

# Image Reconstruction and Artifacts

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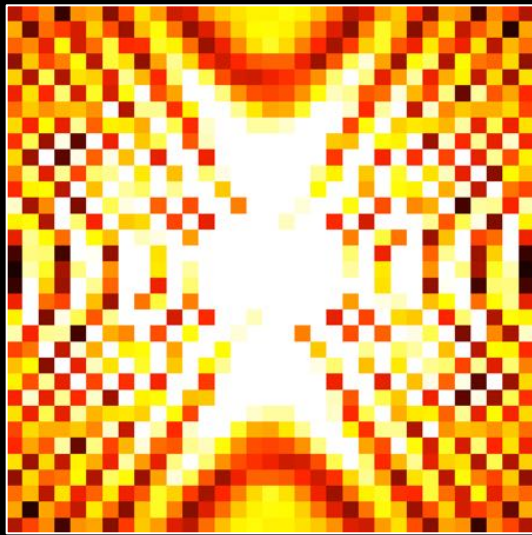
David Geffen  
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**UCLA**  
Radiology

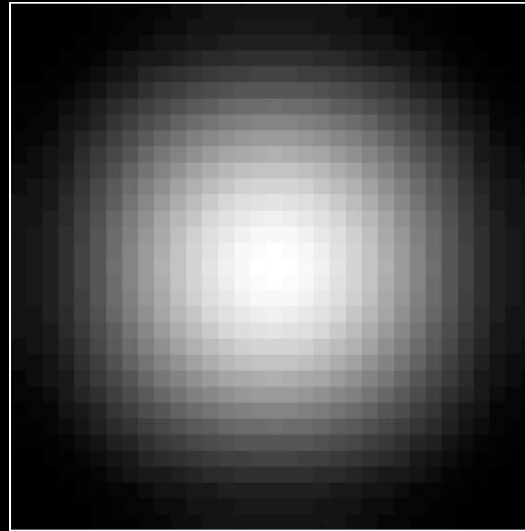
# Lecture #13 - Learning Objectives

- **Understand how to combine data from several receiver channels.**
- **Appreciate how the final image is obtained from the sum over all sampled spatial frequency (Fourier) patterns.**
- **Define how the field-of-view and the number of acquired data points impacts spatial resolution.**
- **Describe the parameters that control the field of view.**
- **Understand the applications of zero padding and windowed reconstructions.**
- **Identify sources of Gibb's ringing and ways to mitigate it.**

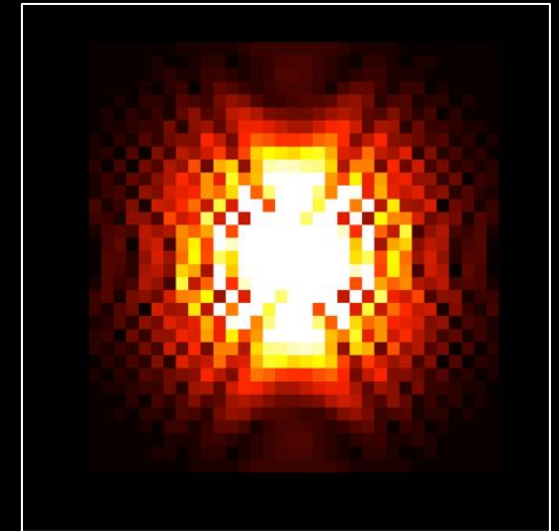
# Lecture #13 Summary



●  
Dot  
Multiply



=



FFT

$$\hat{I}(x) = \Delta k \sum_{n=-N/2}^{N/2-1} S(n\Delta k) w_n e^{i2\pi n\Delta kx}$$

FFT



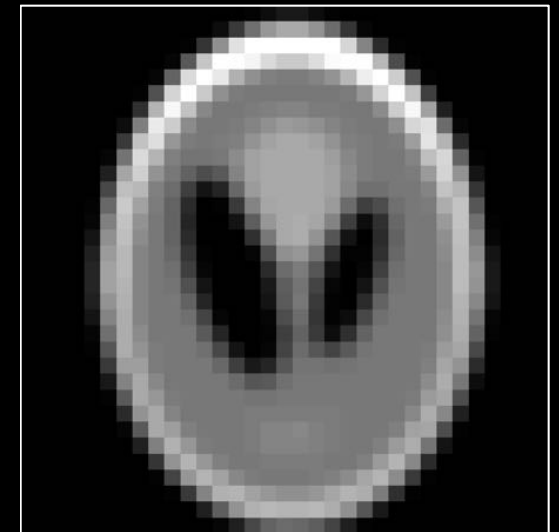
On...  
 $|x| < \frac{1}{\Delta k}$

Series  
Coefficient

Window  
Weight

Spatial  
Frequency  
Encoding

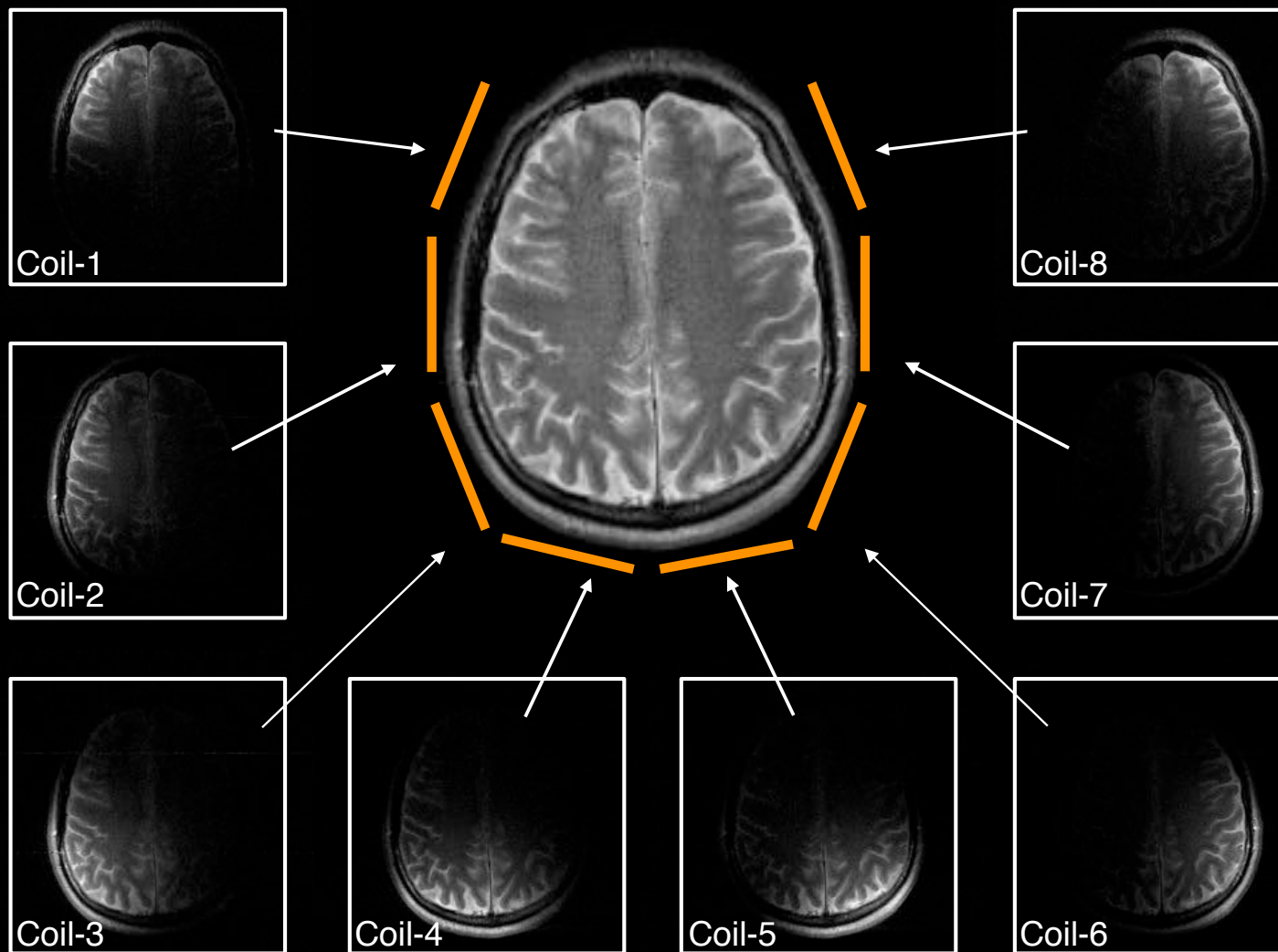
Fourier  
Step-size



**Fourier Reconstruction Formula (Eqn. 6.20)**

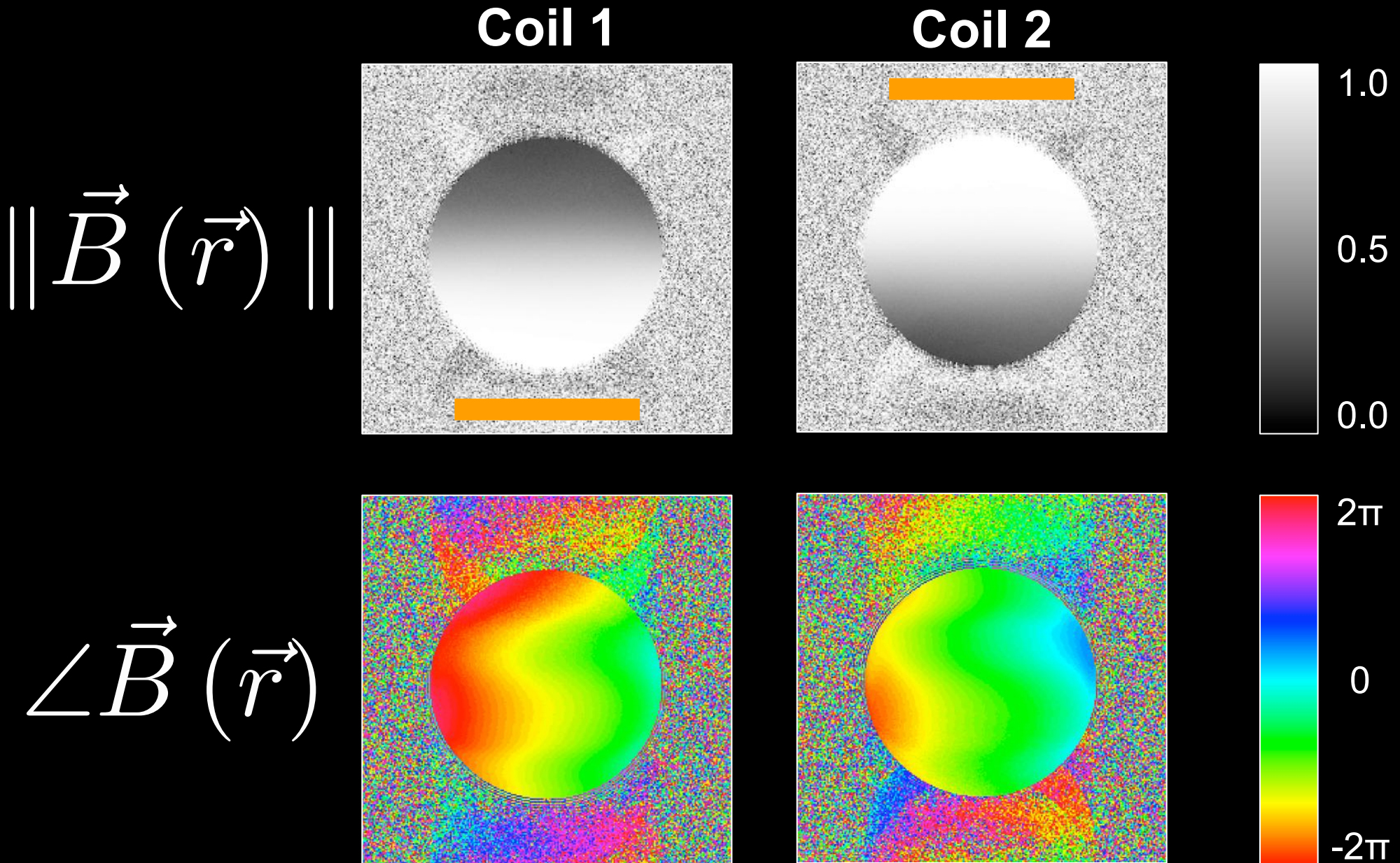
# Multi-Channel Reconstruction

# 8-Channel Head Coil



Each coil element (channel) has a unique sensitivity profile –  $\vec{B}_r(\vec{r})$

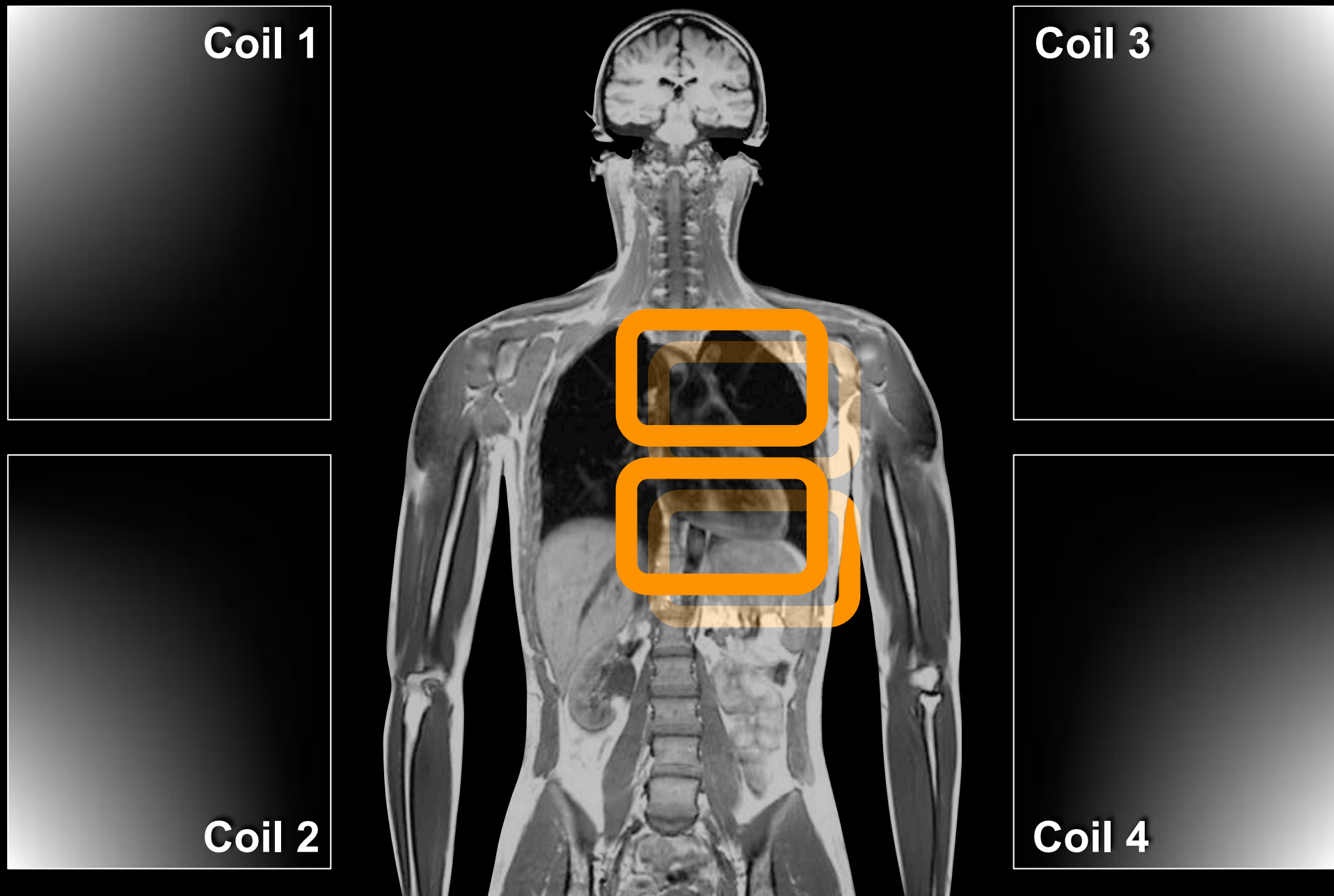
# Multi-coil Magnitude & Phase



Coils “color” the magnitude and phase of the received signal.

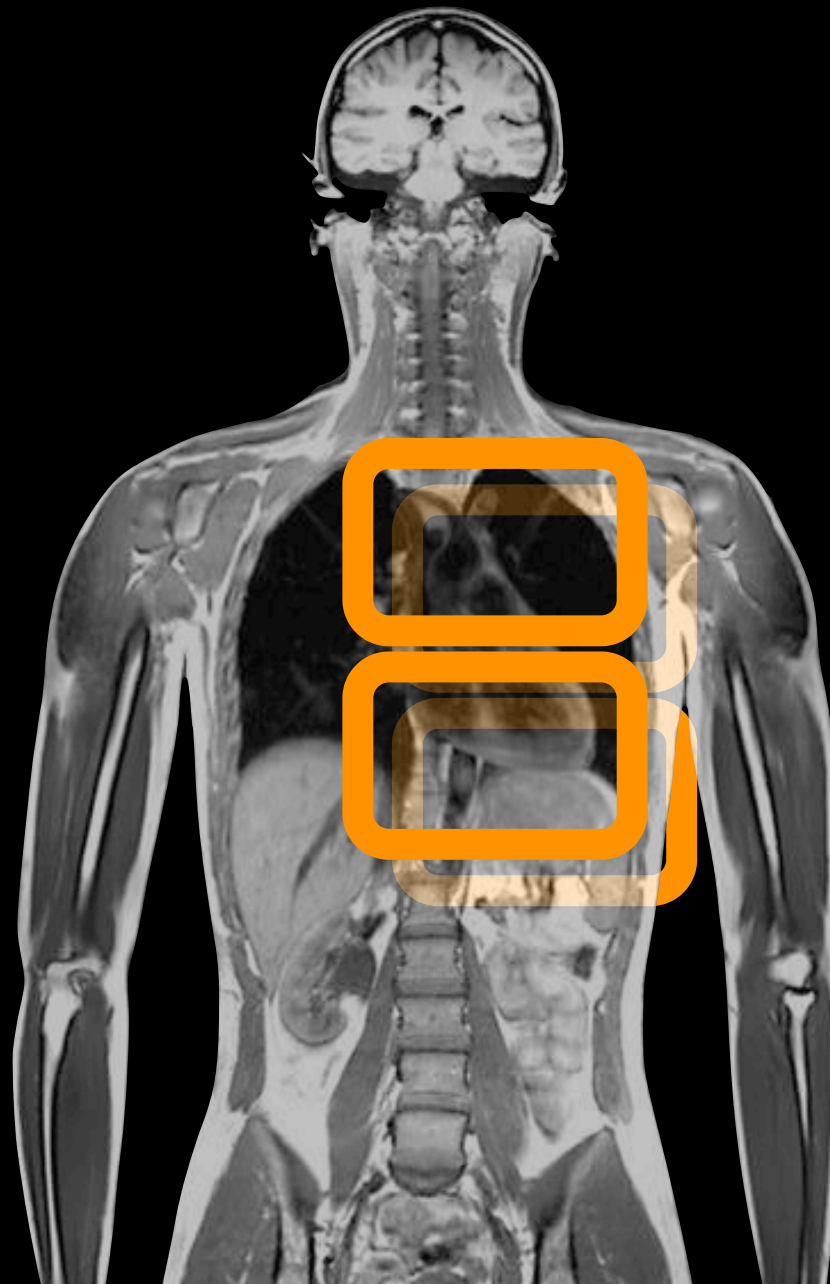
# 4-Channel Cardiac Coil

Each coil element has a unique sensitivity profile.



# 4-Channel Cardiac Coil

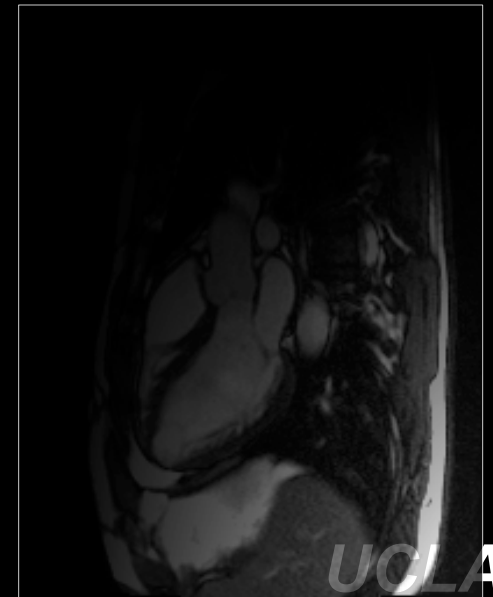
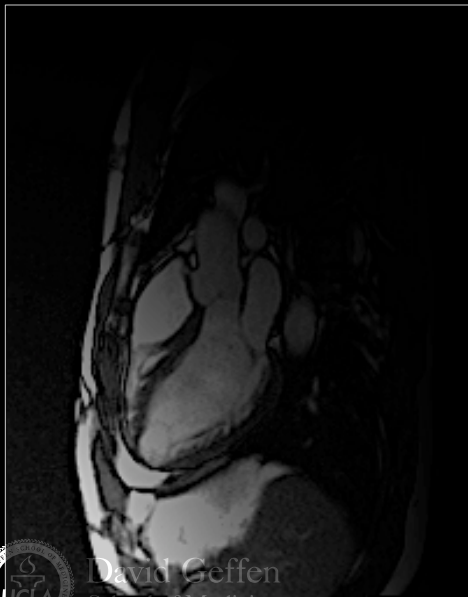
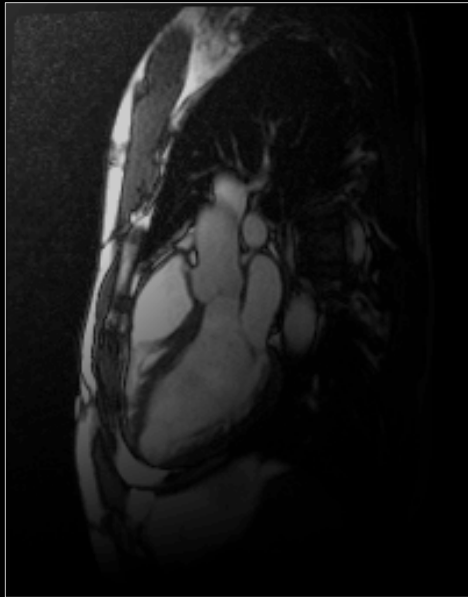
Each coil element has a unique sensitivity profile.



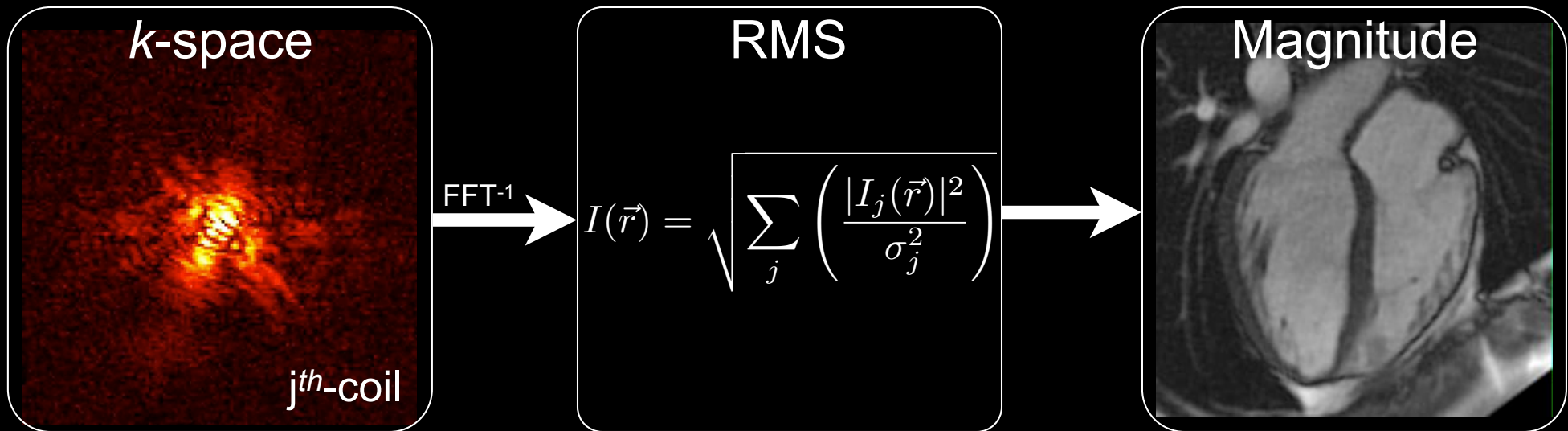


# 4-Channel Cardiac Coil

Coils are combined to form a single image.



# Multiple Coil Reconstruction



$I(\vec{r}) \rightarrow$  Final **magnitude** image

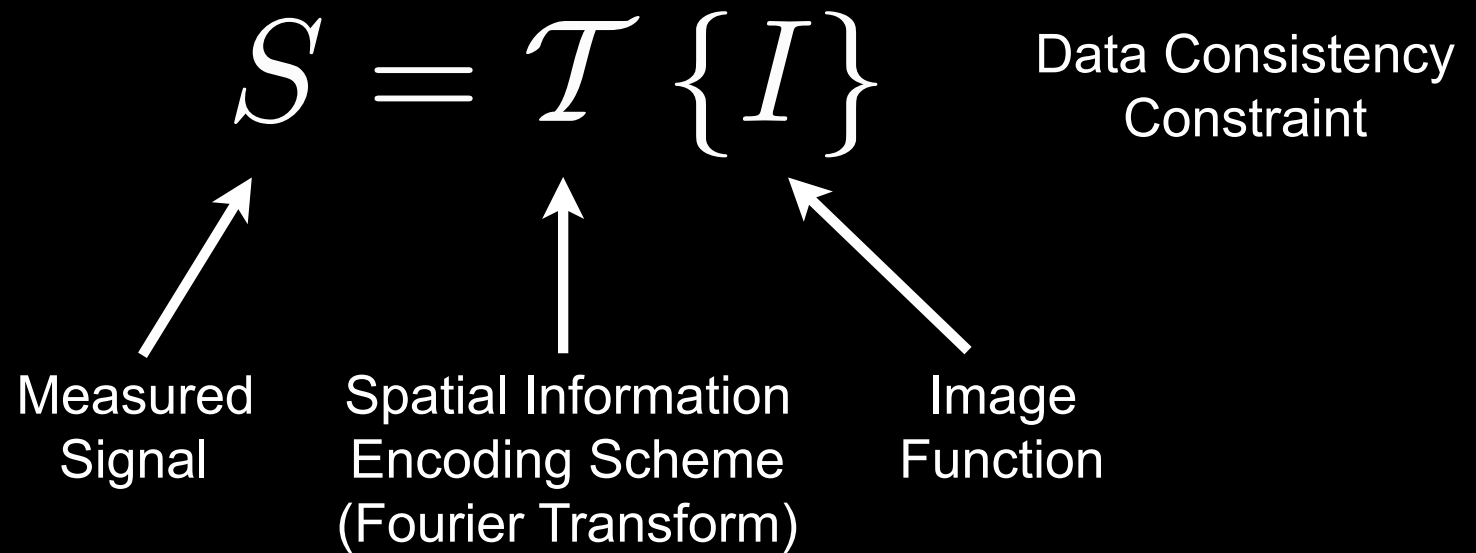
$I_j(\vec{r}) \rightarrow$  Image from  $j^{\text{th}}$  coil

$\sigma_j^2 \rightarrow$  Noise variance

- Depends on coil loading
- Proximity to patient
- Measured with “noise scan”
- Weights each coil’s contribution

# Image Reconstruction

# Image Reconstruction



$$I = \mathcal{T}^{-1} \{S\}$$

Our task is to recover  $I$  from the measured signals.

# MR Signal Equation

$$s(t) = \int \int_{x,y} \vec{M}_{xy}^0(\vec{r}) \cdot e^{-i\Delta\omega(\vec{r})t} d\vec{r}$$

The MRI Signal Equation is the...

$$s(t) = \int \int_{x,y} \vec{M}_{xy}^0(x,y) \cdot e^{-i\Delta\omega(x,y)t} dx dy$$

...2D Fourier Transform!

$$\Delta\omega(x,y) = \gamma G_x \cdot x + \gamma G_y \cdot y$$

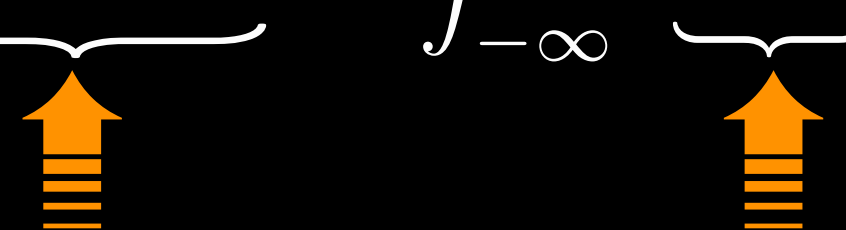
Gradients define  $\Delta\omega$   
(spatial frequencies)

$$k_x(t) = \frac{\gamma}{2\pi} G_x t \quad k_y(t) = \frac{\gamma}{2\pi} G_y t$$

k-space is convenient...

$$s(k_x(t), k_y(t)) = \int \int_{x,y} \underbrace{\vec{M}_{xy}^0(x,y)}_{I(\vec{r})} \cdot e^{-i2\pi[k_x(t)x + k_y(t)y]} dx dy$$

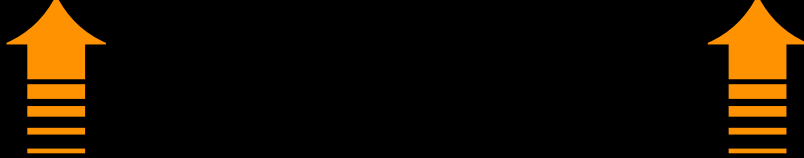
# Image Reconstruction

$$S[n] = \underbrace{S(n\Delta k_x)} = \int_{-\infty}^{+\infty} \underbrace{I(x)} e^{-i2\pi n\Delta k_x \cdot x} dx$$


This is what we measure!

This is what we want!


# Image Reconstruction

$$S[n] = \underbrace{S(n\Delta k_x)} = \int_{-\infty}^{+\infty} \underbrace{I(x)} e^{-i2\pi n\Delta k_x \cdot x} dx \quad \text{Eqn. 6.9}$$


This is what we measure!

This is what we want!

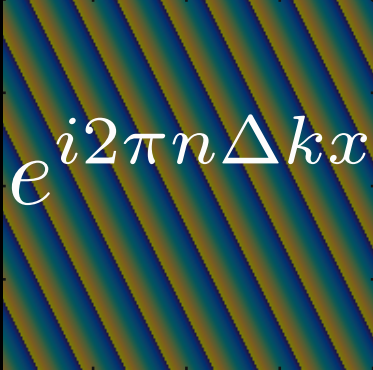
We can show the following...(Page 191 in Lauterbur).

$$\sum_{n=-\infty}^{\infty} S[n] e^{i2\pi n\Delta k x} = \frac{1}{\Delta k} \sum_{n=-\infty}^{\infty} I\left(x - \frac{n}{\Delta k}\right) \quad \text{Eqn. 6.10}$$


Fourier Series

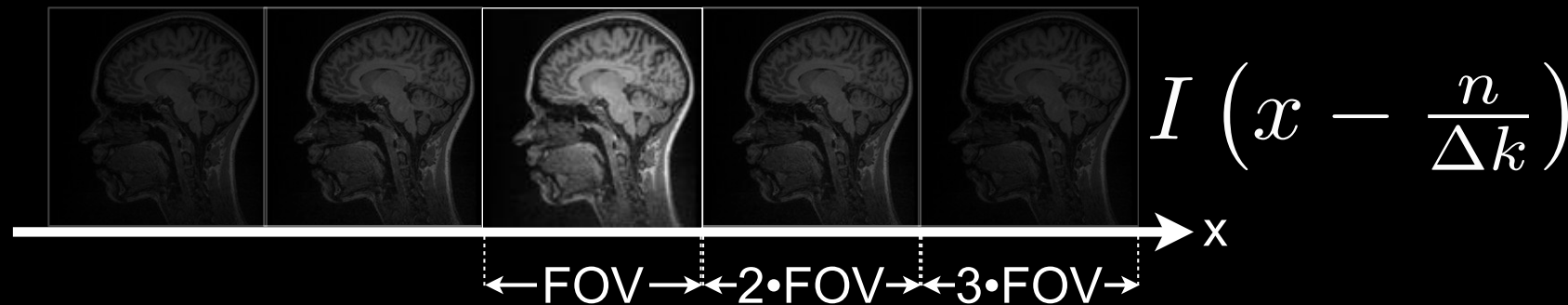
Periodic Extension of I(x)

# Image Reconstruction

$$\sum_{n=-\infty}^{\infty} S[n] e^{i2\pi n \Delta k x} = \frac{1}{\Delta k} \sum_{n=-\infty}^{\infty} I \left( x - \frac{n}{\Delta k} \right)$$


- Fourier series
- $\Delta k$  is the fundamental frequency
- $S[n]$  coefficient of the  $n^{\text{th}}$  harmonic

- Periodic extension of  $I(x)$
- $n$  is an integer
- Period is  $1/\Delta k = \text{FOV}$



Periodic extensions of a object/function.



# Finite Sampling

$S(k)$  is measured at  $k \in \mathcal{D}$

$$\mathcal{D} = \{n\Delta k, -N/2 \leq n \leq +N/2\}$$



Fourier  
Step-size



Number of  
Sample Points

$$I(x) = \Delta k \sum_{n=-N/2}^{N/2-1} S[n] e^{i2\pi n \Delta k x}, \quad |x| < \frac{1}{\Delta k} \quad \text{Eqn. 6.20}$$

# Spatial Resolution

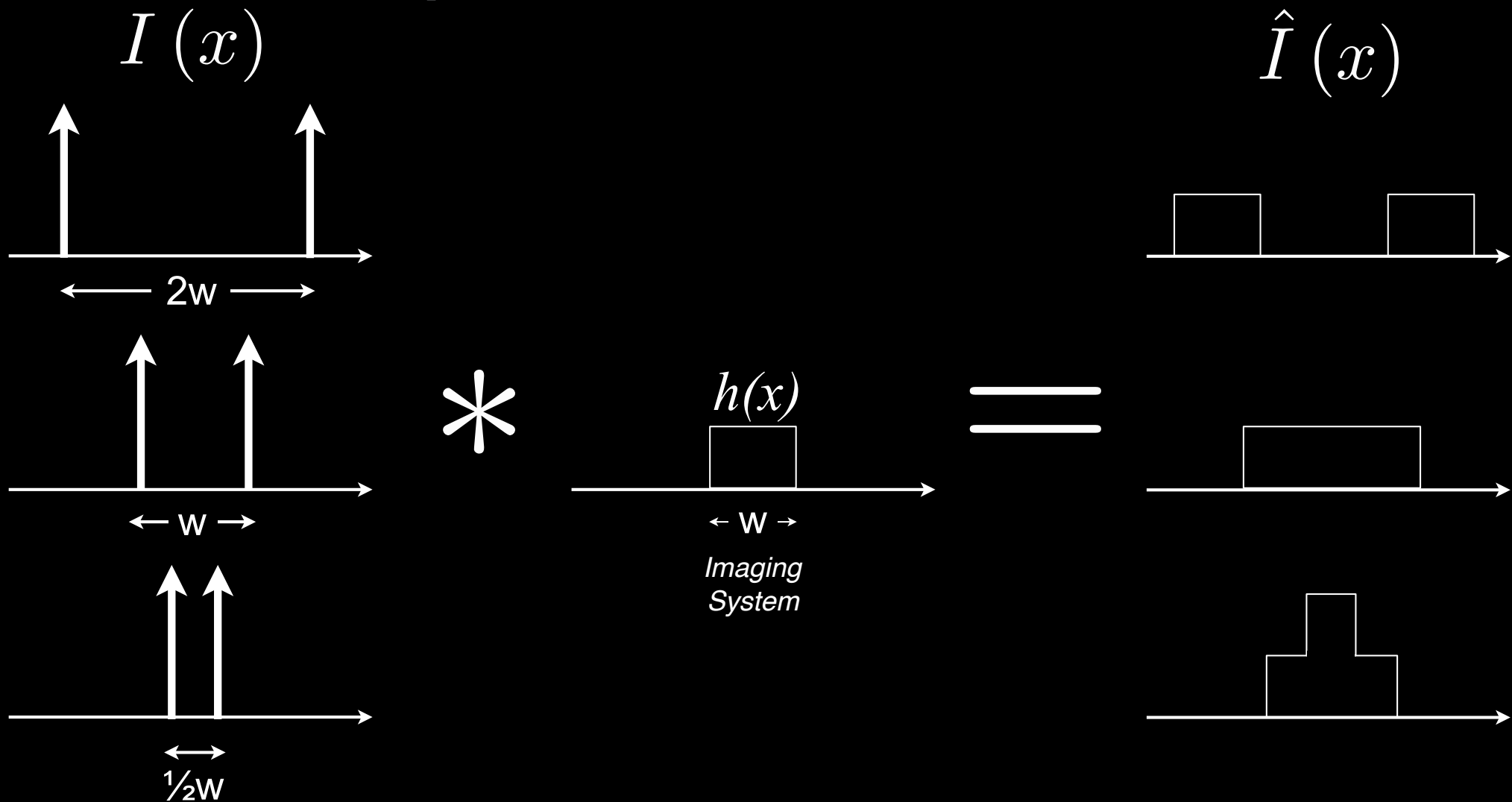
# Spatial Resolution

- **Spatial resolution of an imaging system is the smallest separation  $\delta x$  of two point sources necessary for them to remain resolvable in the resultant image.**

$$\hat{I}(x) = I(x) * h(x)$$

The diagram illustrates the relationship between the terms in the equation above. Three vertical arrows point upwards from the labels below to the corresponding terms in the equation:  $\hat{I}(x)$ ,  $I(x)$ , and  $h(x)$ . The label 'Image' is positioned below the first arrow, 'Object' below the second, and 'Point Spread Function' below the third. The word 'Point' is placed between the 'Point Spread Function' label and the arrow pointing to  $h(x)$ .

# Spatial Resolution

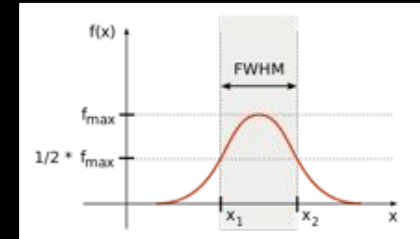


$$\hat{I}(x) = I(x), \text{ if and only if } h(x) = \delta(x)$$

# Spatial Resolution

- The resolution limit of an imaging system is the width ( $W_h$ ) of its point spread function:

- $W_h$  is the full-width half-max of  $h(x)$



- Alternately,

- $W_h$  of  $h(x)$  is the width of an approximating box-function with the same height and area as  $h(x)$ :

$$W_h = \frac{1}{h_{max}} \int_{-\infty}^{+\infty} h(x) dx$$

# Fourier Reconstruction PSF

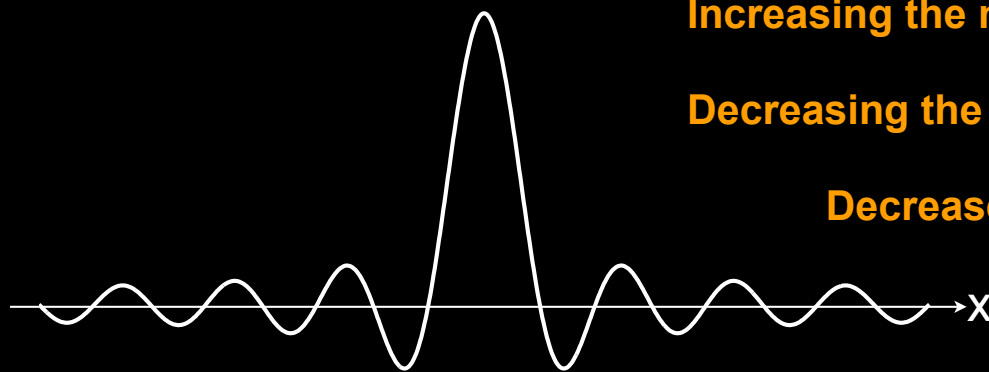
$$h(x) \approx \Delta k \frac{\sin(\pi N \Delta k x)}{\sin(\pi \Delta k x)} = \text{Dir}(N, \chi) \quad \text{Eqn. 8.7}$$

This is the approximate PSF for Fourier sampling.

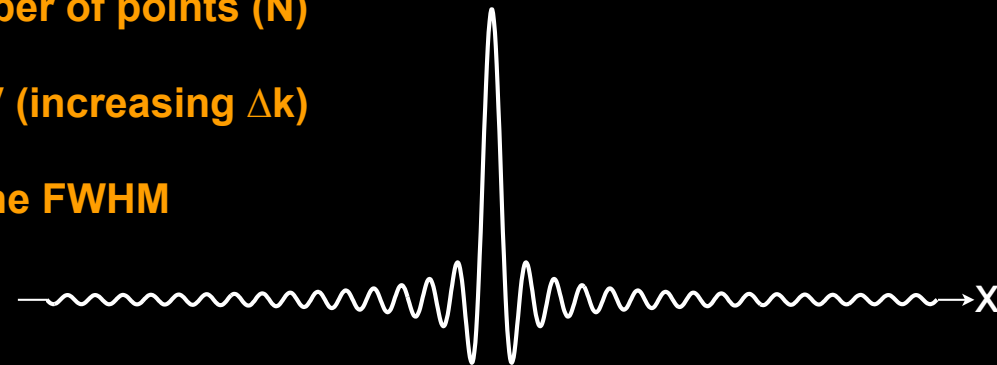
↑  
Dirichlet Function

Increasing the number of points (N)  
-or-  
Decreasing the FOV (increasing  $\Delta k$ )

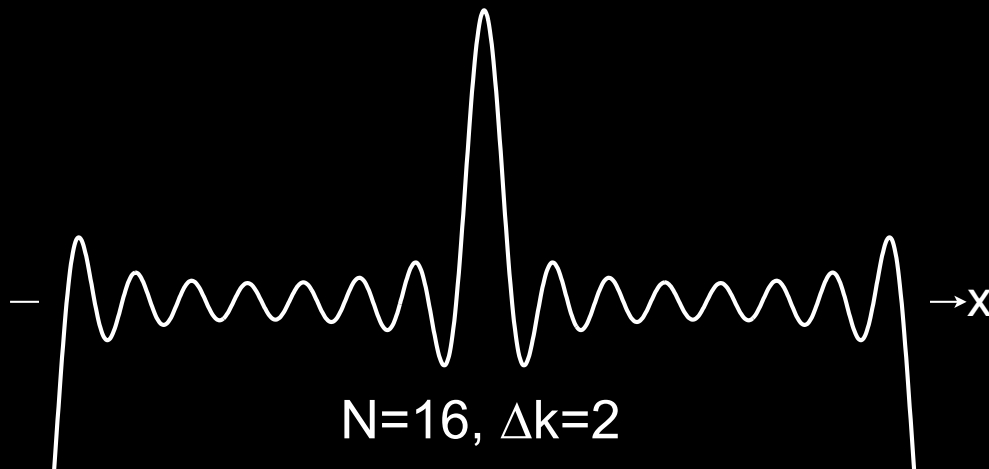
Decreases the FWHM



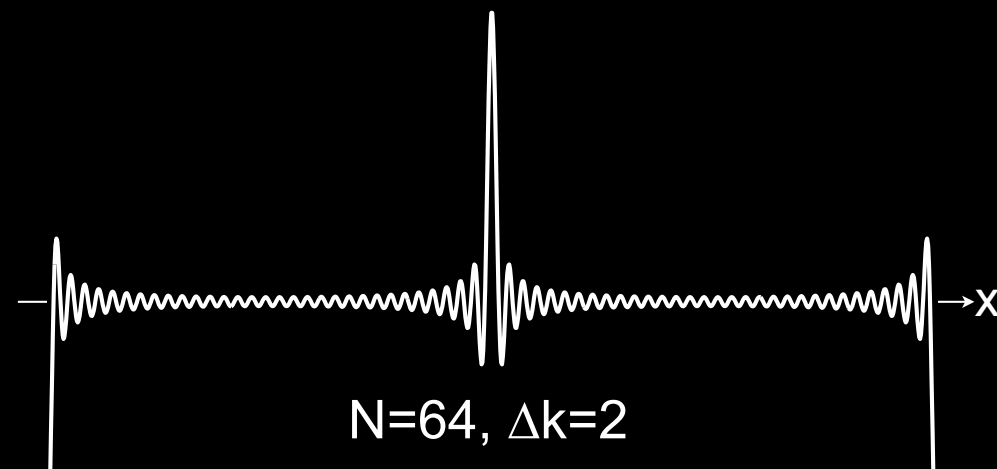
N=16,  $\Delta k=1$



N=64,  $\Delta k=1$



N=16,  $\Delta k=2$



N=64,  $\Delta k=2$

# Fourier Reconstruction PSF

$$W_h = \frac{1}{h_{max}} \int_{-\frac{1}{2\Delta k}}^{\frac{1}{2\Delta k}} h(x) dx = \frac{1}{N\Delta k}$$

↑  
Limits over a  
single period

↑  
Fourier Pixel Size  
( $\Delta x_F$ )

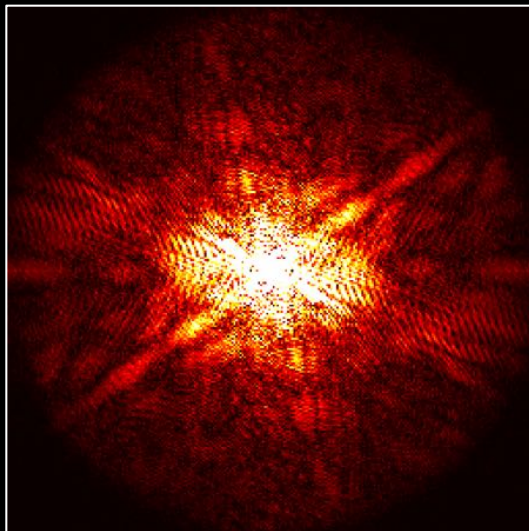
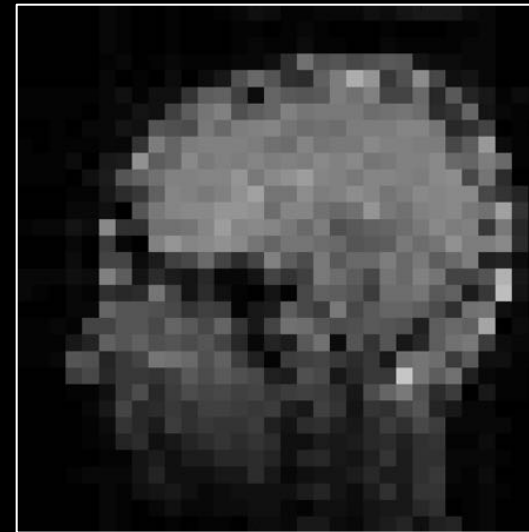
$$W_h = \frac{1}{N\Delta k} = \frac{FOV}{N}$$

Note, we can't reduce  $W_h$  and  $N$  simultaneously, therefore

- An increase in spatial resolution (decrease in  $W_h$ ) requires an increase in  $N$  or  $\Delta k$  (decrease in FOV)
- A decrease in spatial resolution (increase in  $W_h$ ) requires a decrease in  $N$  or  $\Delta k$  (increase in FOV)

# Finite Sampling

$$W_h = \frac{1}{N\Delta k} = \frac{FOV}{N}$$



**What is the same between the two acquisitions? Different?**



# Field of View

$FOV_x$

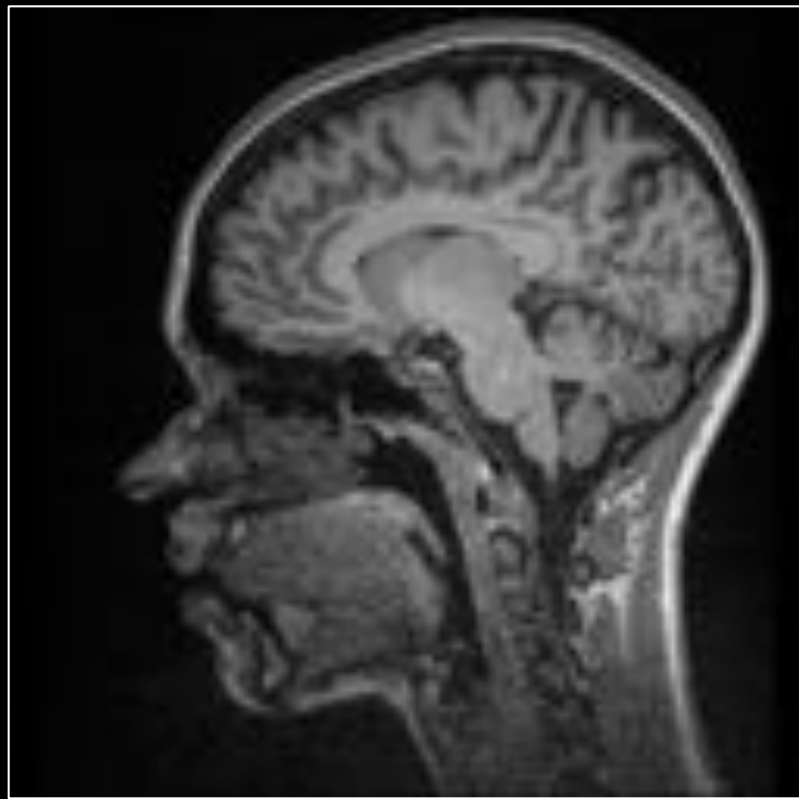
$$\Delta k_x = \frac{1}{FOV_x} = \gamma |\mathbf{G}_x| \Delta t \quad \text{Eqn. 5.123}$$

FOV constraints during readout.

$FOV_y$

$$\Delta k_y = \frac{1}{FOV_y} = \gamma \Delta \mathbf{G}_y T_{pe} \quad \text{Eqn. 5.123}$$

FOV constraints during phase encoding.



# Field of View

$FOV_x$

$$\Delta k_x = \frac{1}{FOV_x} = \gamma |\mathbf{G}_x| \Delta t$$

Eqn. 5.123

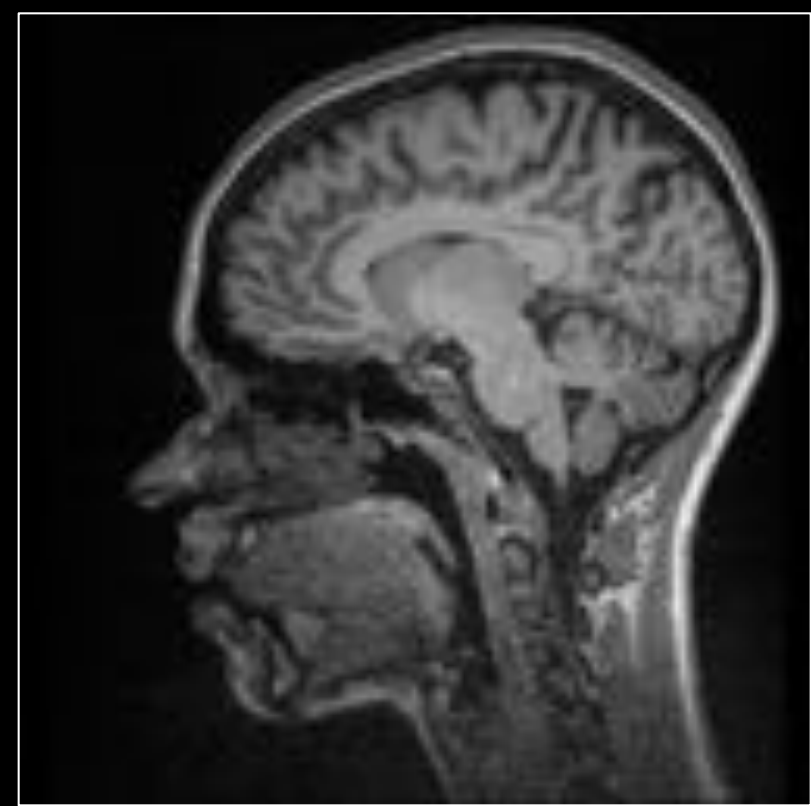
$$\Delta k_y = \frac{1}{FOV_y} = \gamma \Delta \mathbf{G}_y T_{pe}$$

$$\Delta t = \frac{1}{\gamma |\mathbf{G}_x| FOV_x}$$

Eqn. 5.124

$$\Delta \mathbf{G}_y = \frac{1}{\gamma T_{pe} FOV_y}$$

$FOV_y$





# Imperfections & Artifacts

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<http://www.ajronline.org/doi/pdf/10.2214/ajr.182.2.1820532>



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# Lecture #14 - Learning Objectives

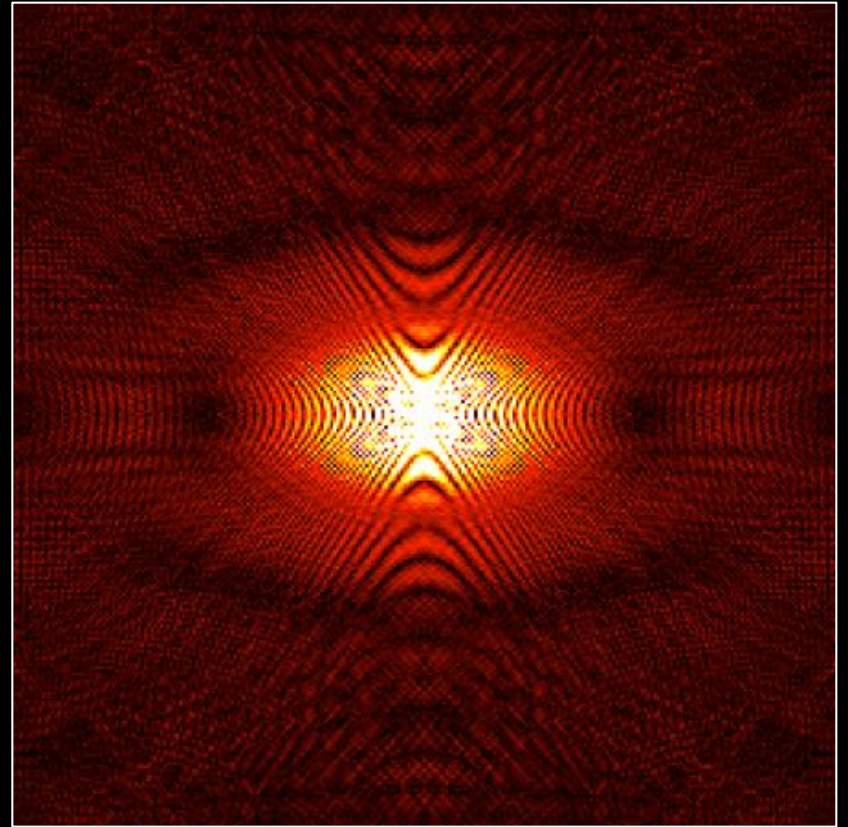
- Describe the origin and correction for several artifacts.
- Understand the impact of spatial resolution and scan time on signal-to-noise ratio.
- Explain the importance of readout bandwidth and the +/- of high (or low) readout bandwidth.
- Define the origin, artifact, and possible correction for chemical shift artifacts.
- Appreciate why motion causes image artifacts in MRI
- Be able to identify several artifacts in an MR image.

# Gibb's Ringing

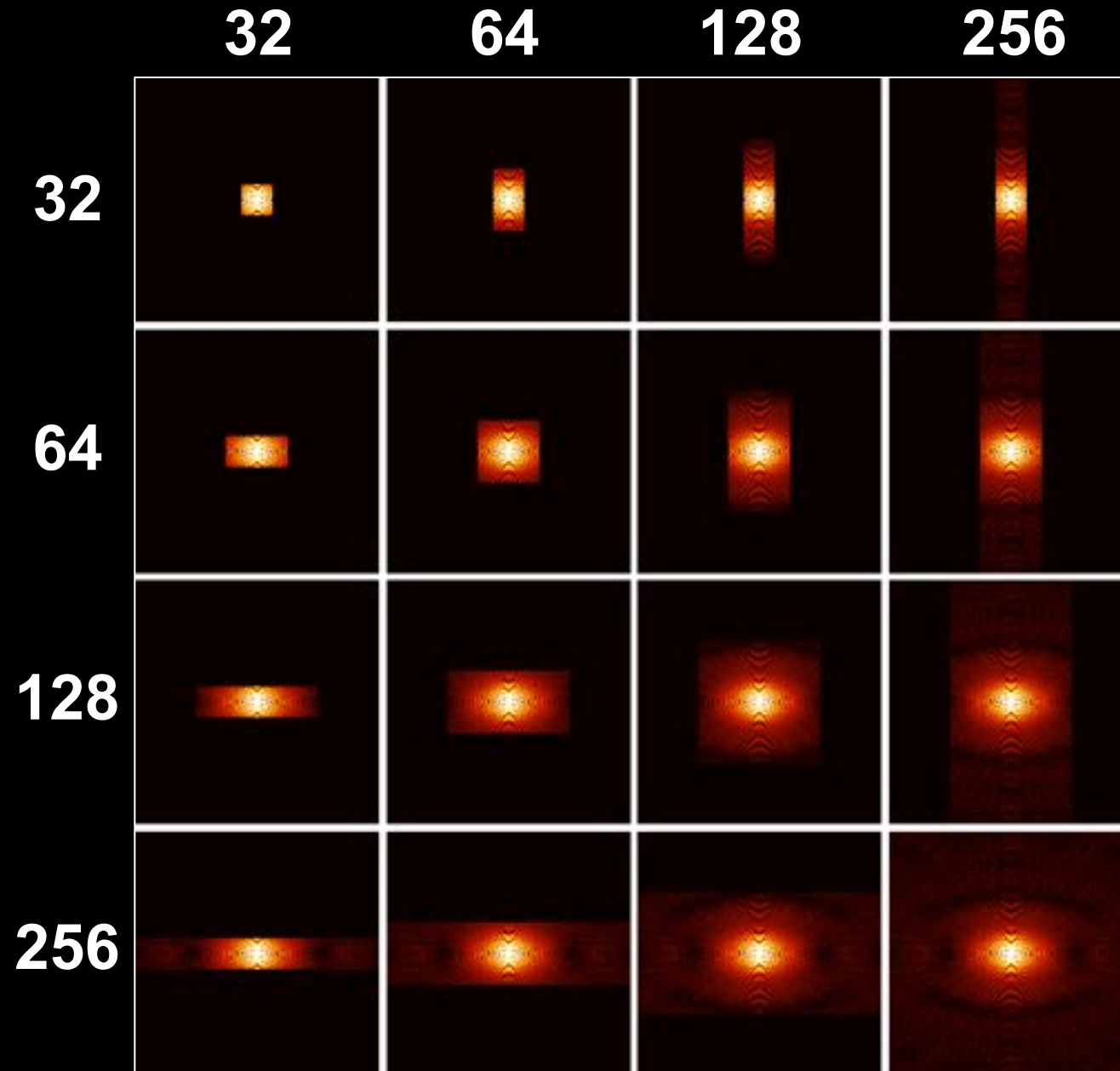
# Gibb's Ringing

- **Spurious ringing around sharp edges**
- **Max/Min overshoot is ~9% of the intensity discontinuity**
  - Independent of the # of recon points
  - Frequency of ringing increases as # of recon points increases
    - Ringing becomes less apparent
- **Result of truncating the Fourier series model as a consequence of finite sampling**
- **Can reduce by:**
  - Acquiring more data
  - Filtering the data which reduces oscillations in the PSF

# Shepp-Logan



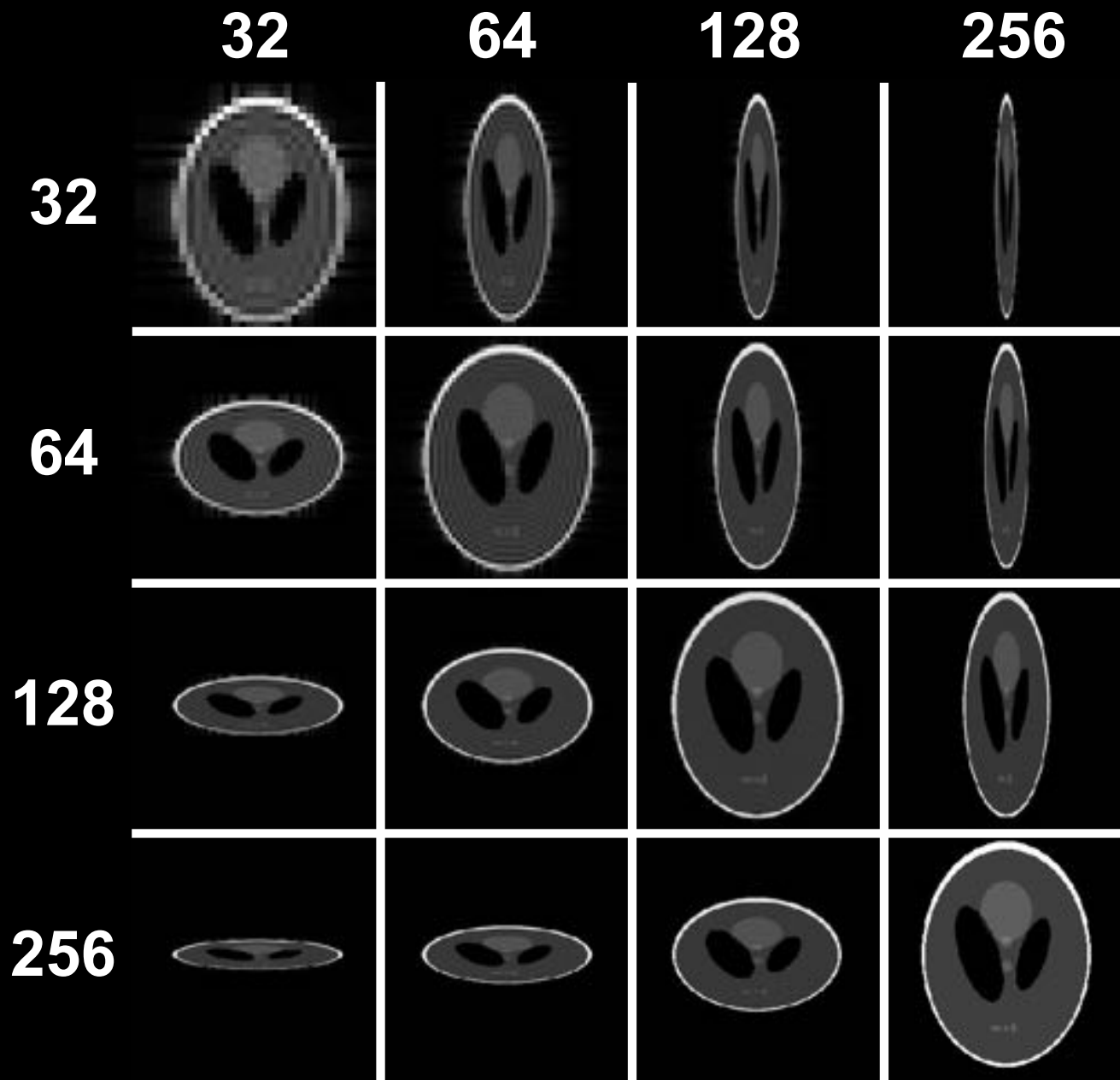
# Gibb's Ringing



What is the difference between these acquisitions?

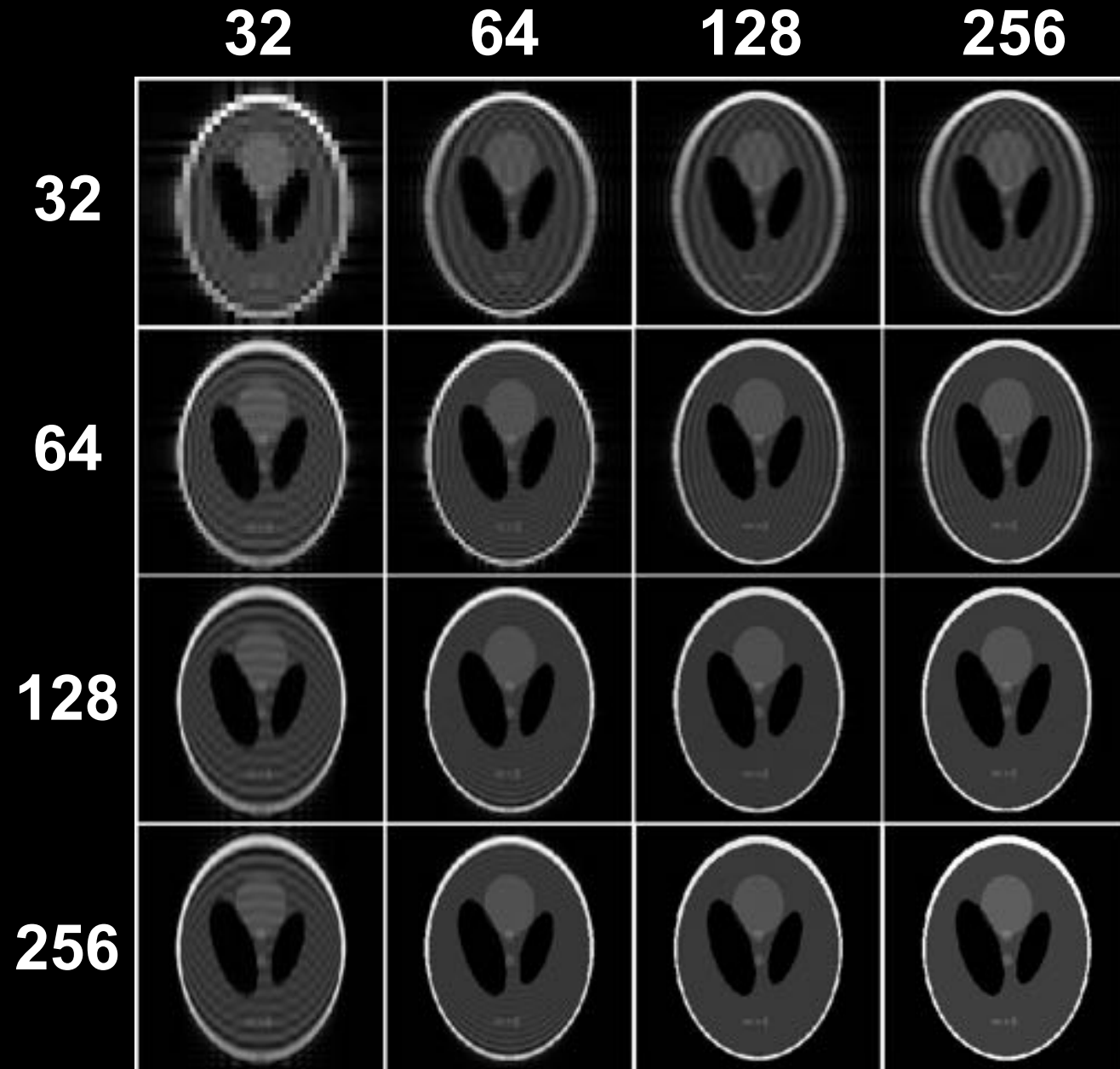


# Gibb's Ringing



Why do the images look like this?

# Zero-Pad



# Windowed Reconstruction

# Windowed Reconstruction

$$\hat{I}(x) = \Delta k \sum_{n=-N/2}^{N/2-1} S(n\Delta k) e^{i2\pi n\Delta kx}$$

Fourier reconstruction

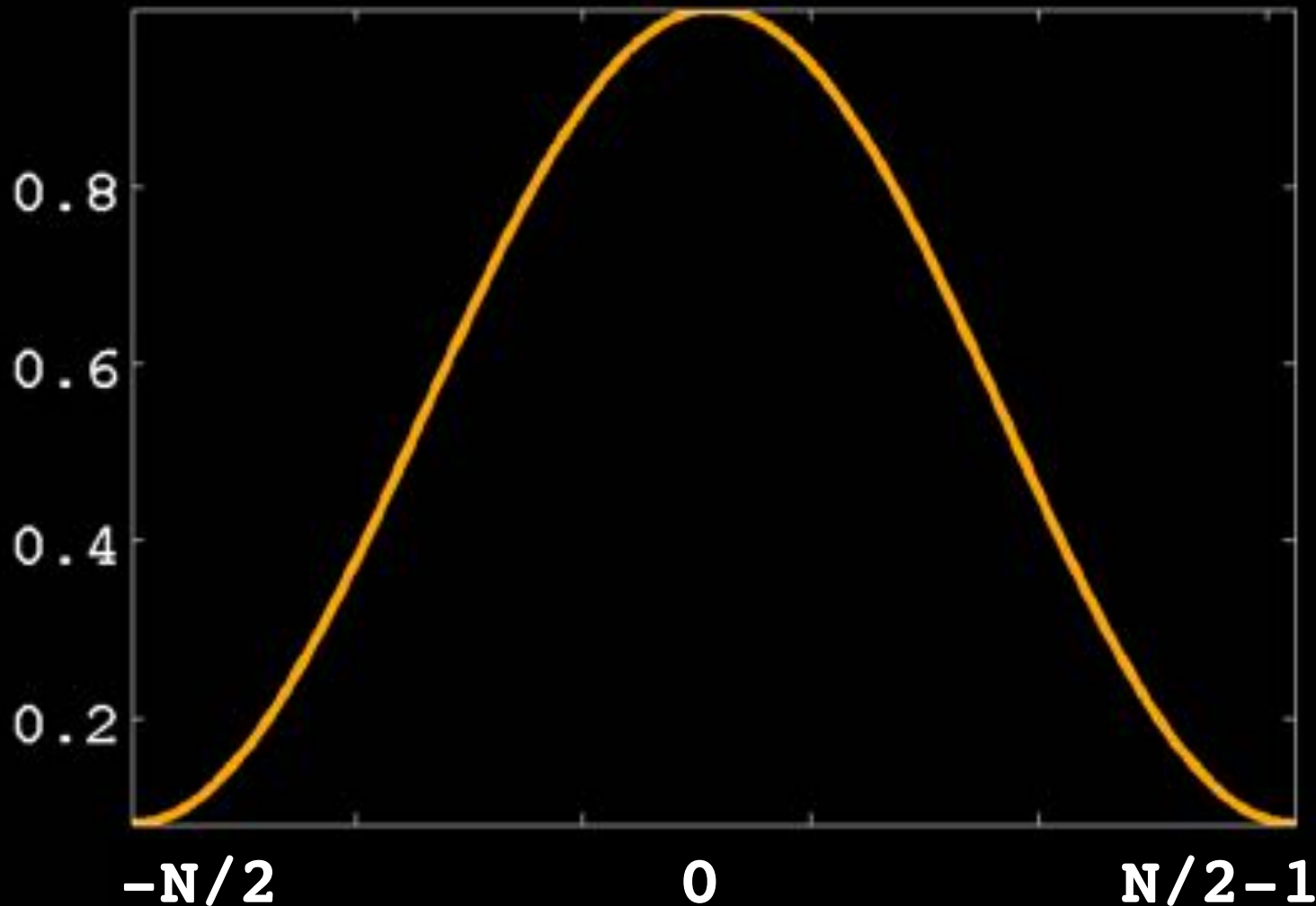
$$\hat{I}(x) = \Delta k \sum_{n=-N/2}^{N/2-1} S(n\Delta k) w_n e^{i2\pi n\Delta kx} \quad \text{Eqn. 6.21}$$

Windowed Fourier  
reconstruction

↑  
*k*-space  
filter/window  
function

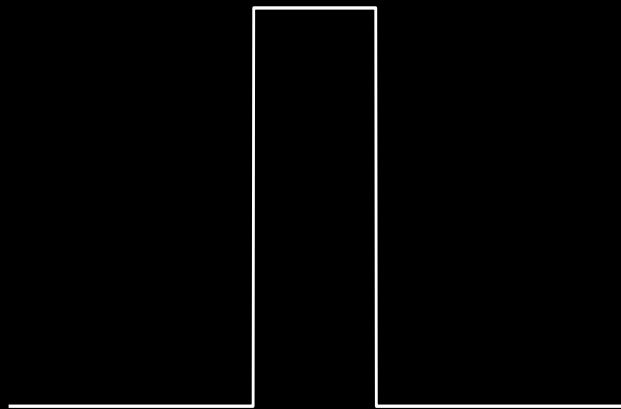
# Hamming Filter - 1D

$$w(n) \triangleq \begin{cases} 0.54 + 0.46 \cos(2\pi \frac{n}{N}) & -N/2 \leq n \leq N/2 - 1 \\ 0 & \text{otherwise} \end{cases}$$



# Windowed Reconstruction

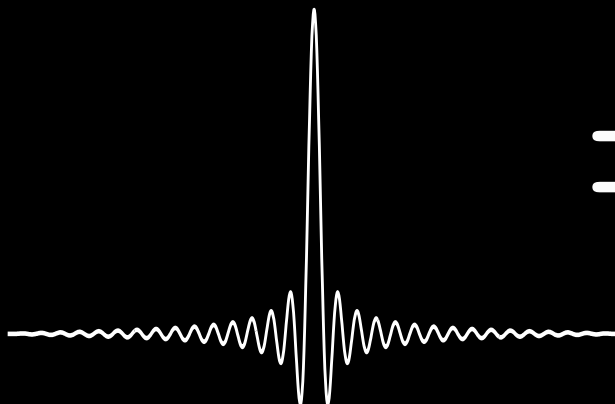
$I(x)$



True Object

\*

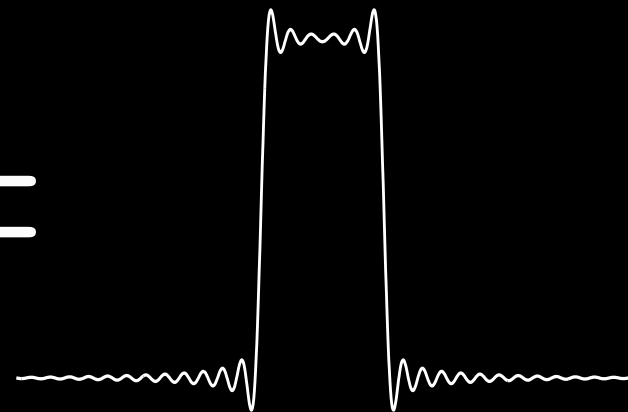
$h(x)$



Fourier Recon PSF

=

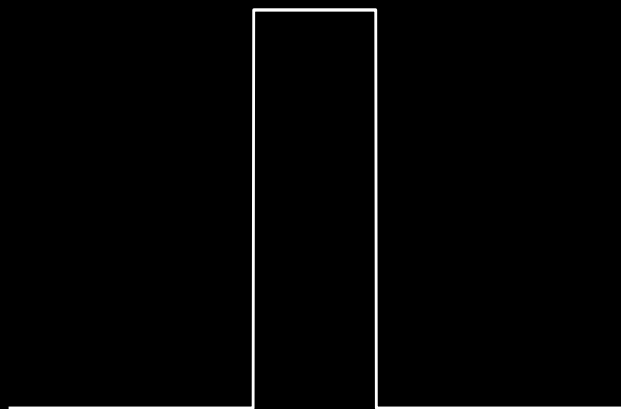
$\hat{I}(x)$



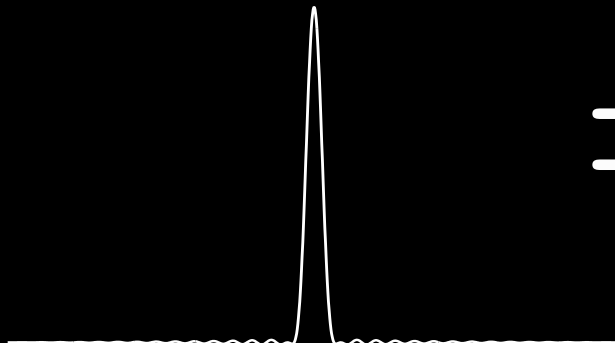
Fourier Recon

\*

True Object

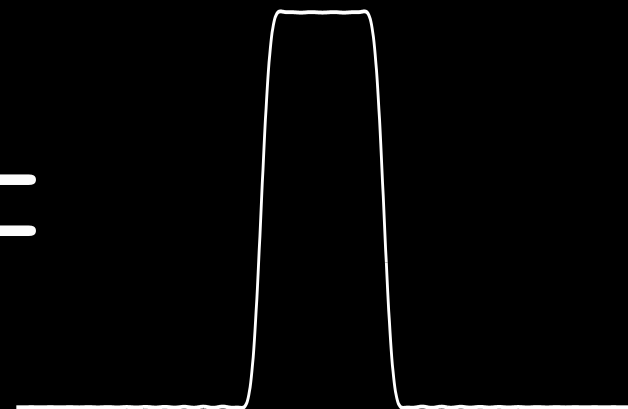


Hamming  
Weighted PSF



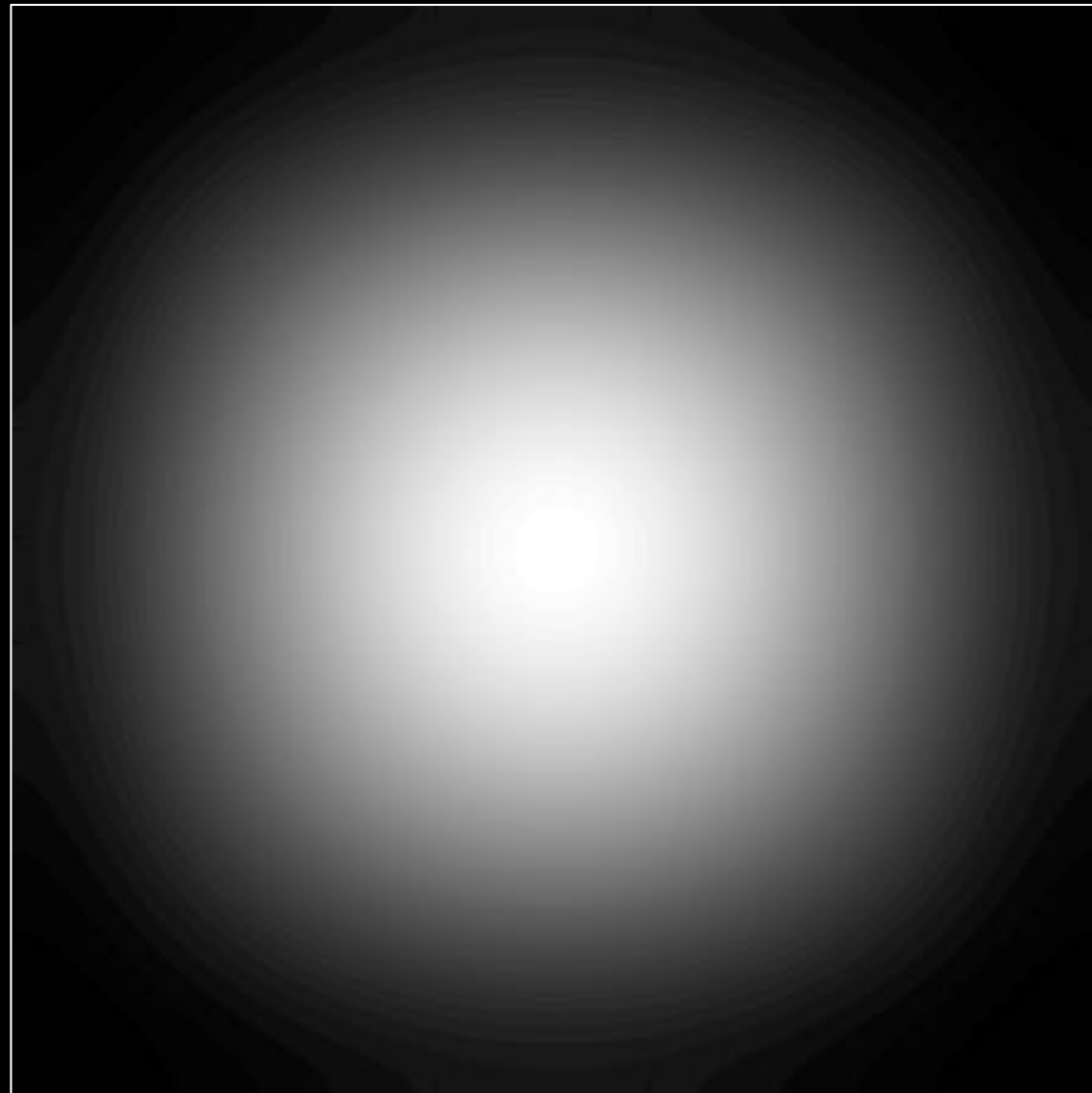
=

Hamming Windowed  
Fourier Recon

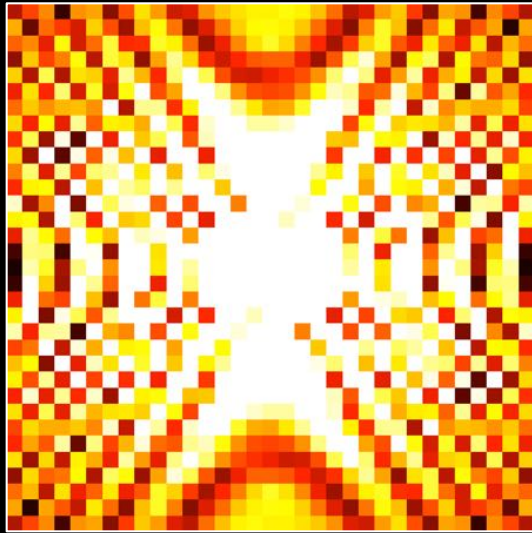


# Hamming Filter - 2D

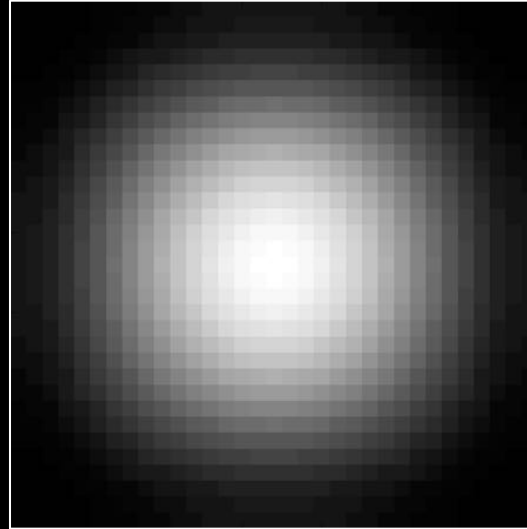
$$W(n) \triangleq w(n) \otimes w(n)$$



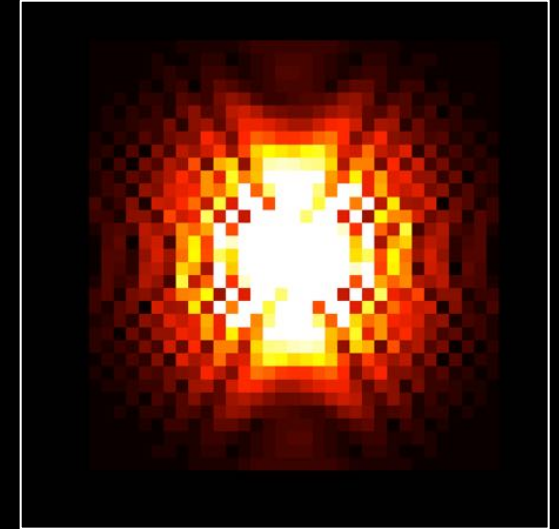
# Hamming Filter



●  
Dot  
Multiply



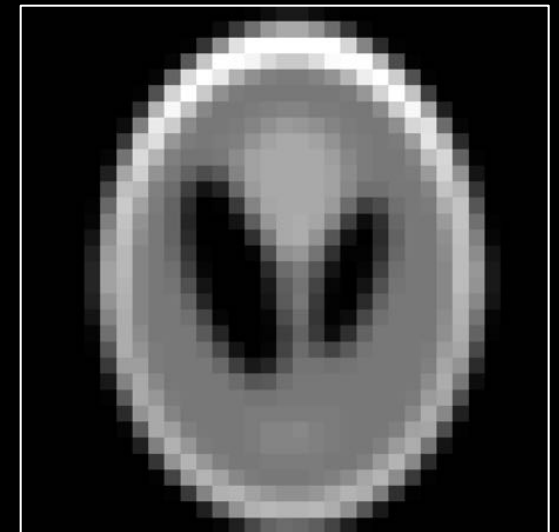
=



≡  
↓  
FFT

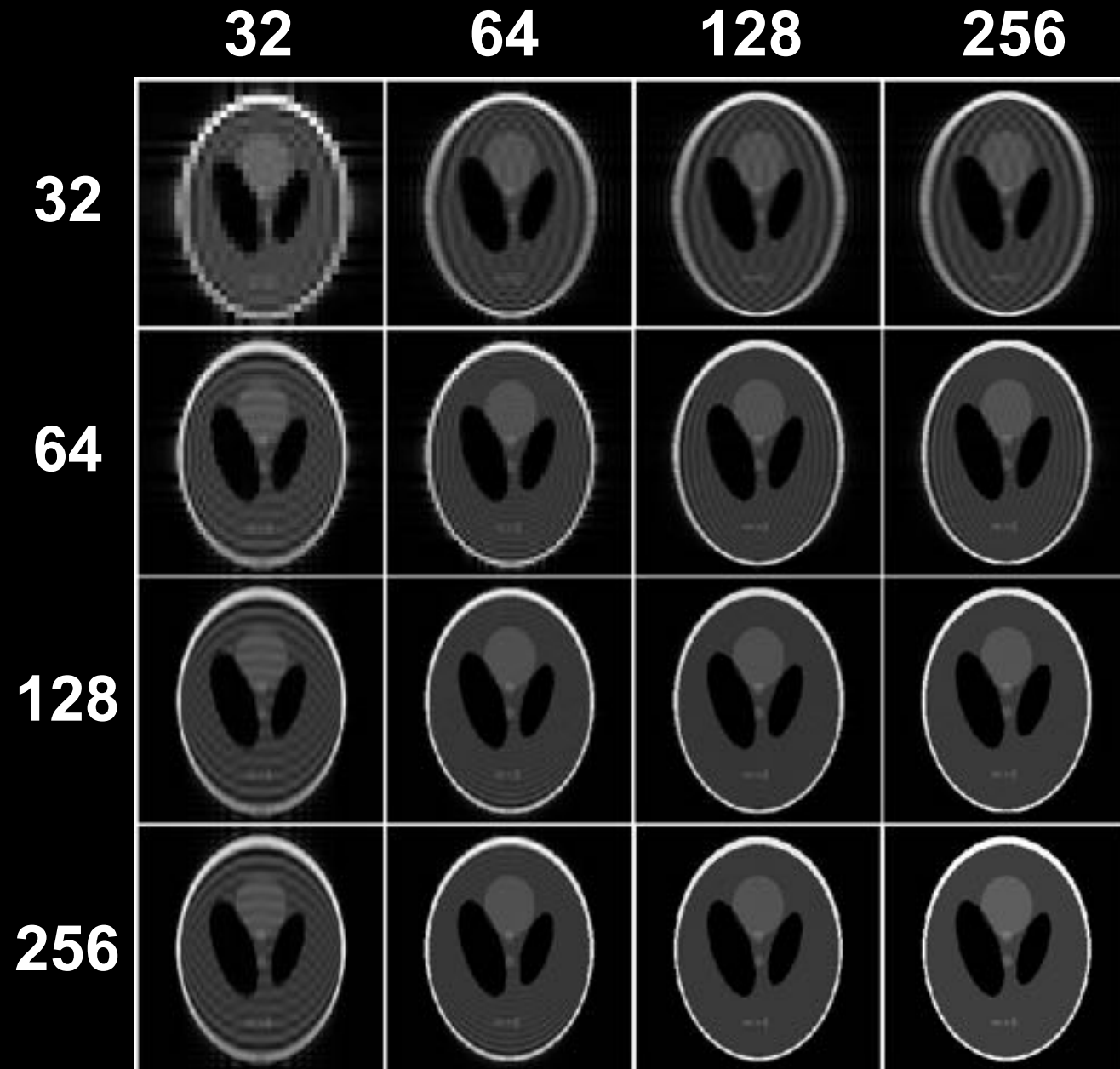


≡  
↓  
FFT



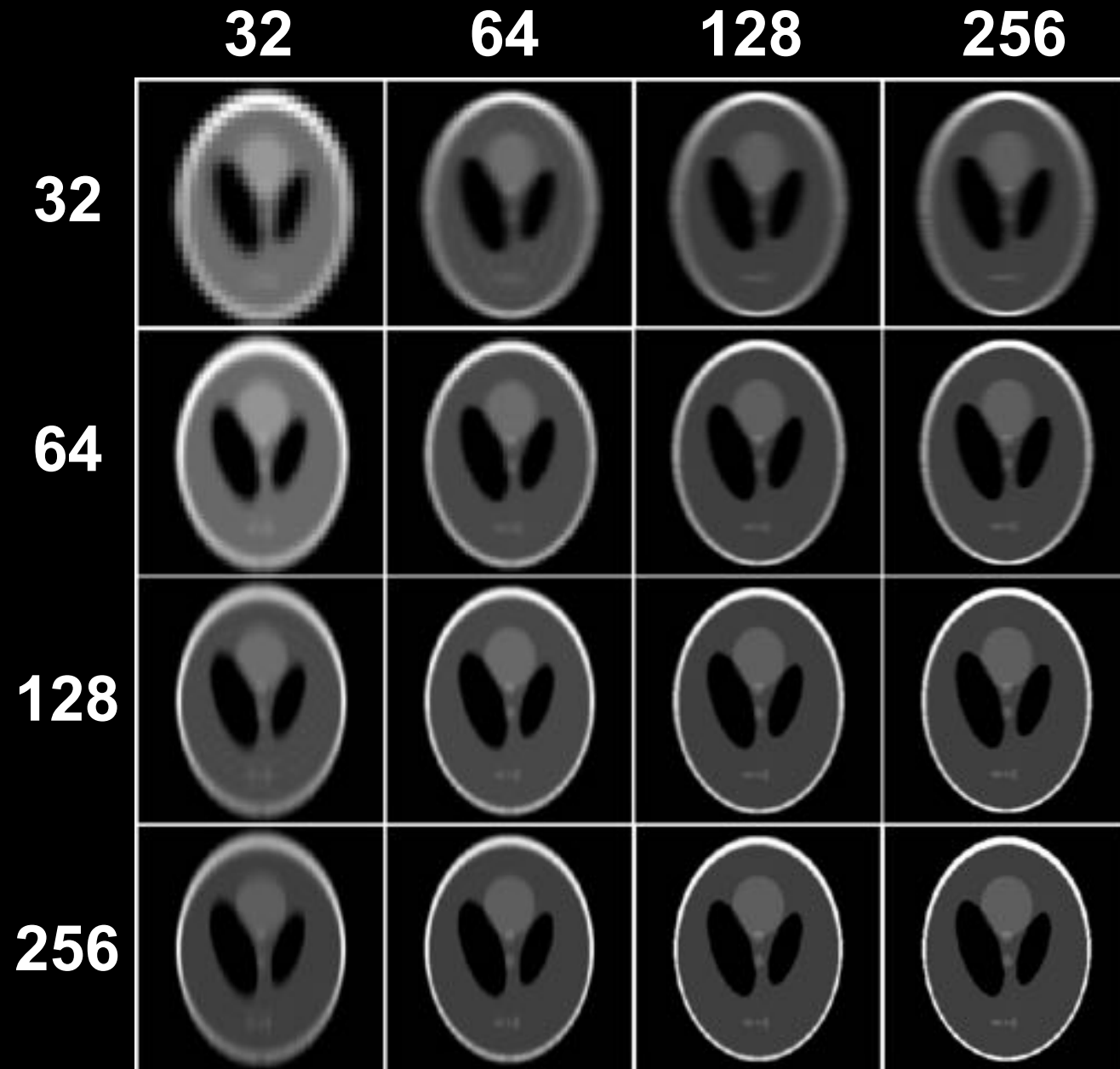


# Zero-Pad



With zero padding only, Gibbs ringing is evident.

# Hamming Window & Zero-Pad



Windowing  $k$ -space mitigates Gibb's ringing, but blurs a little.

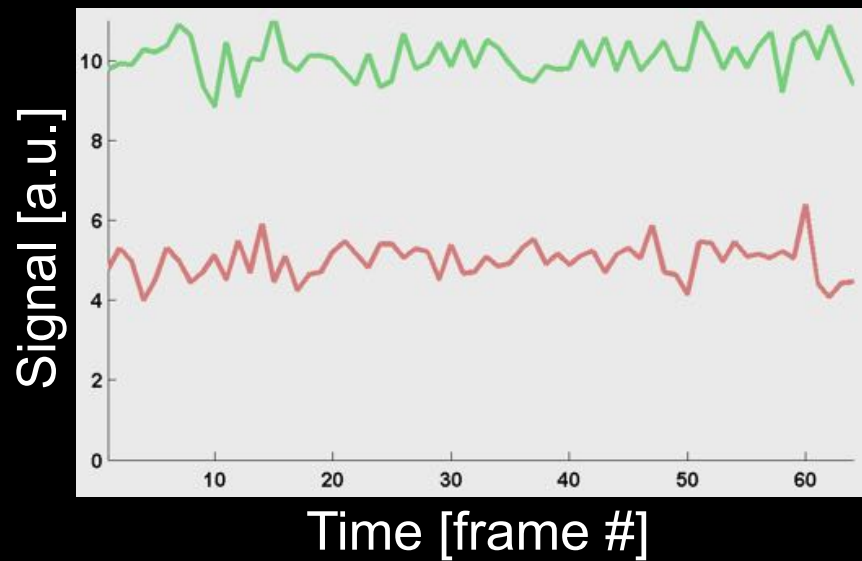
**Artifacts**

# Artifacts

- Aliasing
- Gibb's Ringing
- Noisy spike artifacts
- Noise
- Chemical shift
- Motion Artifacts
- Metal artifacts
- Gradient Non-linearity
- Data clipping
- RF interference
- And more...

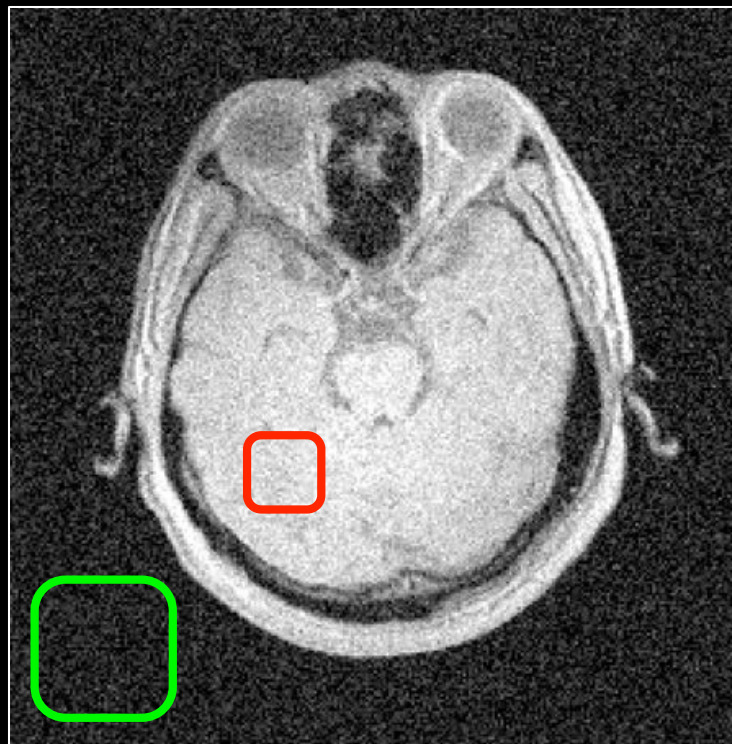
Noise

# Signal-to-Noise Ratio



# Signal-to-Noise Ratio

- **SNR – Signal-to-noise ratio**
  - **Signal** – Mean signal intensity in ROI. Assumes:
    - 1) Tissue homogeneity
    - 2) Noise is only source of variance
  - **Noise** – SD of background ROI outside object. Assumes:
    - 1) Noise is only source of variance



This method of measuring the SNR is widespread, but imperfect.

# Signal-to-Noise Ratio

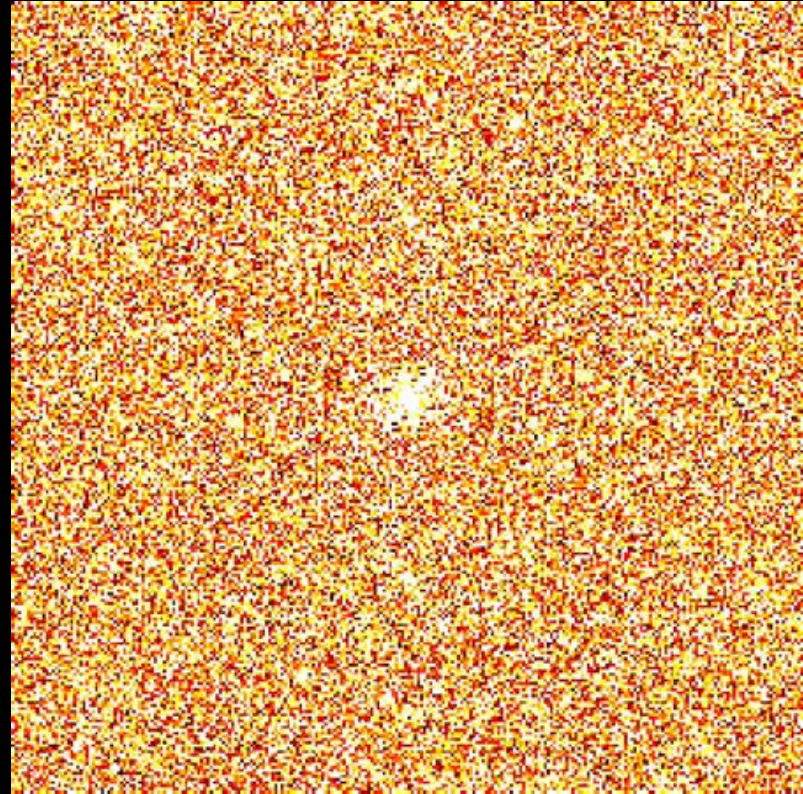
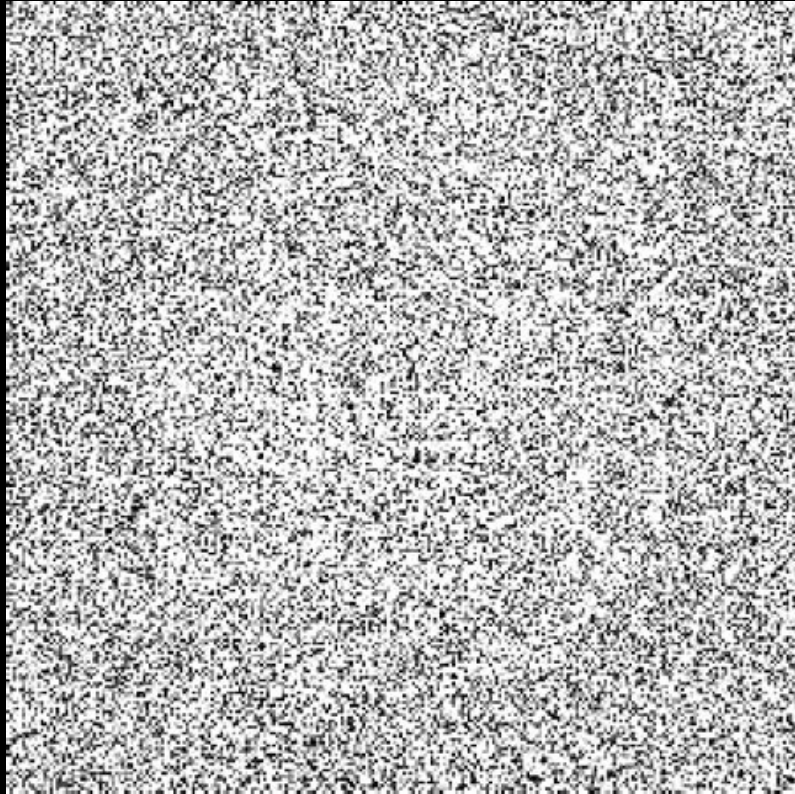
$$SNR \triangleq \frac{\text{signal amplitude}}{\text{standard deviation of noise}}$$

- **SNR – Signal-to-noise ratio**
  - **Signal** – Mean signal intensity in ROI
  - **Noise** – Standard deviation of noise
- **CNR - Contrast-to-noise ratio**
  - **Signal Difference**
    - Difference between mean signal intensity in two ROIs
  - **Noise** - Standard deviation of noise

$$CNR \triangleq \frac{\text{signal difference}}{\text{standard deviation of noise}}$$



# What is the FT of noise? Noise.



To The Board...

# SNR & Imaging Parameters

- **Gradient Echo vs. Spin Echo**
- **TR, TE, TI**
- **Flip Angle (Gradient Echos)**
- **Field of View (FOV)**
  - Square or Rectangular
- **Slice Thickness (h)**
- **Matrix Size**
  - Number of readout points (x)
  - Number of phase encodes (y)
- **Bandwidth (Hz)**
  - AKA Pixel Bandwidth (Hz/pixel)

# Signal-to-noise Ratio

$$SNR \propto V \sqrt{t}$$

Large Voxels (Low Resolution)  $\Leftrightarrow$  High SNR

Long Scan Time  $\Leftrightarrow$  High SNR

High Resolution + Fast Imaging Severely Compromises SNR

# Signal-to-noise Ratio

$$SNR \propto V \sqrt{t}$$

- **V – Voxel Volume**
  - Slice-thickness (h) x X-res x Y-res
    - X-res =  $FOV_x/N_{kx}$
    - Y-res =  $FOV_y/N_{ky}$
- **t – Data acquisition time**
  - $(N_{kx} \times N_{ky} \times N_{averages})/\text{bandwidth}$

$$SNR \propto \frac{FOV_x}{N_{kx}} \frac{FOV_y}{N_{ky}} h \sqrt{\frac{N_{kx} N_{ky} N_{avg}}{BW}}$$

# Signal-to-noise Ratio

$$SNR \propto V \sqrt{t}$$

- **Example #1**

- Halving slice thickness requires 4x averages to maintain SNR

- **Example #2**

- Doubling slice thickness requires 25% time to maintain SNR

- **Example #3**

- FOV is, in general, fixed.
- To increase resolution we increase  $N_{k_x}$  or  $N_{k_y}$ .
- This results in increased scan time, but
- The SNR decreases.

$$SNR \propto \frac{FOV_x}{N_{k_x}} \frac{FOV_y}{N_{k_y}} h \sqrt{\frac{N_{k_x} N_{k_y} N_{avg}}{BW}}$$

# Parallel Imaging and SNR

$$SNR_{P.I.} = \frac{SNR}{g\sqrt{R}}$$

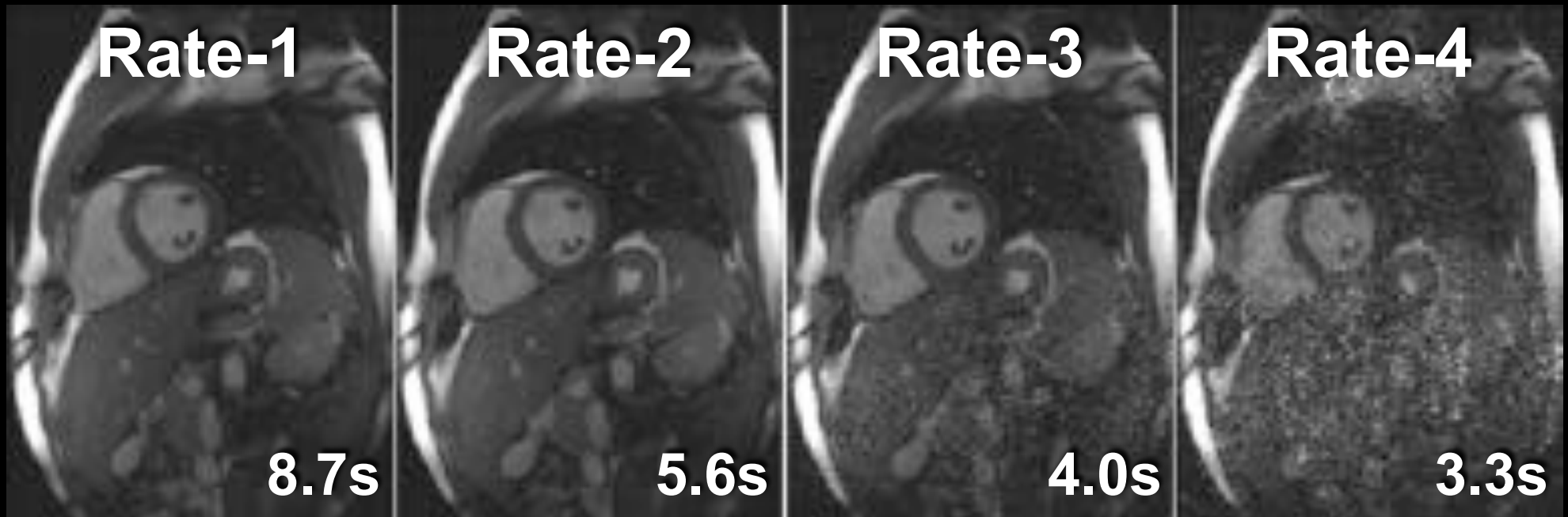
- **g - geometry factor**
  - Loss associated with coil noise-correlation
  - For R=1, g=1
  - For R=2, g=~1.1-1.5
- **R - reduction or acceleration factor**
  - Loss associated with scan time reduction
  - Typically ~1/2 N-coils
- **SNR for P.I. is spatially dependent**
  - Higher in areas of aliasing

Parallel imaging has additional SNR penalties, but decreases scan time.

# Impact of Acceleration

High SNR  
“Long” Acq.

Low SNR  
Short Acq.



P. Kellman (NIH)

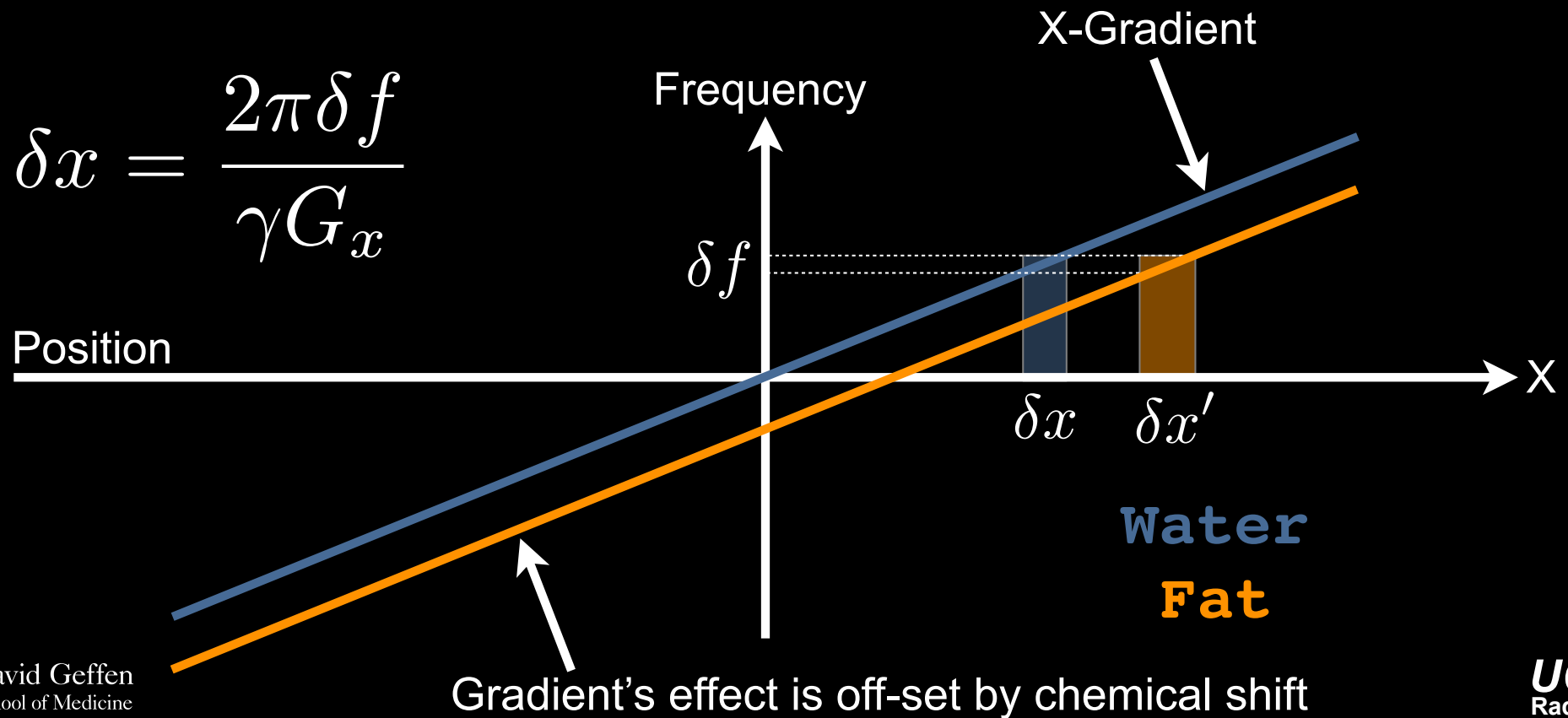
High acceleration rates lead to local noise amplification.



# Chemical Shift

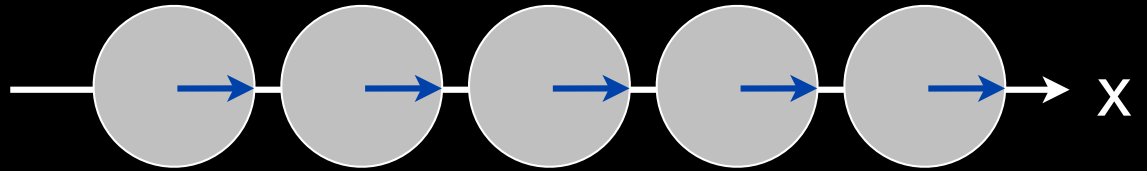
# Chemical Shift Artifact

- Gradients provide linear variation in frequency
- Fat has a 3.5ppm lower frequency than water
  - -222Hz @ 1.5T and -444Hz @ 3.0T
- Scanner detects frequency, then maps to position
- Scanner “assumes” everything is water, therefore fat (lower frequency) is interpreted as lower frequency (shifted position) water.

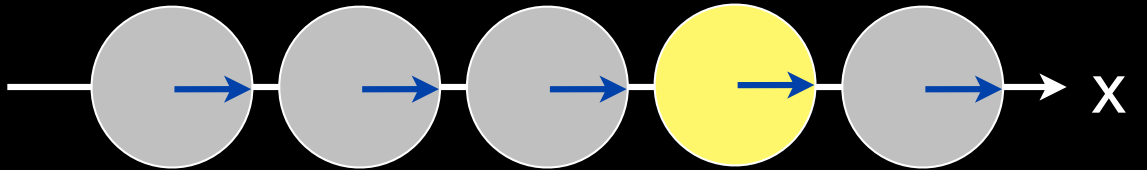


# Chemical Shift Artifact

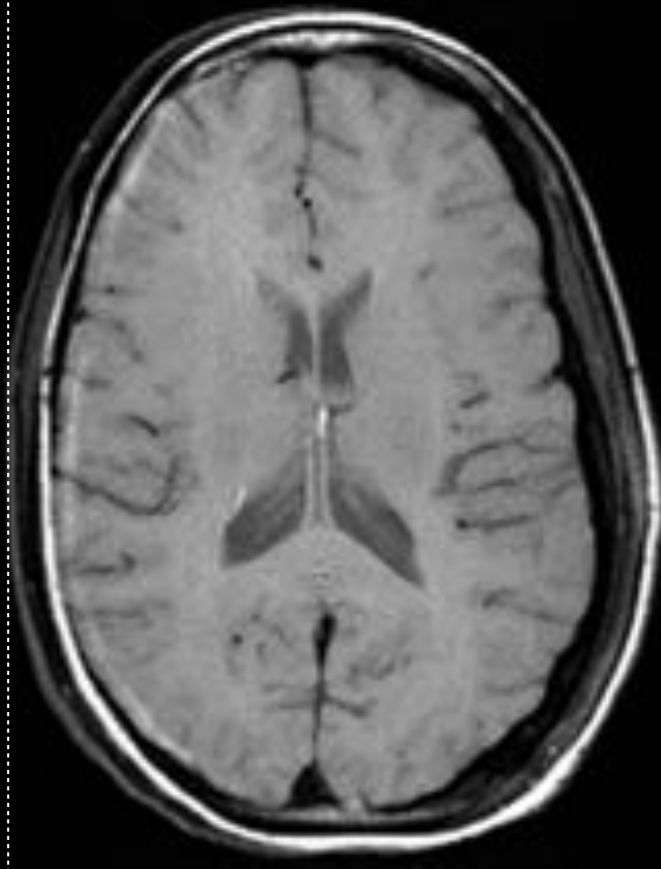
Normal Spins



Off-Resonant Spin

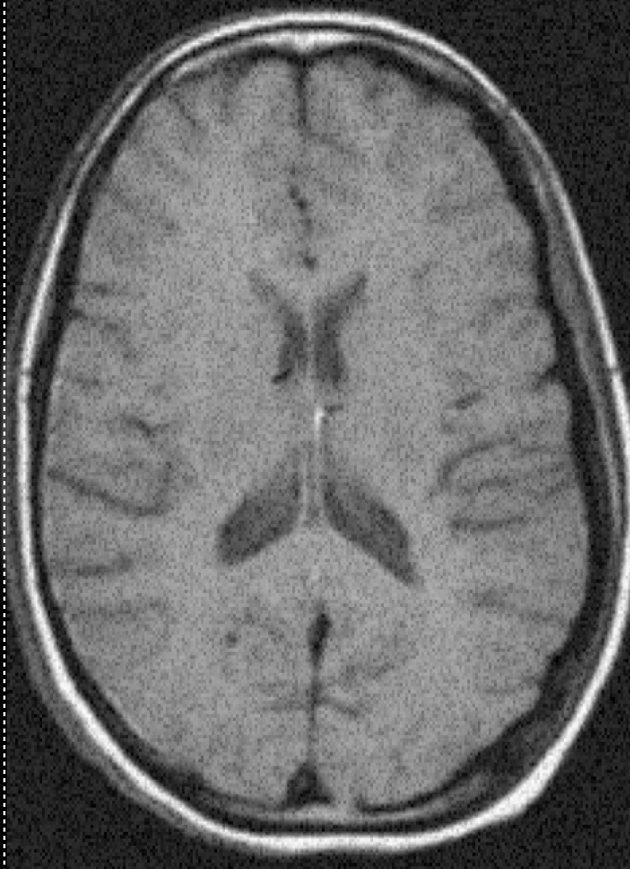


# Chemical Shift Artifact



$\text{BW} = \pm 4\text{kHz}$

**Low Bandwidth  
Large Fat-Water Shift  
High SNR**



$\text{BW} = \pm 8\text{kHz}$

**Readout** →



$\text{BW} = \pm 16\text{kHz}$

**High Bandwidth  
Small Fat-Water Shift  
Low SNR**

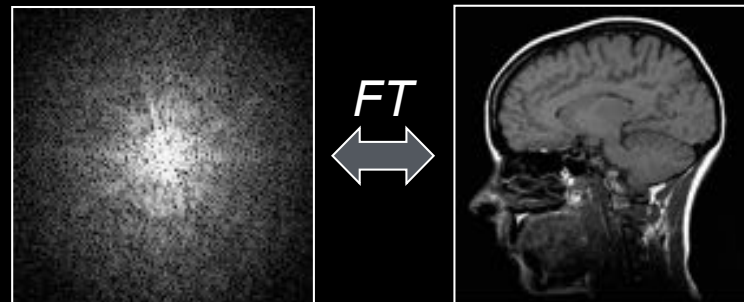
# Solution

- **High bandwidth pulse sequences**
  - **Degrades SNR (reduces acquisition time)**
  - **Reduces chemical shift artifact**
- **Fat saturation pulses/techniques**

# Motion Artifacts

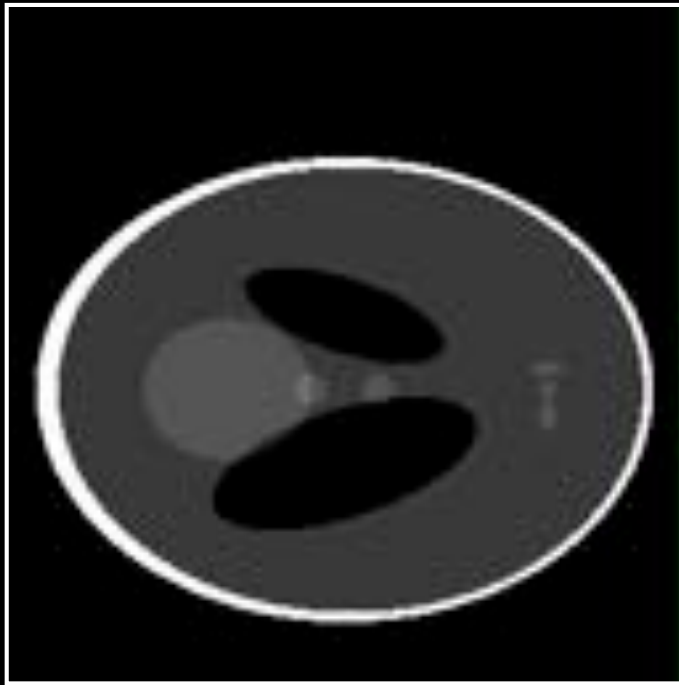
# Motion in MRI

- **Motion is responsible for a corruption in spatial localization in PE direction, resulting in blurring and/or ghosting artifacts.**
- **Typical types of motion in body**
  - Patient motion
  - Respiration
  - Cardiac motion and vascular pulsation
  - Peristalsis & bowel gas.
- **Recording signal in *k*-space not image domain!**



# Motion Artifacts - Part I

## Slow/Bulk Motion



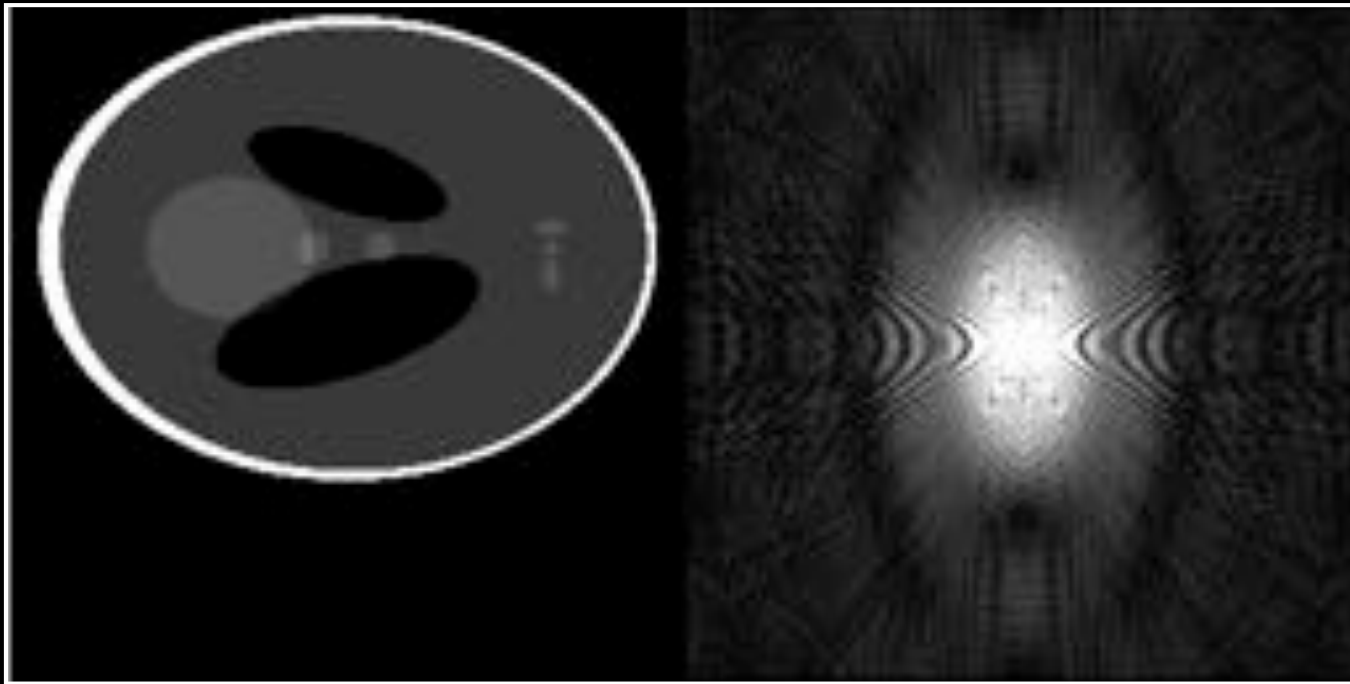
## Examples:

- Respiration
- Feet motion
- Swallowing

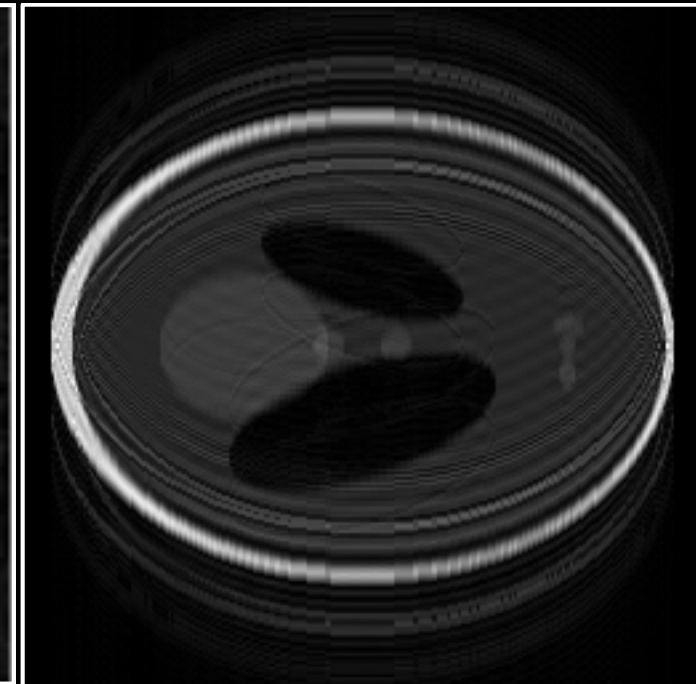


# Motion Artifacts - Part I

Slow/Bulk Motion

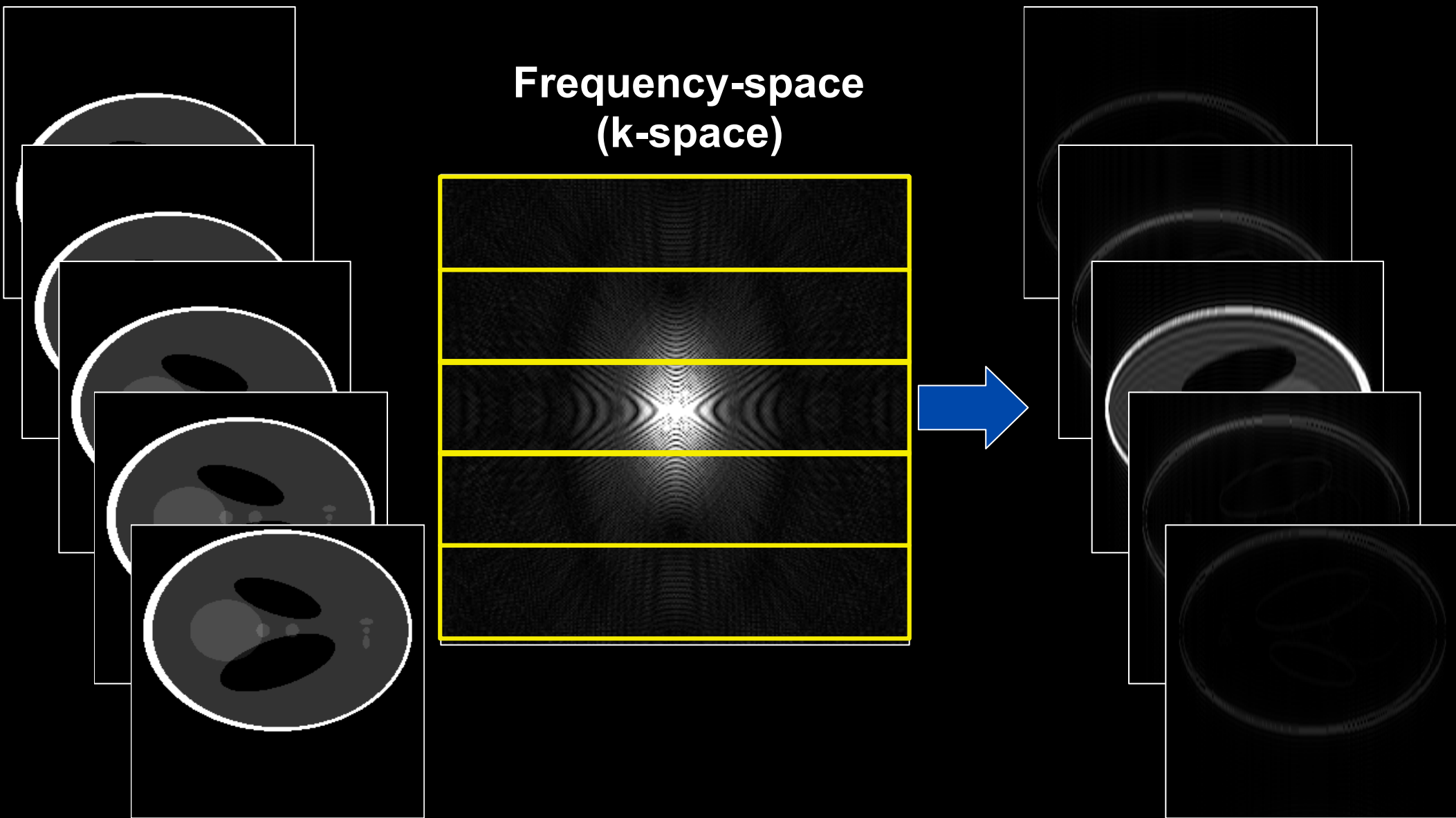


MR Image with Motion Artifacts



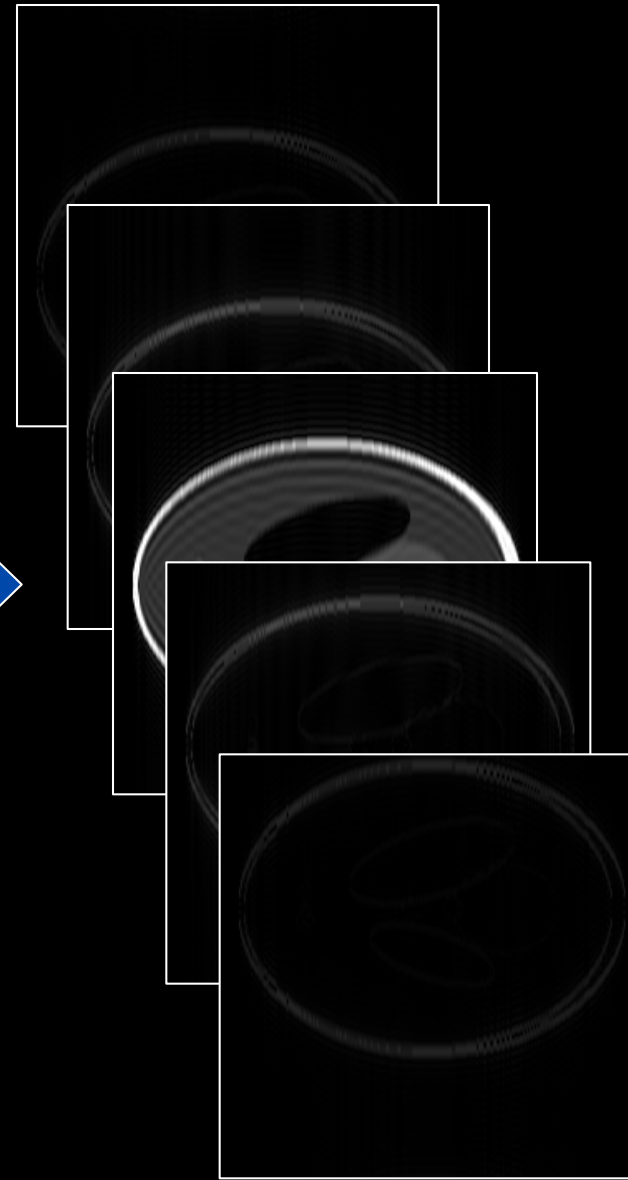
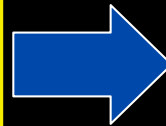
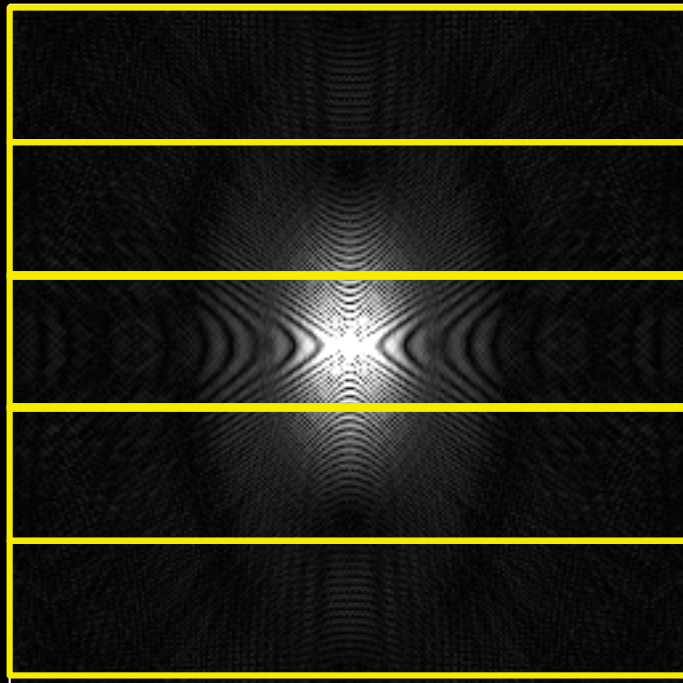
Fourier Transform

# Motion Artifacts - Part I



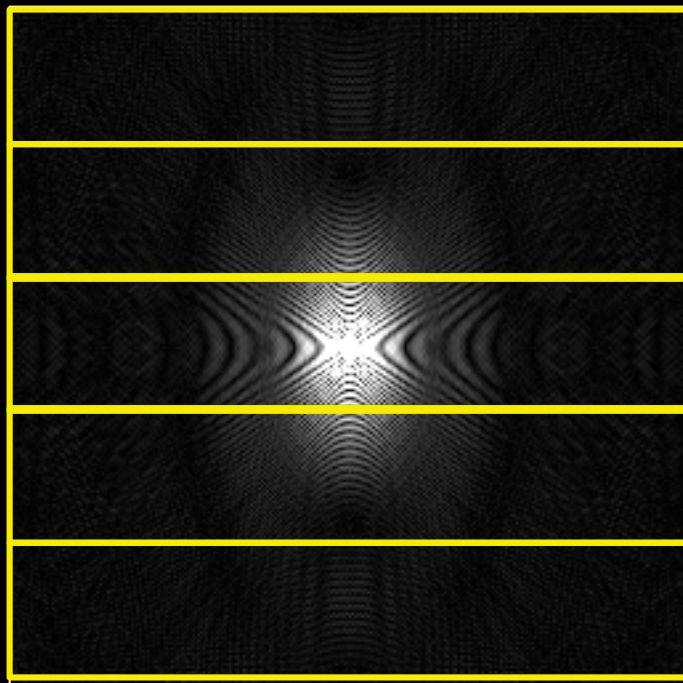
# Motion Artifacts - Part I

Frequency-space  
(k-space)

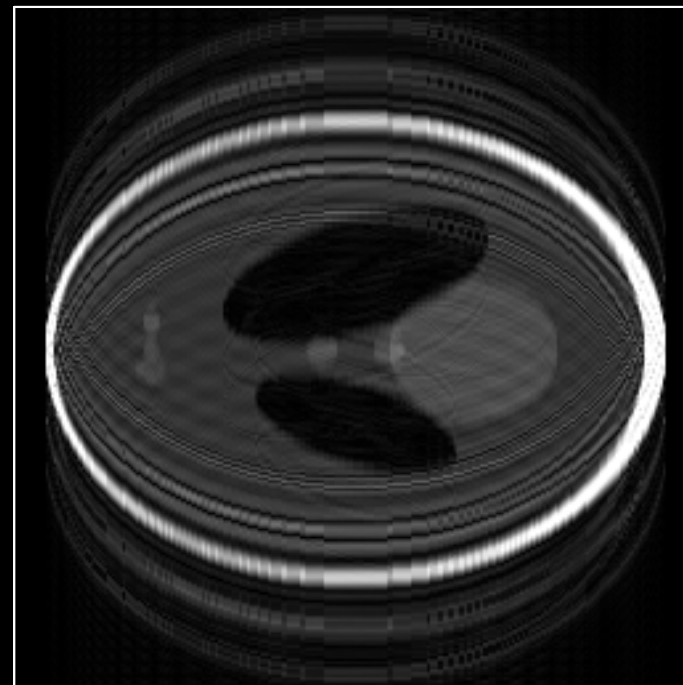


# Motion Artifacts - Part I

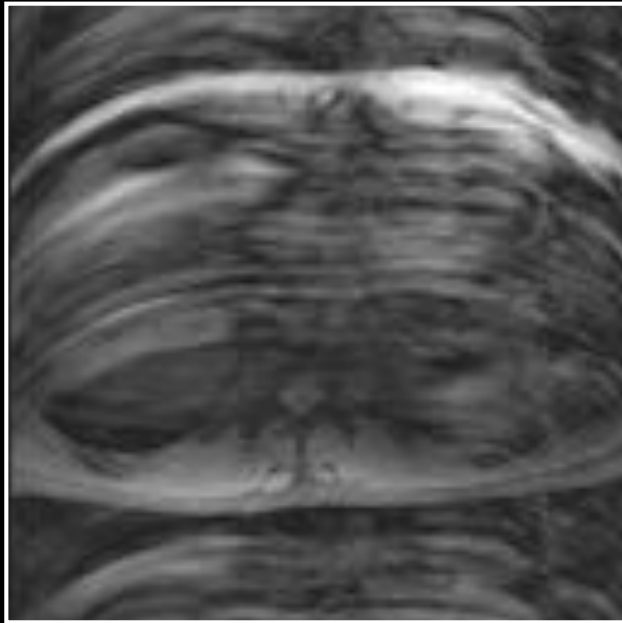
Frequency-space  
(k-space)



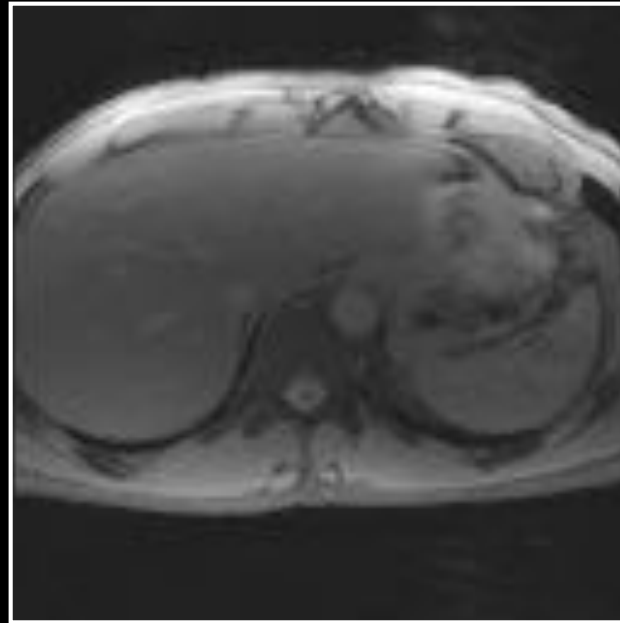
MR Image with  
Motion Artifacts



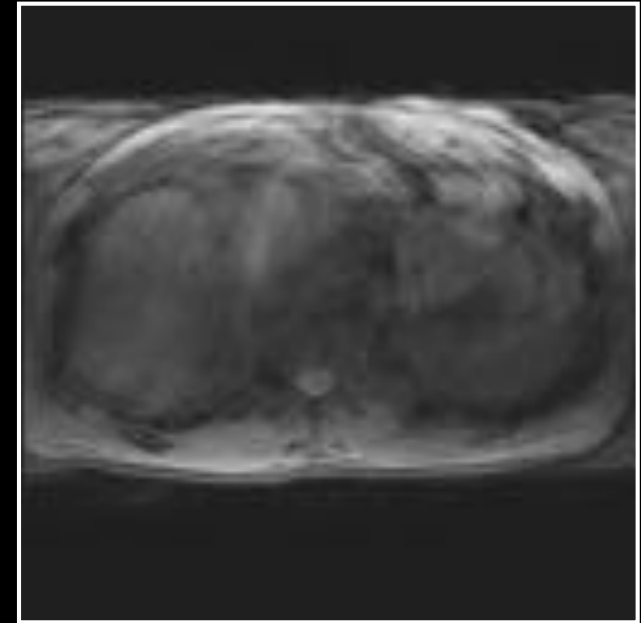
# Breathing (Motion) Artifacts



Free Breathing



Breath held



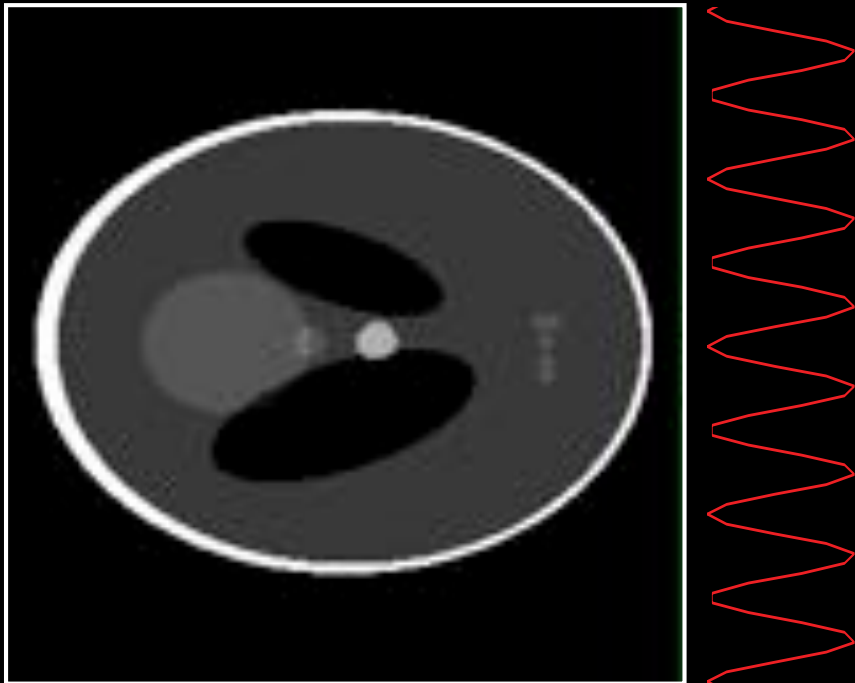
Free Breathing

# Remedies (and Penalties)

- **Possible solutions?**
  - **Breath-holding**
  - **Respiratory gating**
  - **Reduces body movements**
    - **Patient coaching, physical restraint, sedation**
- **Disadvantages**
  - **Requires fast sequences**
  - **Increases the scan time; restricts the available TRs**
  - **Patients acceptance and discomfort**

# Motion Artifacts - Part II

## Periodic Motion



## Examples:

- Aortic Pulsation
- Arterial Pulsation

# Motion Artifacts - Part II

Periodic Motion

MR Image with  
Motion Artifacts

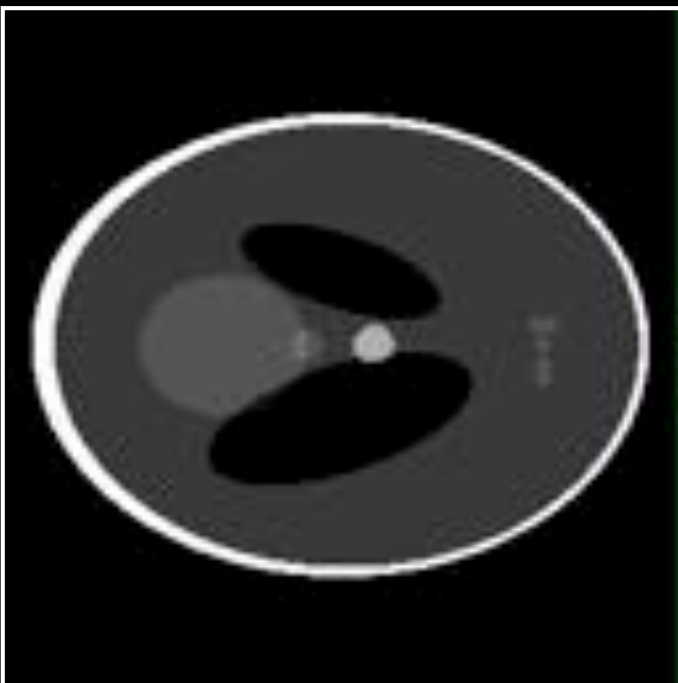


Fourier  
Transform

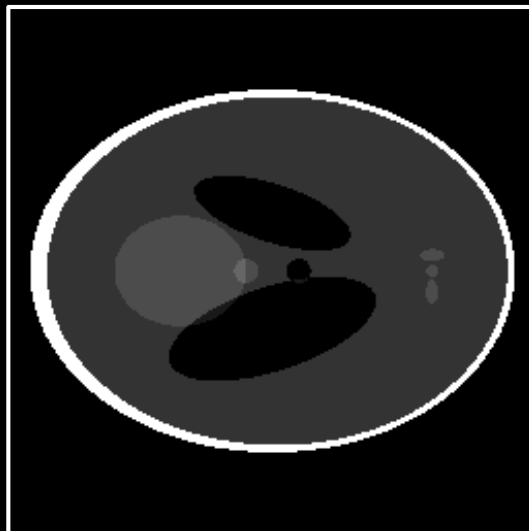


# Motion Artifacts - Part II

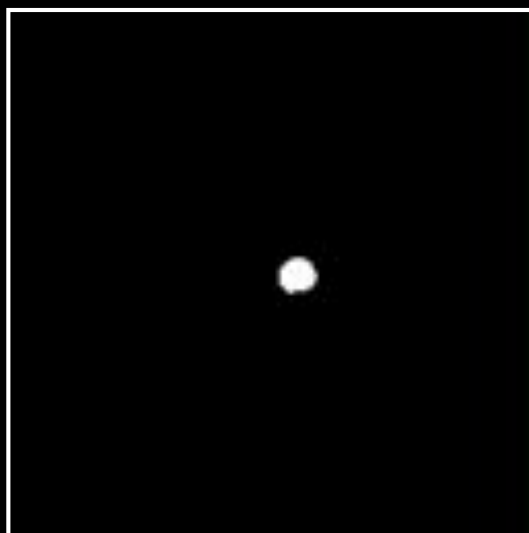
Periodic Motion



Static Part

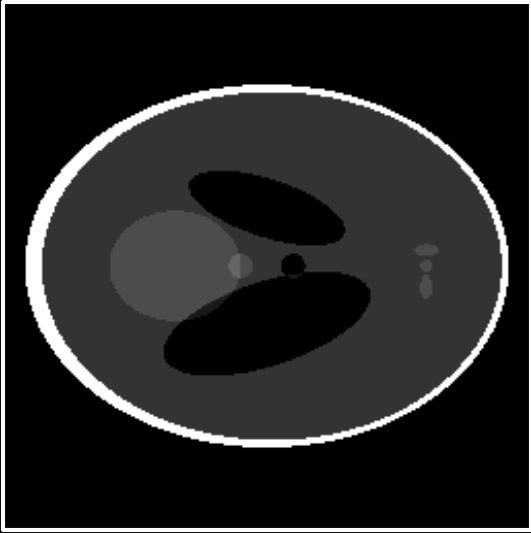


Moving Part

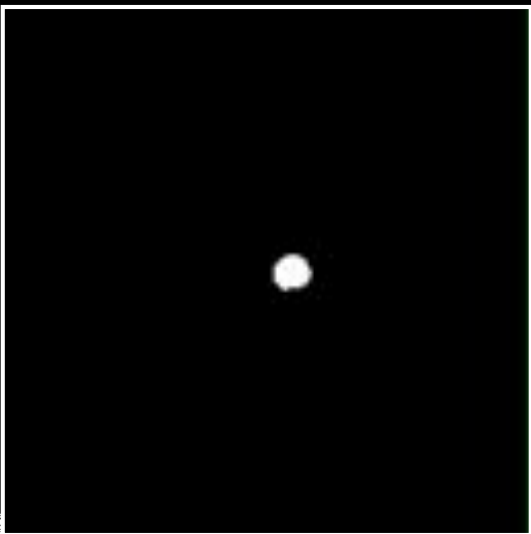


# Motion Artifacts - Part II

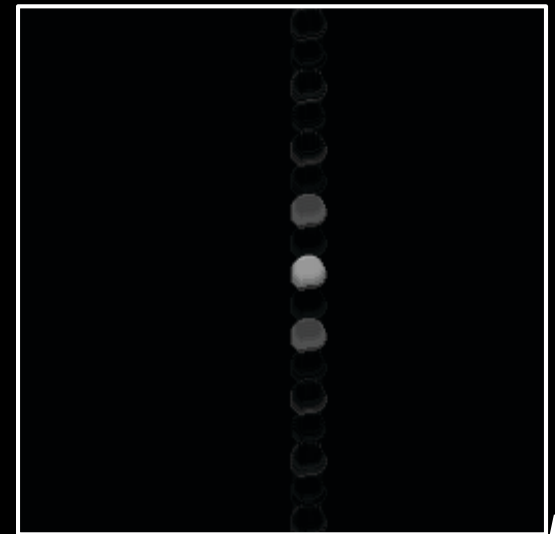
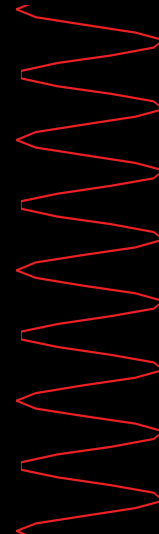
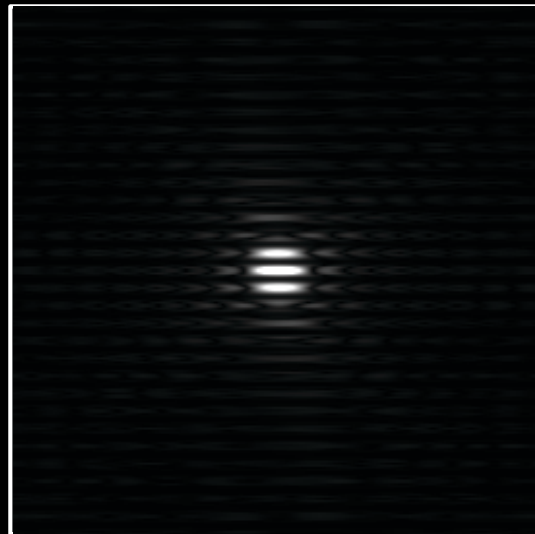
Static Part



Moving Part

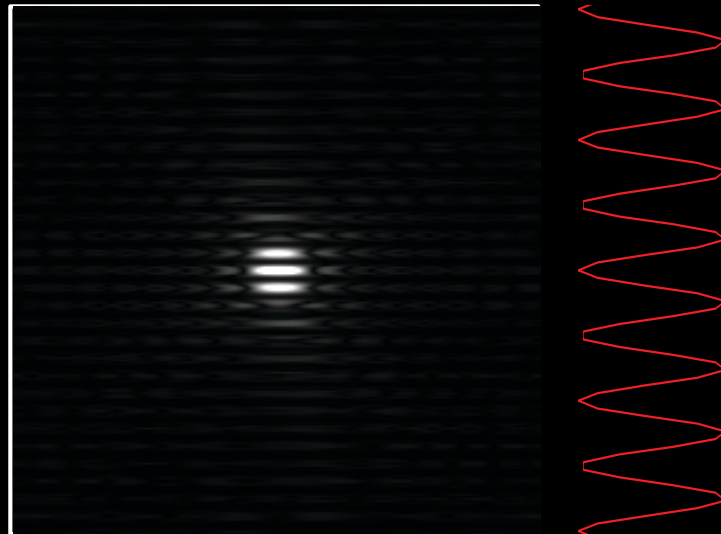
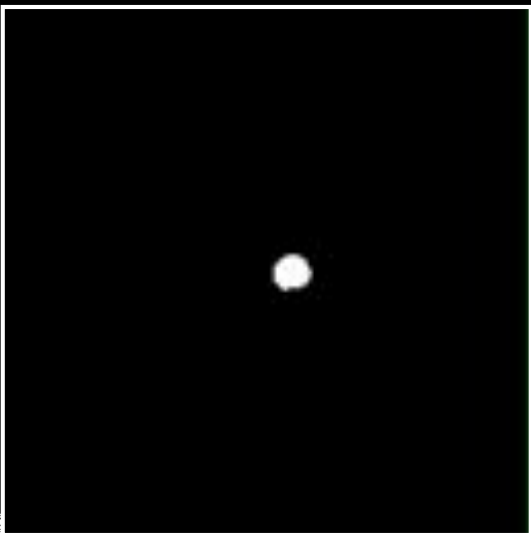


Fourier Transform

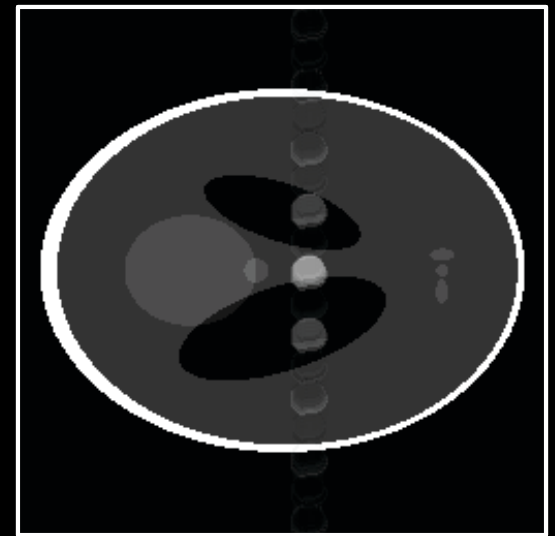


# Motion Artifacts - Part II

Moving Part

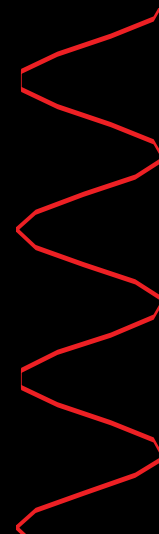
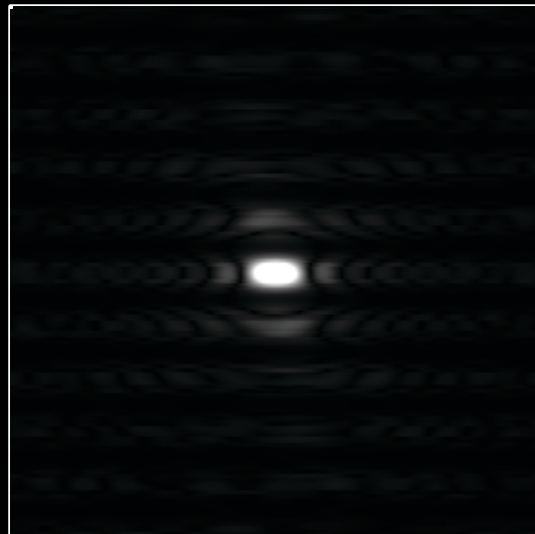
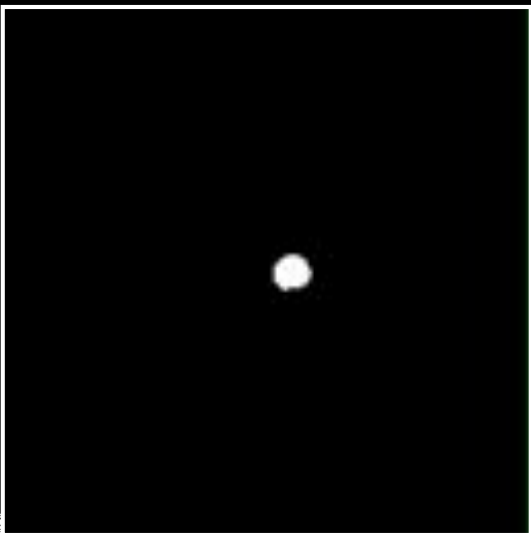


MR Image with Ghosting Artifacts

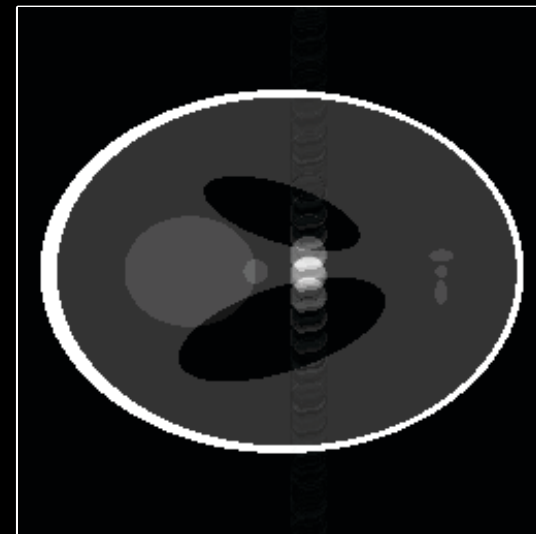


# Motion Artifacts - Part II

Moving Part



MR Image with Ghosting Artifacts



# Remedies (and Penalties)

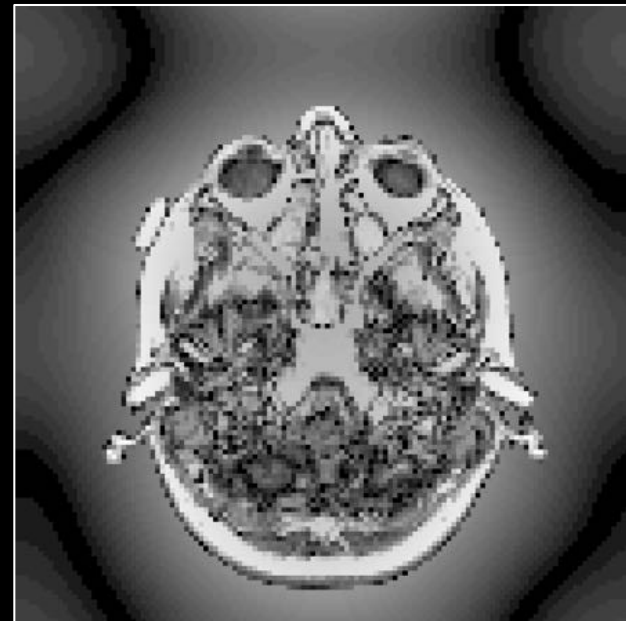
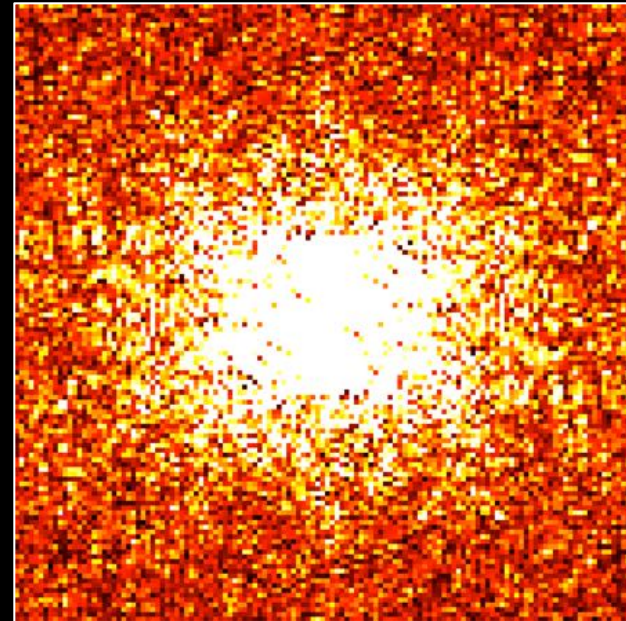
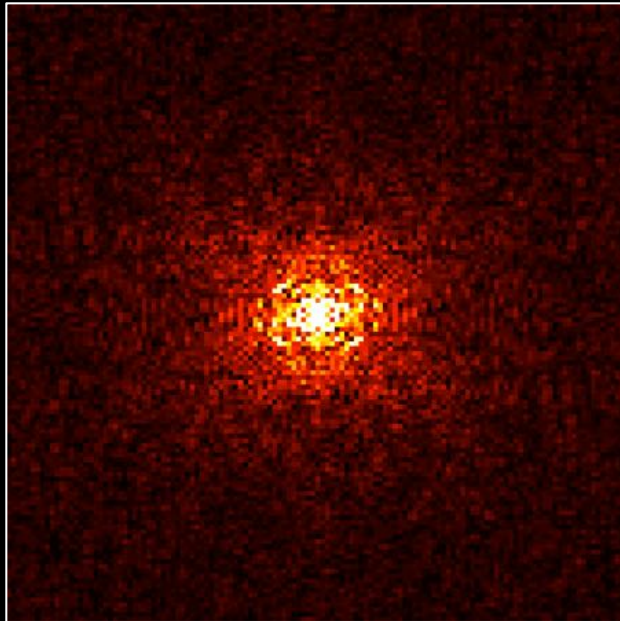
- **Possible solutions?**
  - Cardiac gating  $\pm$  segmented imaging.
  - Signal suppression of moving tissues.
  - Swapping phase-encoding and frequency encoding directions
- **Disadvantages**
  - Increases scan time.
  - Increases TR (due to preparation pulses).
  - Only shifts the artifacts.

# Data Clipping

# Data Clipping

- **Received signal saturates the receiver.**
- **Peak signal usually in the middle of  $k$ -space, therefore lose low spatial frequency information:**
  - **Contrast**
  - **Intensity**
- **Pre-scan procedure usually avoids data clipping by adjusting receiver gains.**

# Data Clipping





# Radio Frequency Interference

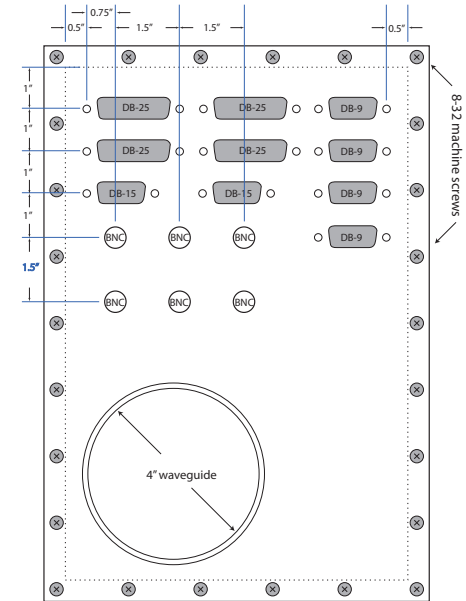
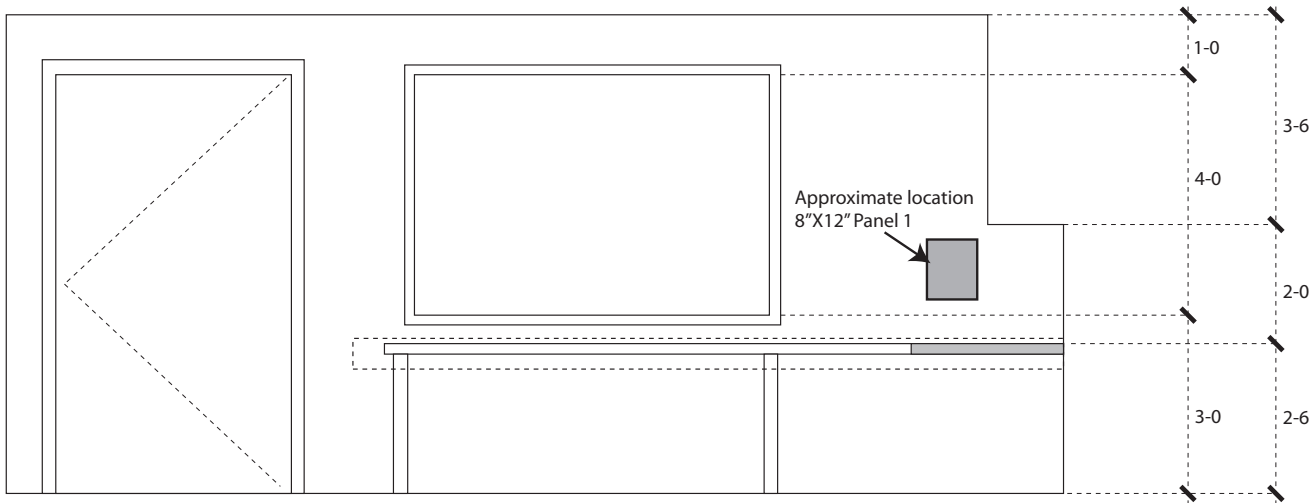
# RF Shielding

- **RF fields are close to FM radio**
  - $^1\text{H}$  @ 1.5T  $\Rightarrow$  63.85 MHz
  - $^1\text{H}$  @ 3.0T  $\Rightarrow$  127.71 MHz
  - KROQ  $\Rightarrow$  106.7 MHz
- **Need to shield local sources from interfering**
- **Copper room shielding required**

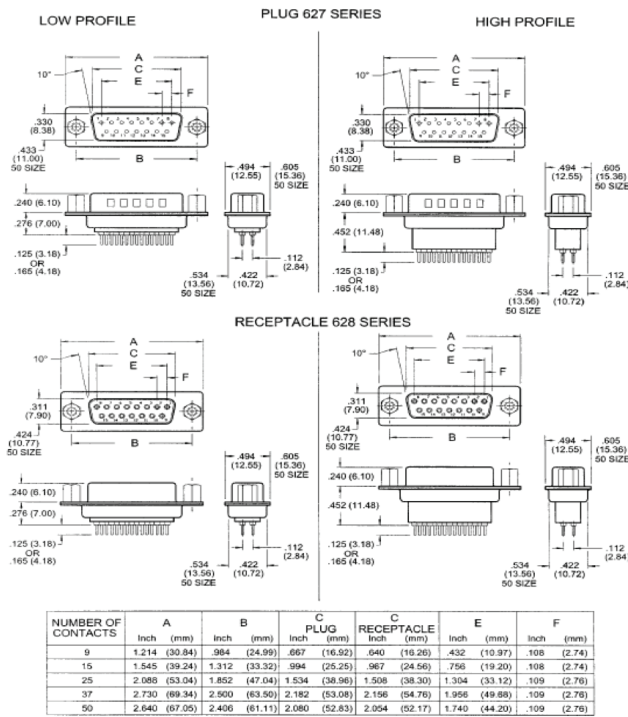


Penetration Panel

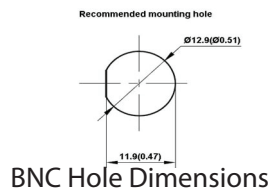
# Penetration Panel



Panel 1 - between scan room and console room  
8" X 12" penetration (panel size is 9" X 13")

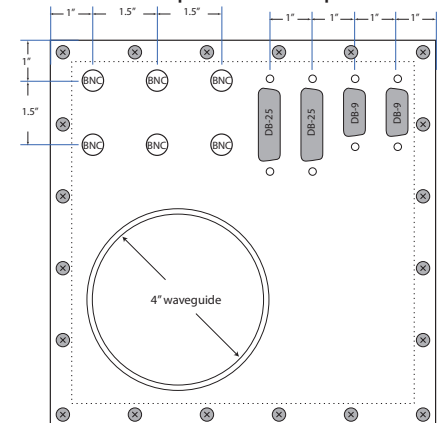


DB cutout dimensions



Penetration panels should be made from 16 ga. steel or aluminum

Location of Panel 2 is to be in the proximity of the Siemens penetration panel.



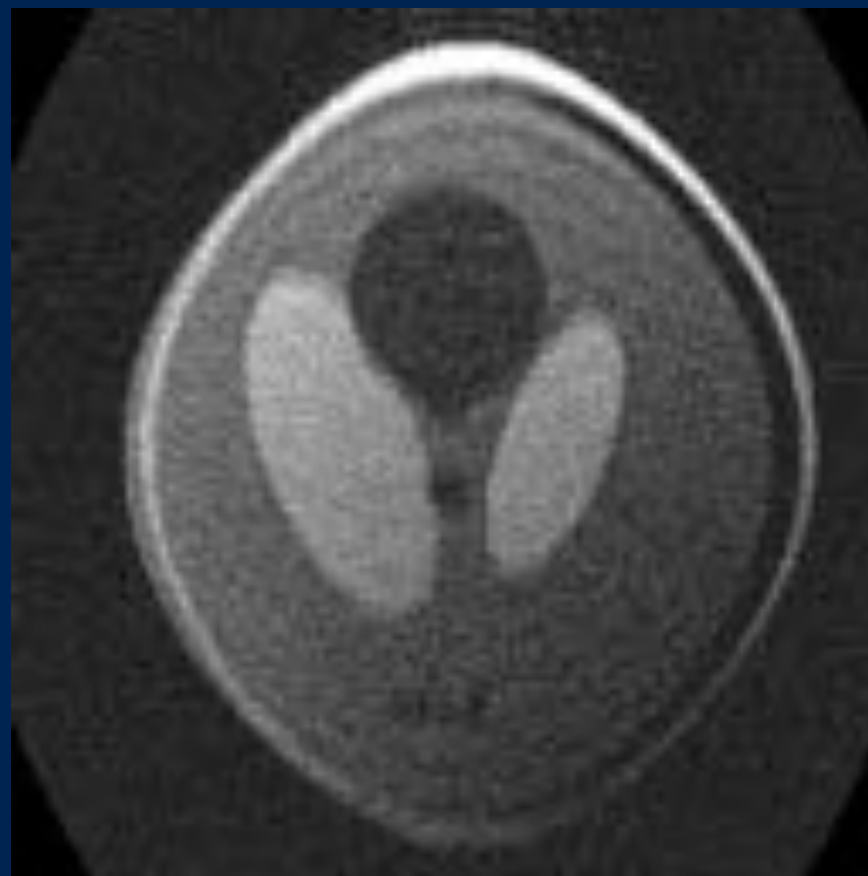
8" Penetration (panel size is 9")  
Panel 2 - between equipment room and scan room

# Radiofrequency Interference

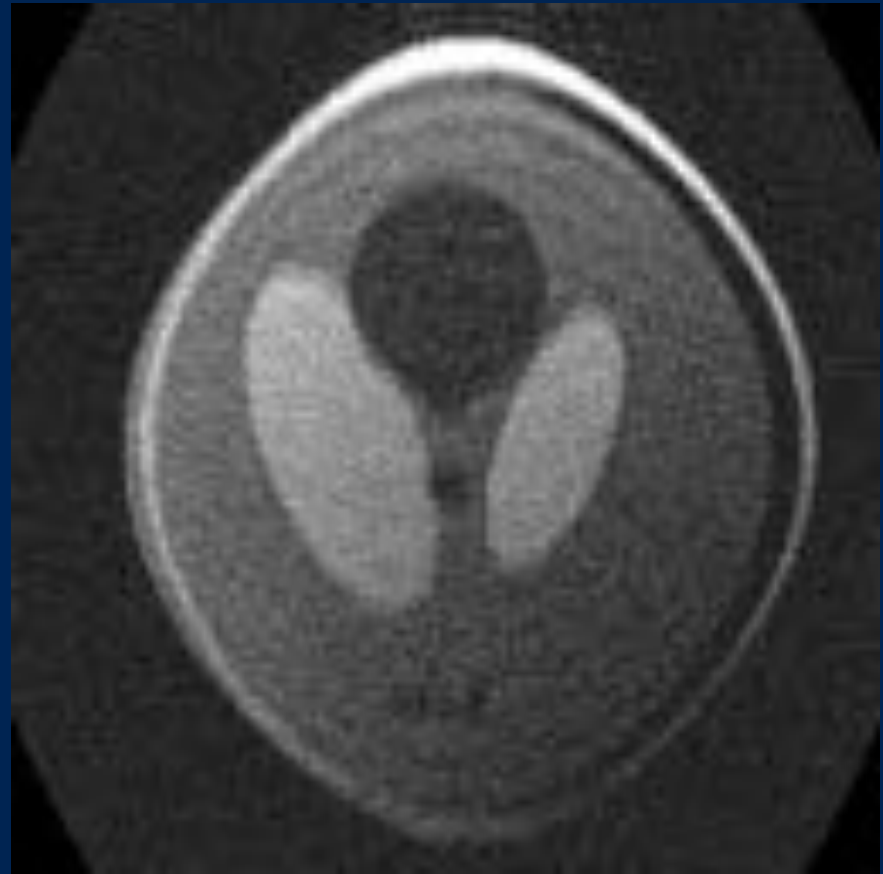
- **Caused by RF leak**
  - Scanner Door is Open
  - Wires running in/out of scan room
  - Faulty Room Shielding



# How many artifacts can you see?



# How many artifacts can you see?



**Noise**  
**Gradient Distortion**  
**Gibb's Ringing**  
**Chemical Shift**  
**Coil shading**

# Thanks



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