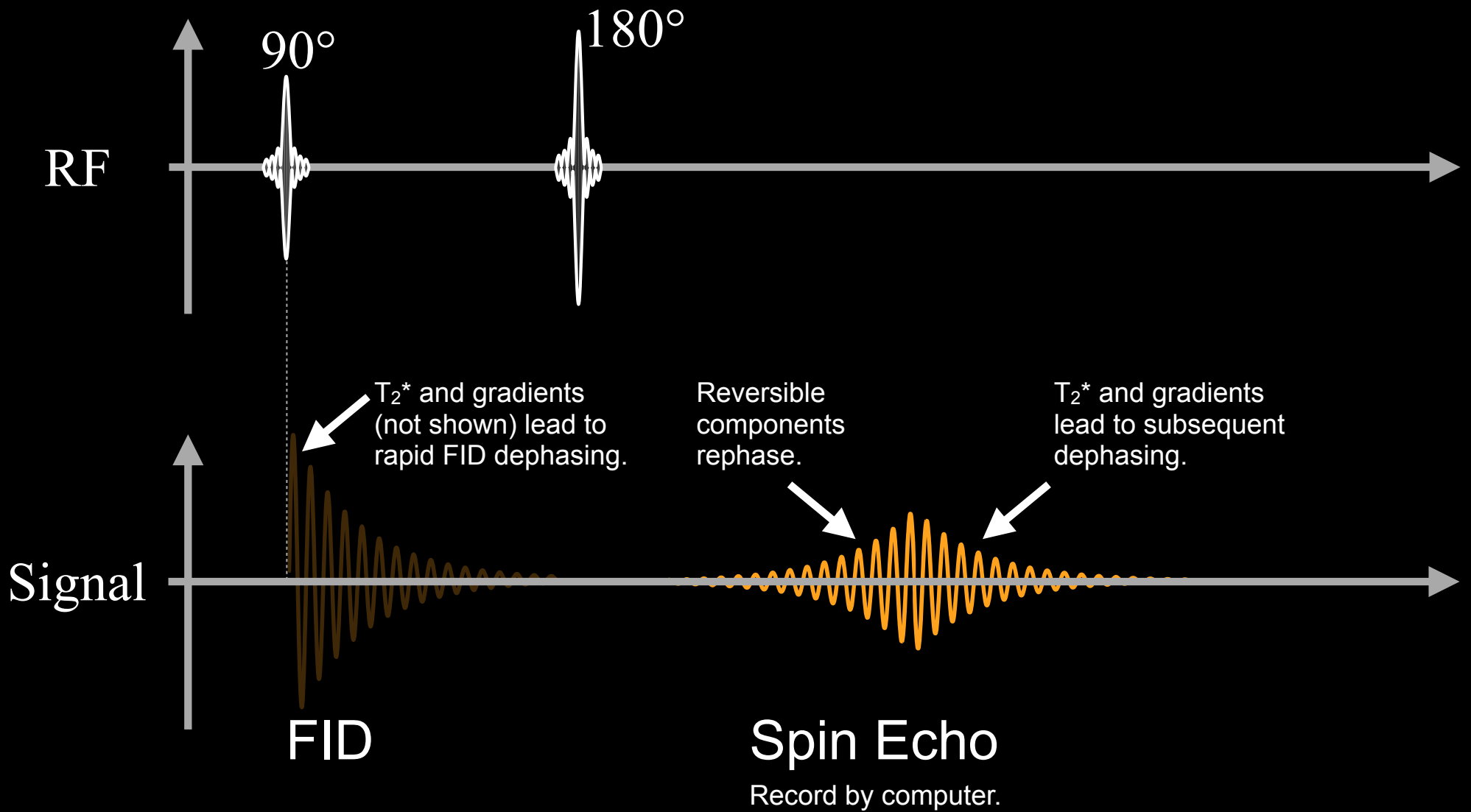
# Hard Refocusing Pulses

$$\text{RF}_\theta^\alpha = \begin{bmatrix} c^2\theta + s^2\theta c\alpha & c\theta s\theta - c\theta s\theta c\alpha & -s\theta s\alpha \\ c\theta s\theta - c\theta s\theta c\alpha & s^2\theta + c^2\theta c\alpha & c\theta s\alpha \\ s\theta s\alpha & -c\theta s\alpha & c\alpha \end{bmatrix}$$

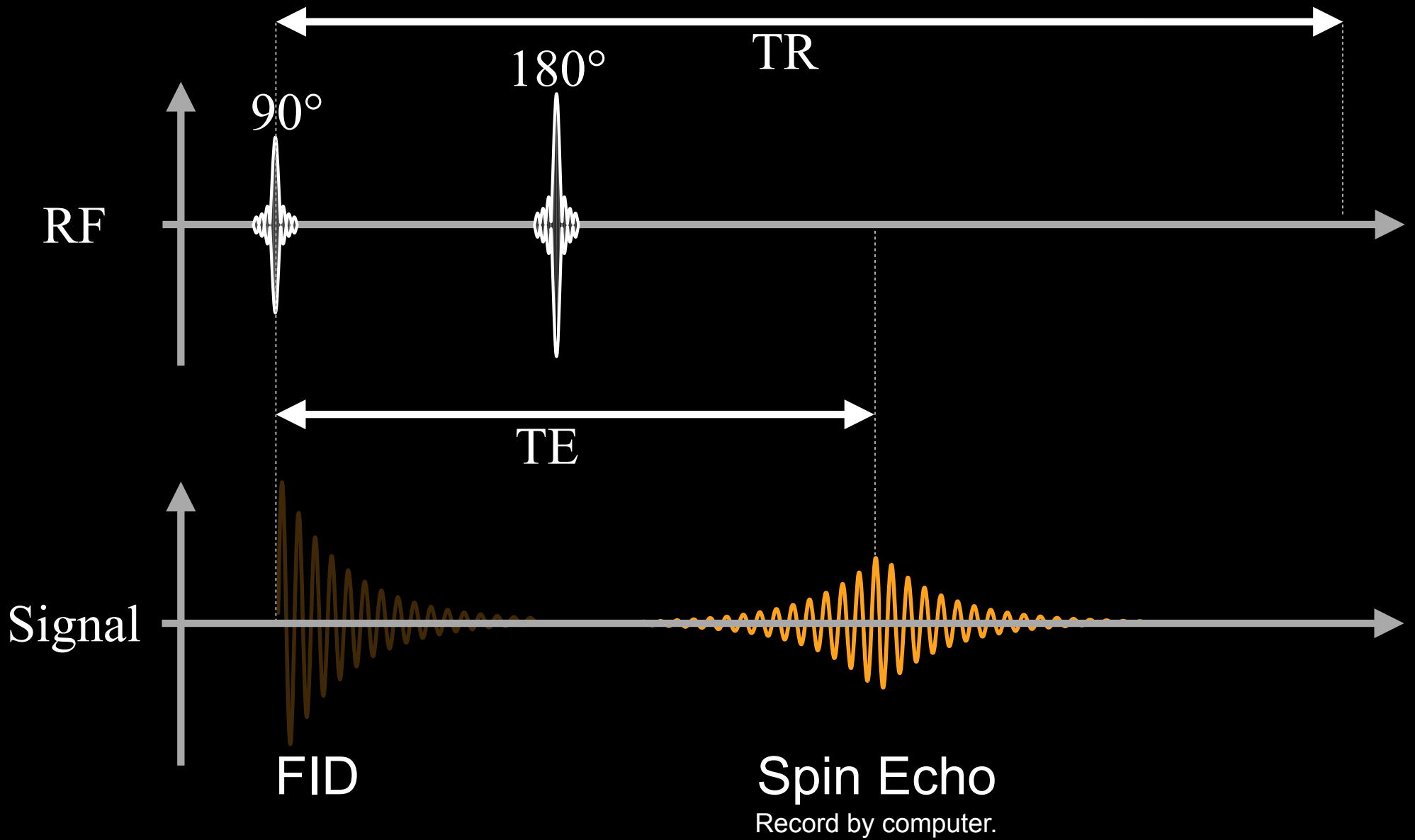
$$\text{RF}_\theta^\alpha = \text{RF}_0^\pi = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} M_x \\ M_y \\ M_z \end{bmatrix} \quad \text{RF}_\theta^\alpha = \text{RF}_{\pi/2}^\pi = \begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$



# Spin Echo

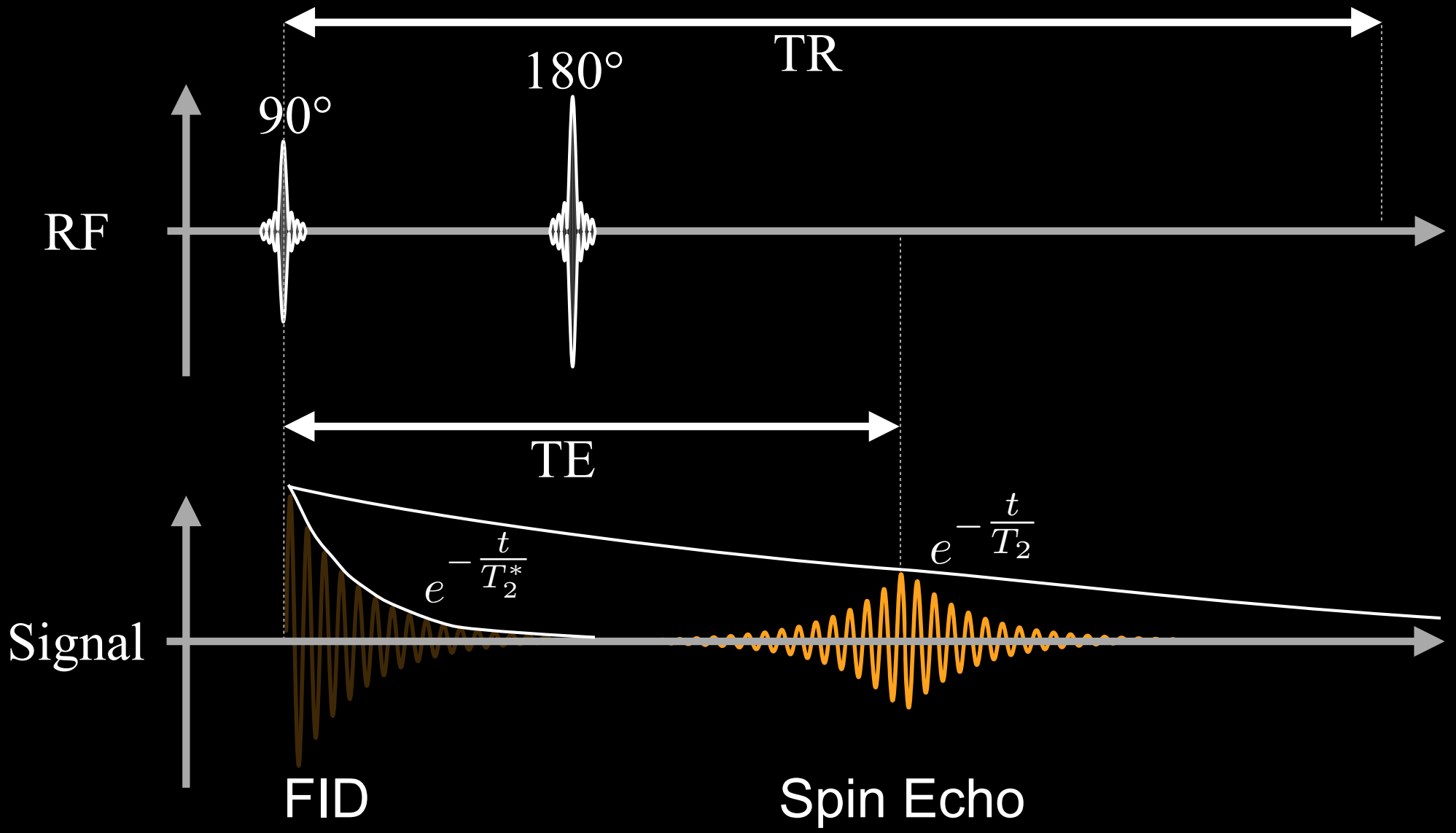


# Spin Echo



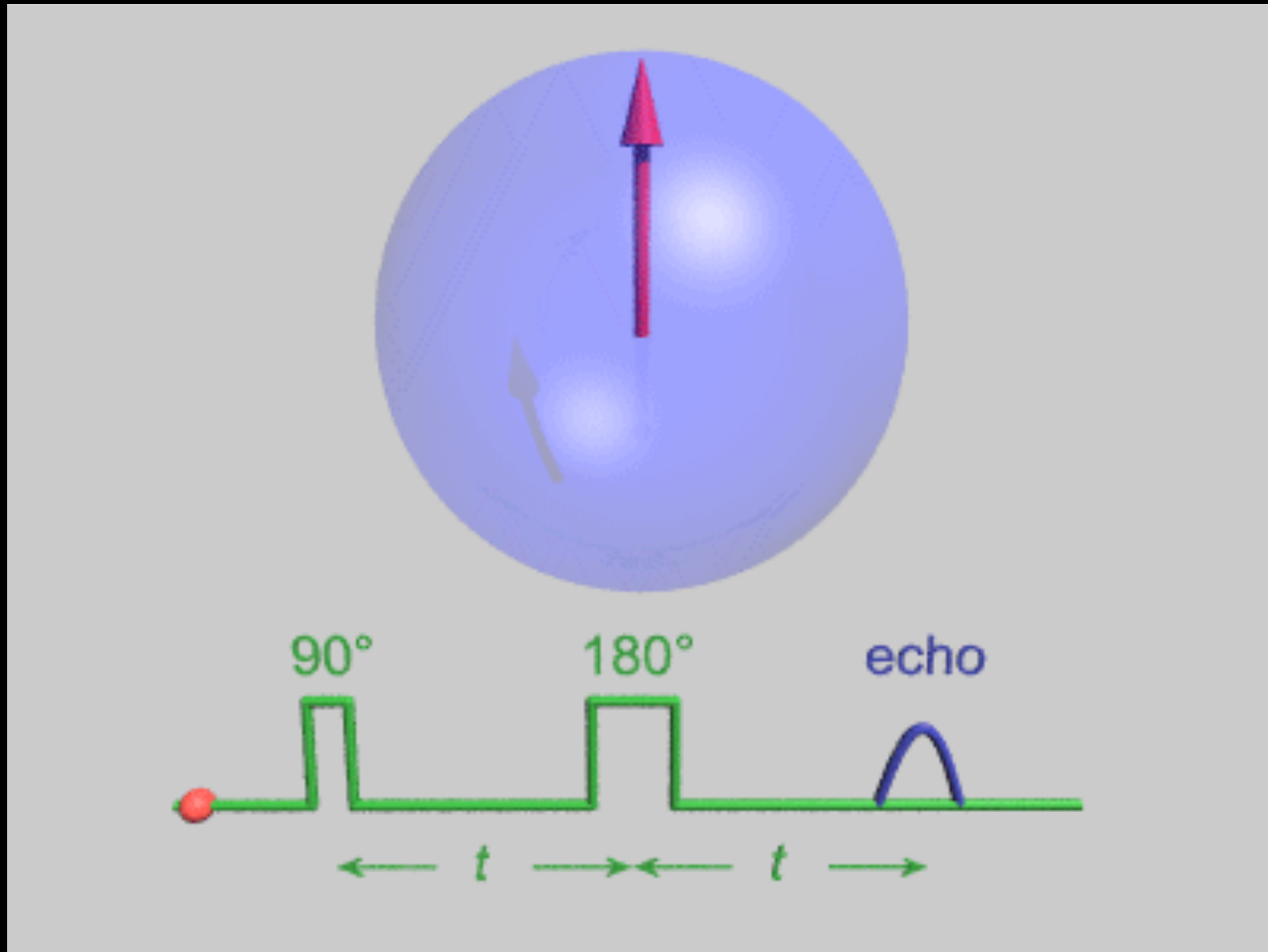
Record by computer.

# Spin Echo

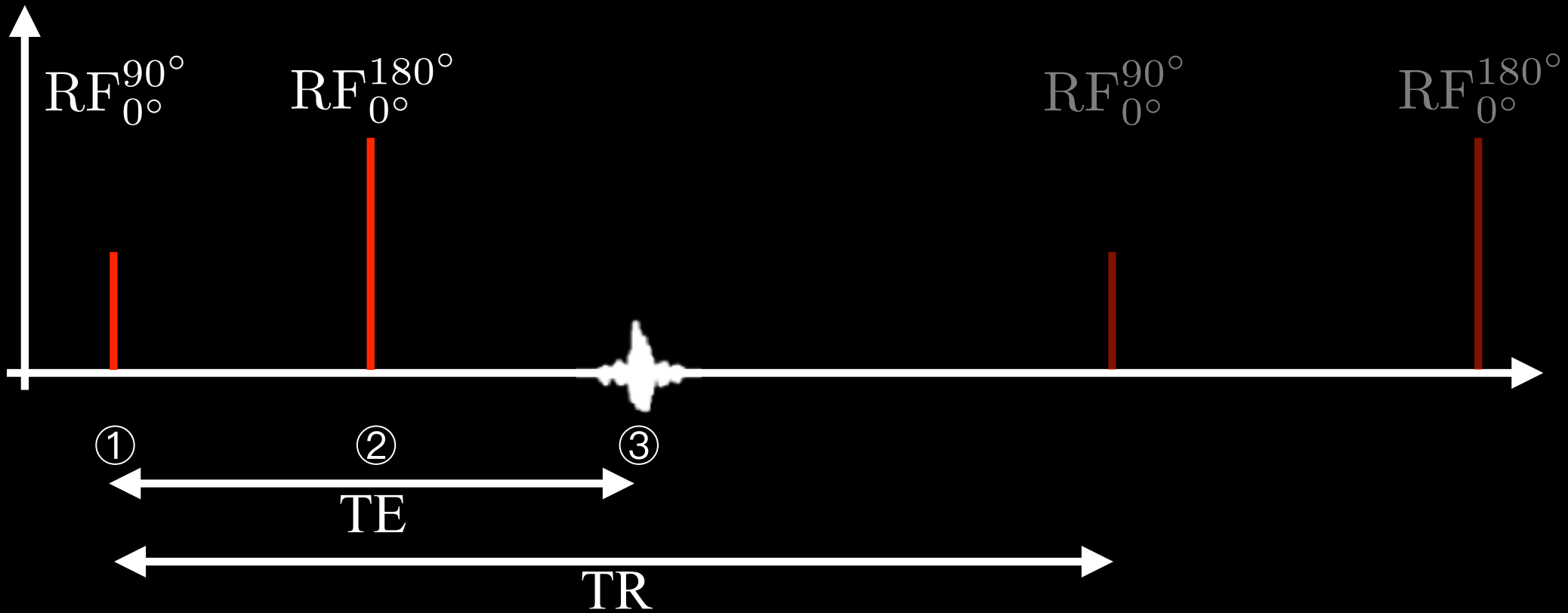


How do you adjust the TR?  
How do you adjust the TE?

# Spin Echo - Refocusing



# Spin Echo



To The Board...

# Spin Echo Contrast

$$M_{z'}^{(4)}(0_-) = M_z^0 \left( 1 - 2e^{-(TR-TE/2)/T_1} + e^{-TR/T_1} \right)$$

This becomes the initial condition for the subsequent TR. Eqn. 7.24

$$A_{Echo} \propto \rho \left( 1 - 2e^{-(TR-TE/2)/T_1} + e^{-TR/T_1} \right) e^{-TE/T_2}$$

This the signal at time-point #3 for the second TR. Eqn. 7.25

If  $TE \ll TR$ , then

$$A_{Echo} \propto \rho \left( 1 - e^{-TR/T_1} \right) e^{-TE/T_2} \quad \text{Eqn. 7.26}$$

This the signal at time-point #3 for the second TR when  $TE \ll TR$ .



# Spin Echo Contrast

## Spin Echo Parameters

	TE	TR
Spin Density	Short	Long
T <sub>1</sub> -Weighted	Short	Intermediate
T <sub>2</sub> -Weighted	Intermediate	Long

$$A_{Echo} \propto \rho \left( 1 - e^{-TR/T_1} \right) e^{-TE/T_2}$$

Long TR  
Minimizes This  
Term

Limits T<sub>1</sub> signal  
contribution.

Short T<sub>1</sub>  
Maximizes  
This Term

Leads to T<sub>1</sub>  
weighting.

Long TE  
Emphasizes  
This Term

Adds T<sub>2</sub> contrast.

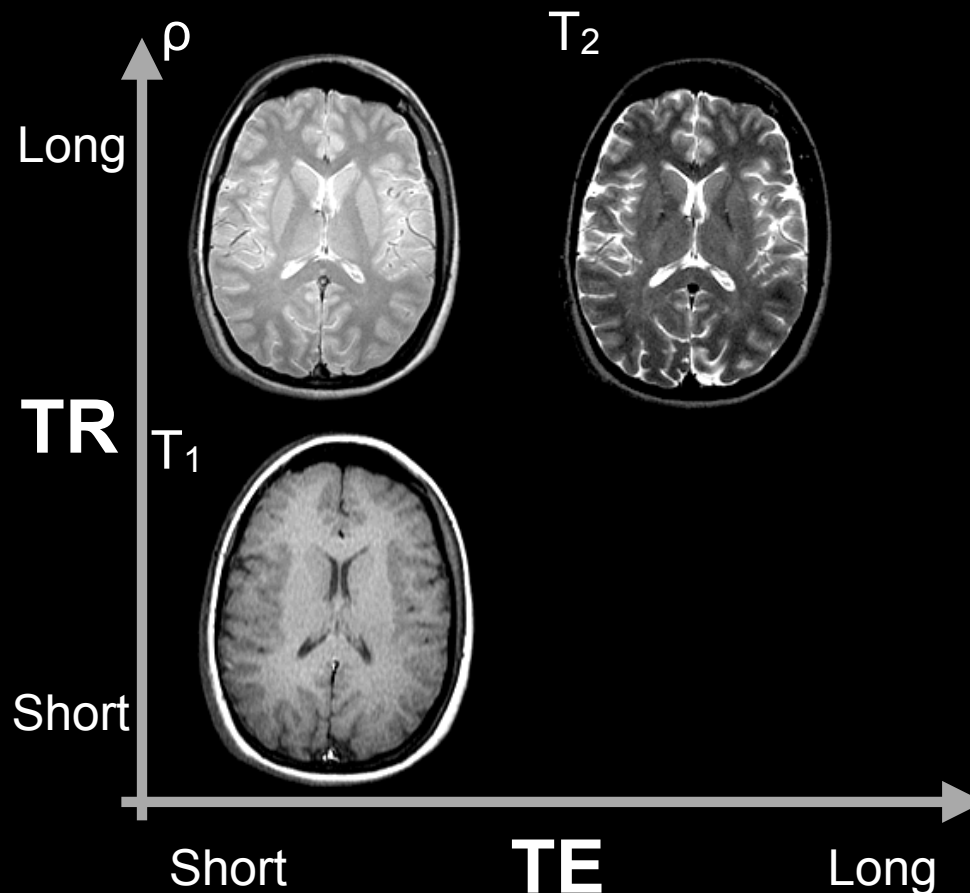
Long T<sub>2</sub>  
Maximizes  
This Term

Long T<sub>2</sub> is bright on  
T<sub>2</sub>-weighted images.

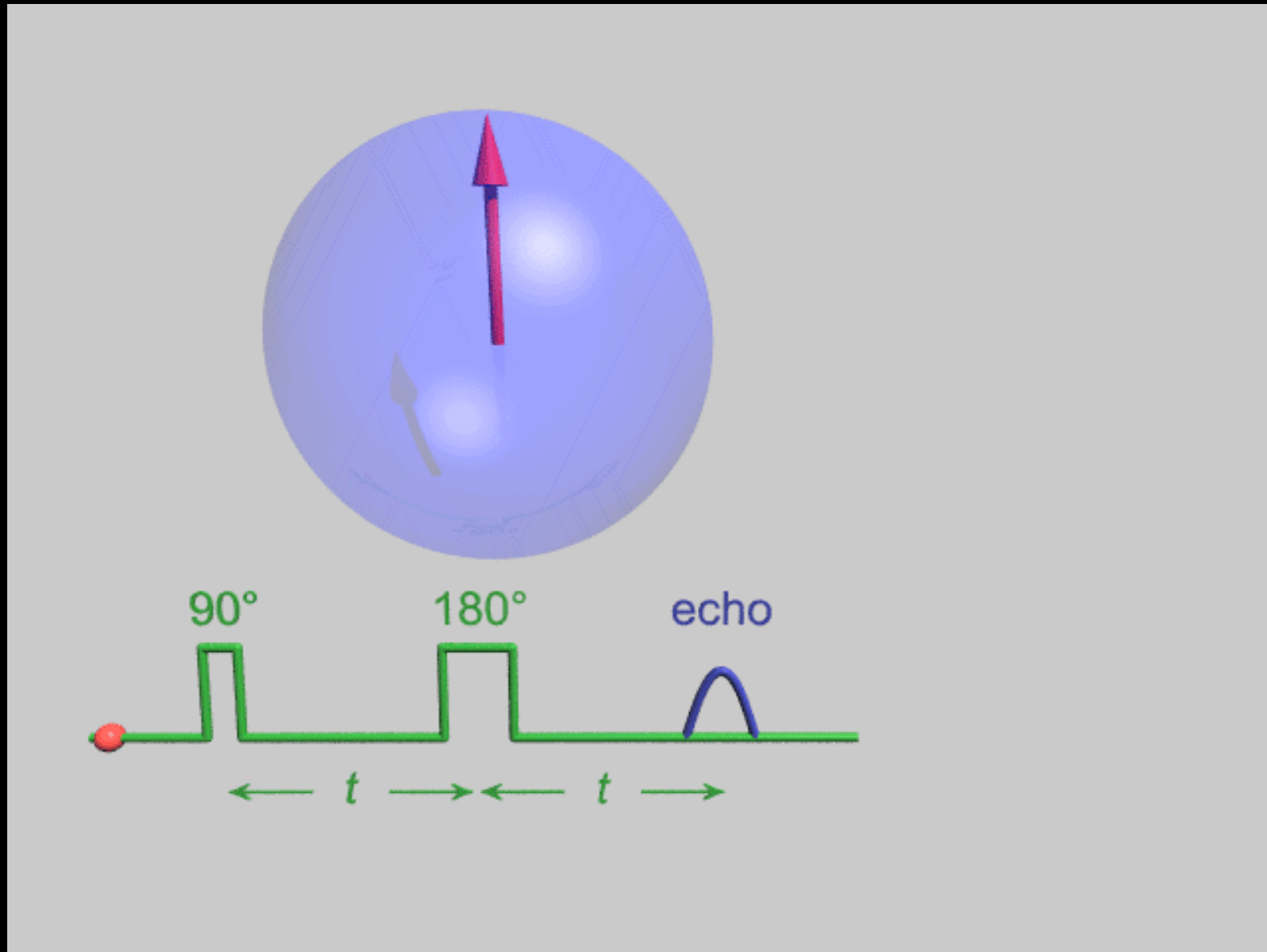
# Spin Echo Contrast

## Spin Echo Parameters

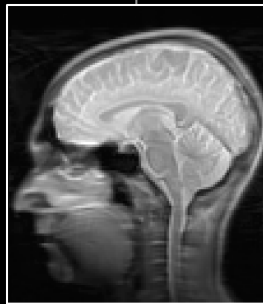
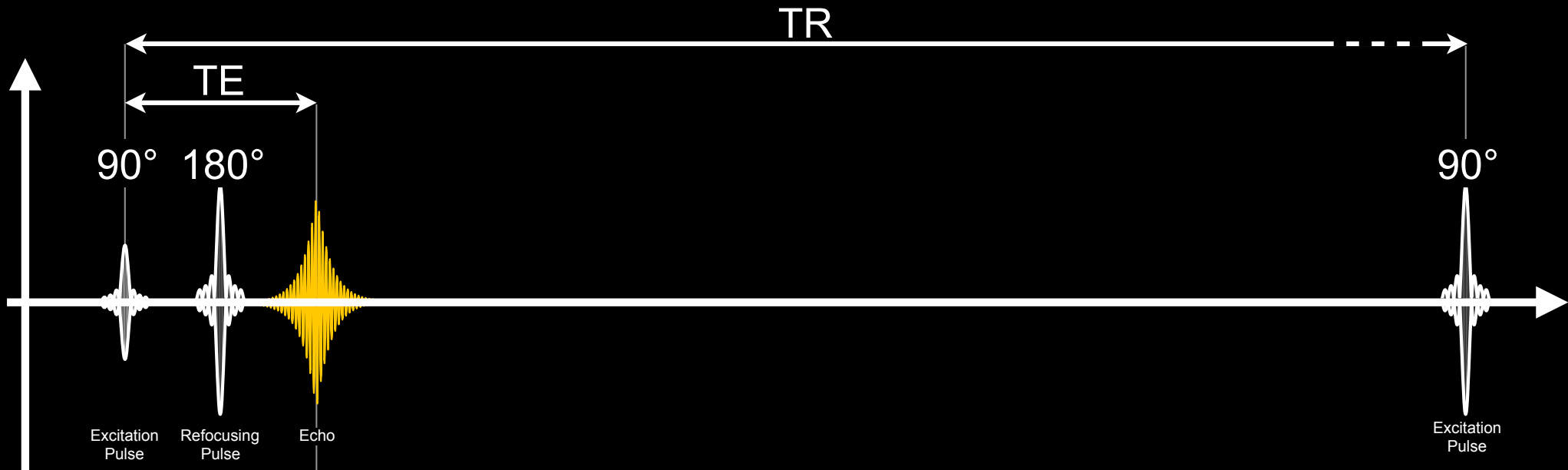
	TE	TR
Spin Density	Short	Long
T <sub>1</sub> -Weighted	Short	Intermediate
T <sub>2</sub> -Weighted	Intermediate	Long



# Spin Echo - Contrast



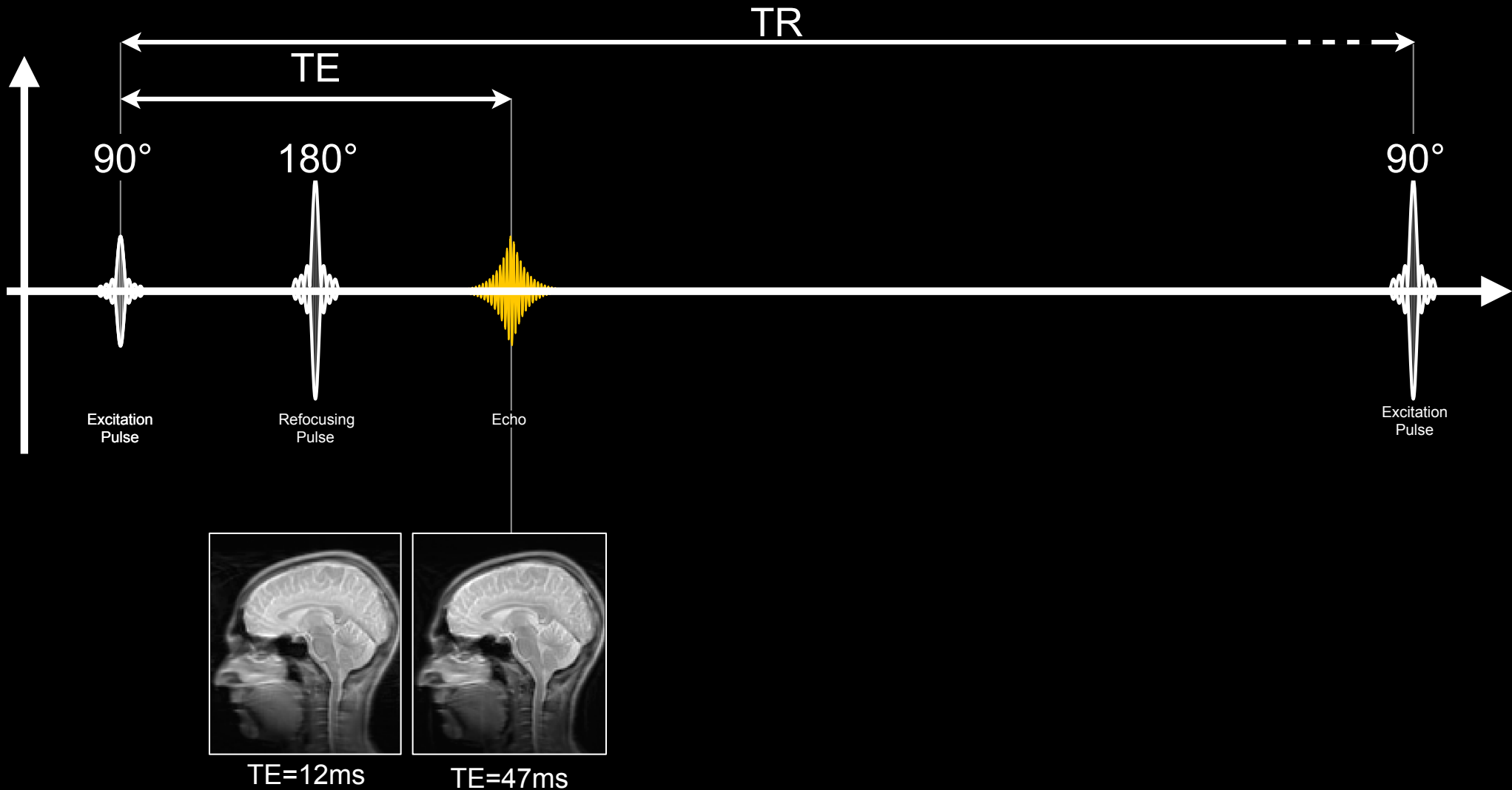
# Spin Echo



TE=12ms

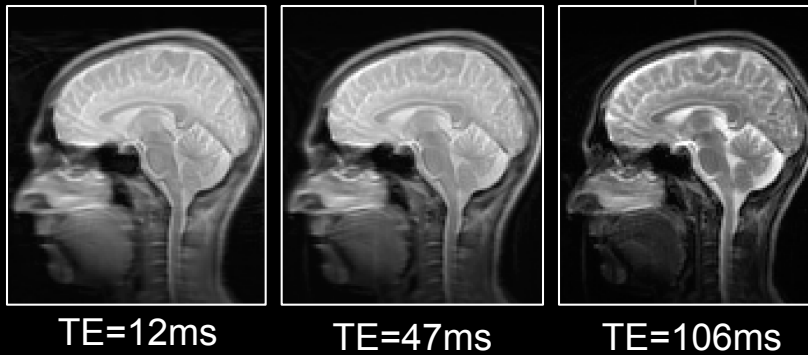
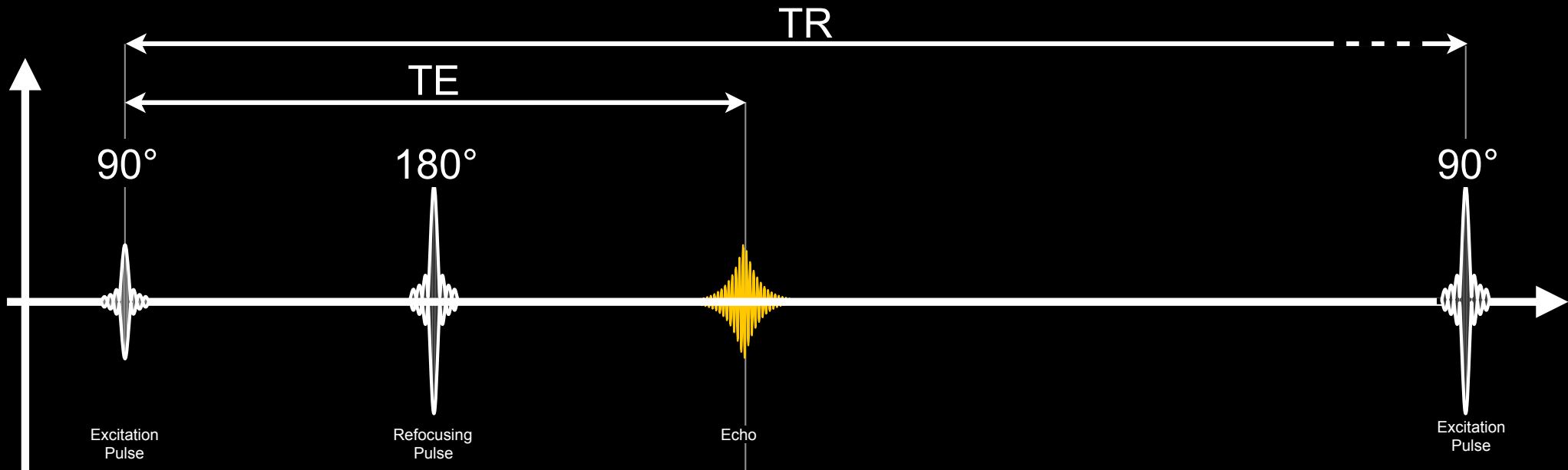
Short TE and Long TR is proton density weighted.

# Spin Echo



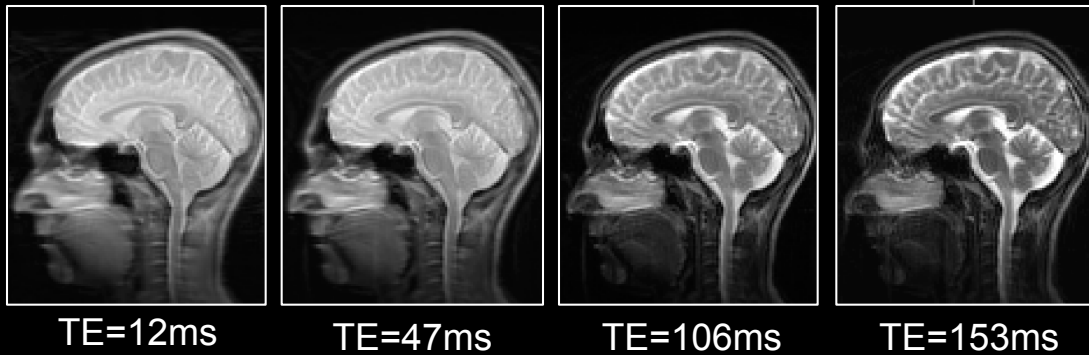
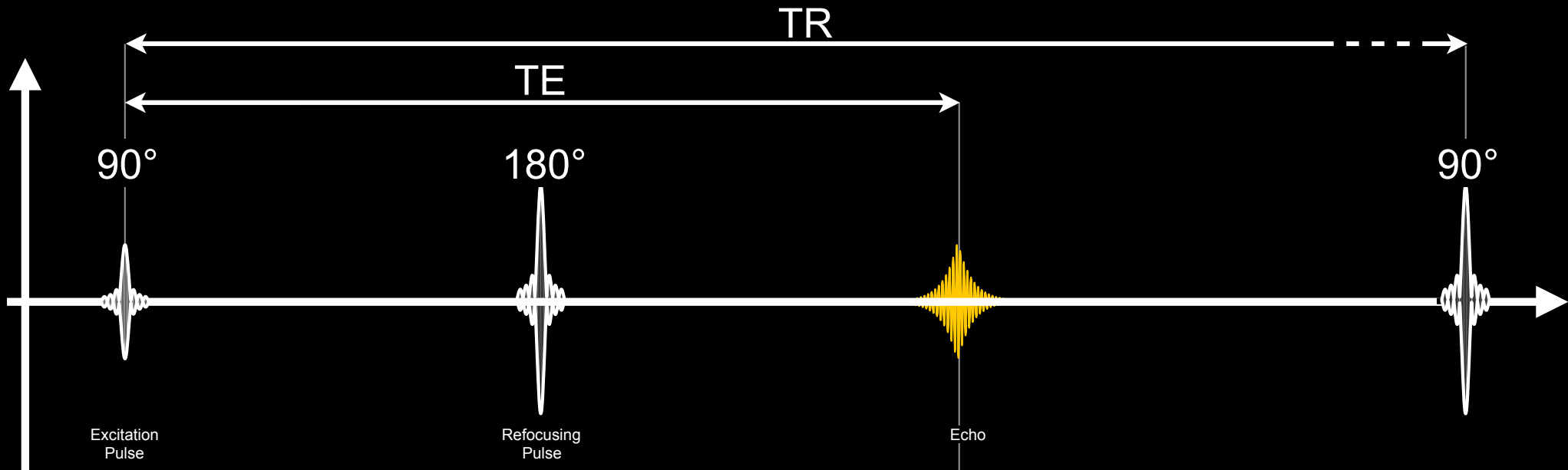
Delaying the 180° refocusing pulse delays the TE.

# Spin Echo



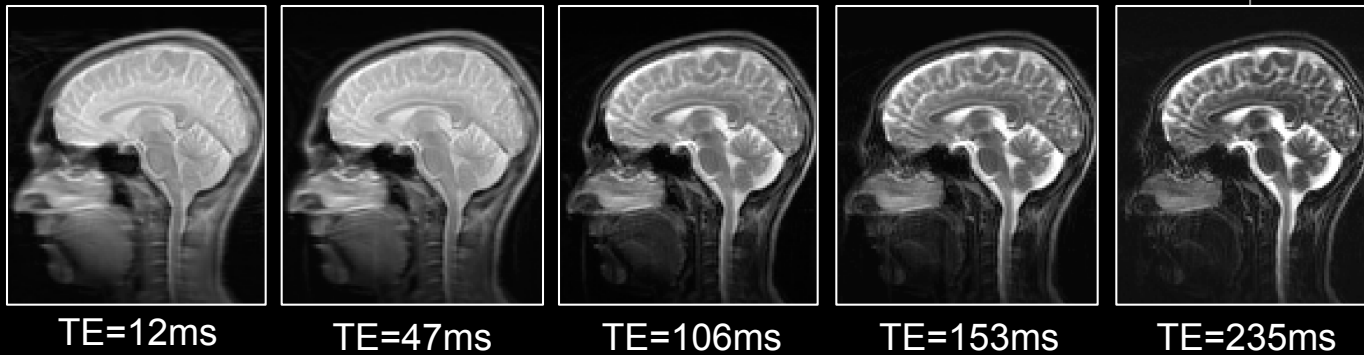
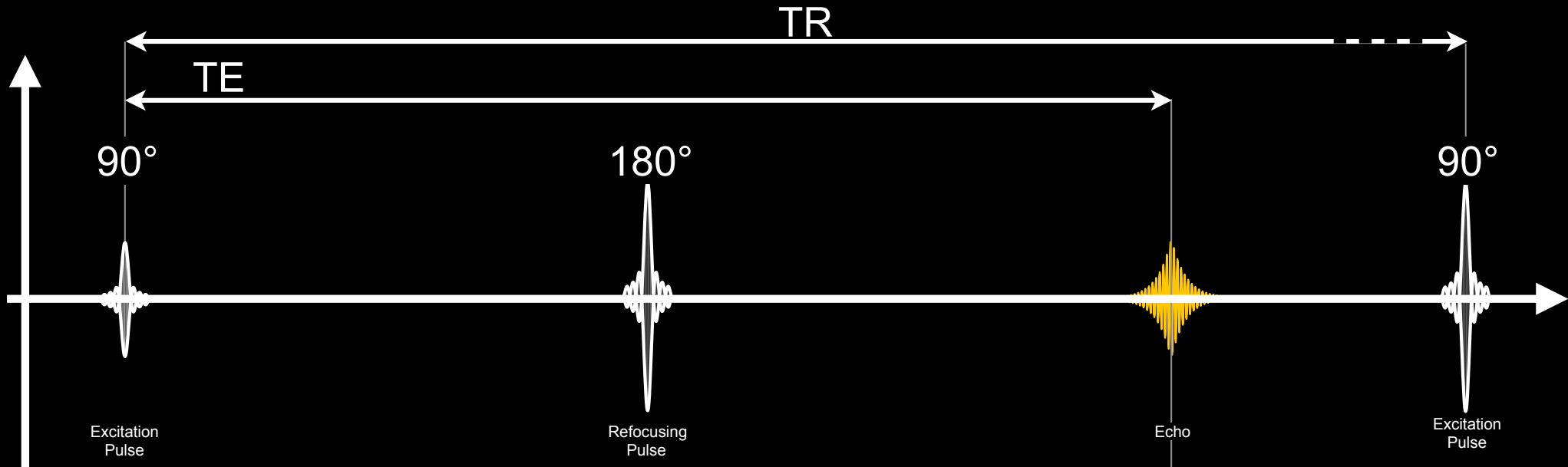
Longer TEs produce more T<sub>2</sub>-weighting.

# Spin Echo



Longer TEs produce more T<sub>2</sub>-weighting.

# Spin Echo



Long  $T_2$  is bright on  $T_2$ -weighted (long TE) images.



# Thanks



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