

# Perfusion Imaging: Dynamic Contrast-Enhanced MRI



David Geffen  
School of Medicine

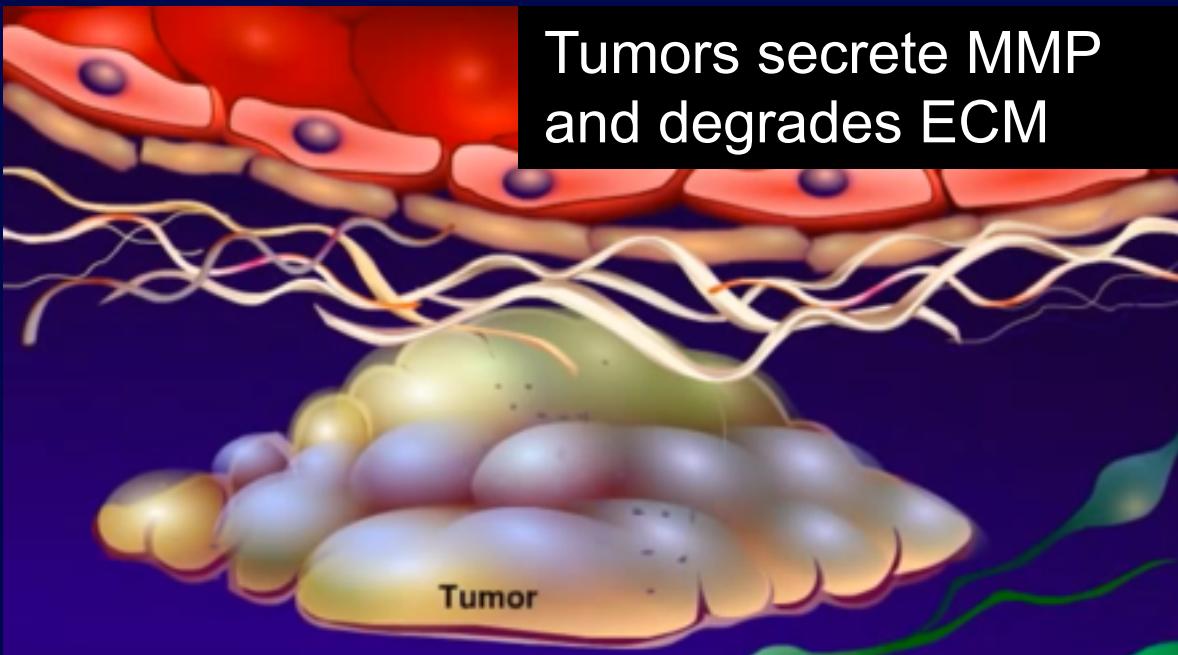


Kyung Sung, PhD

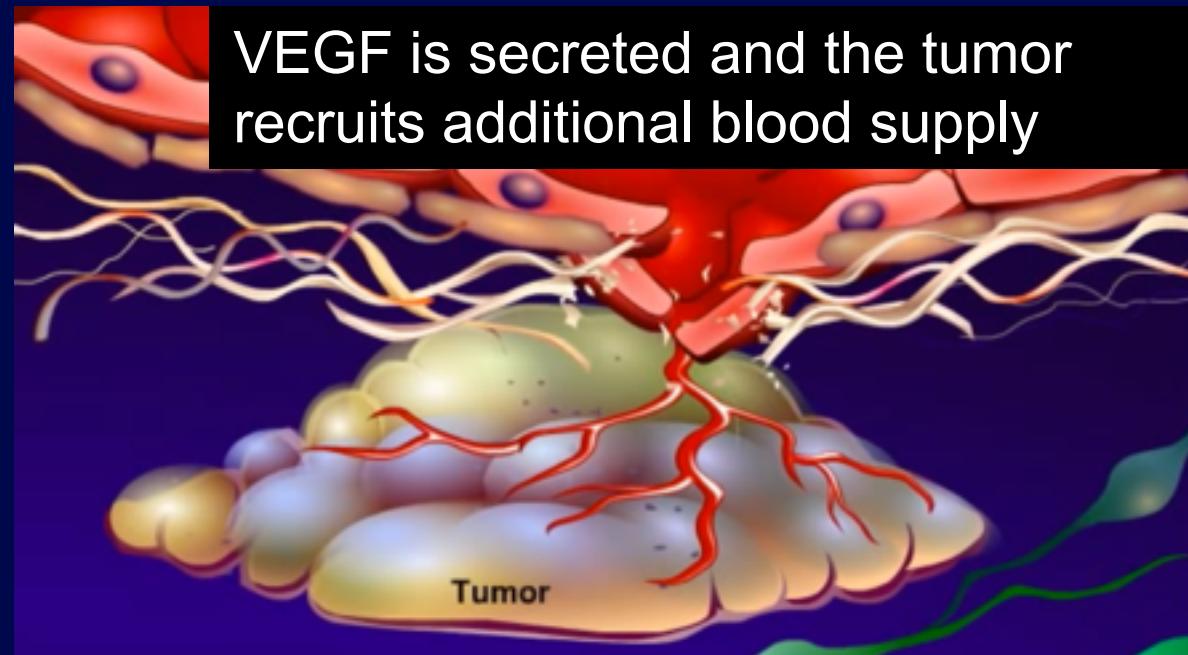
3/9/2017

Department of Radiological Sciences  
David Geffen School of Medicine  
University of California, Los Angeles

# Tumor Angiogenesis



Tumors secrete MMP  
and degrades ECM



VEGF is secreted and the tumor  
recruits additional blood supply

- Cancer cannot grow beyond a certain size without developing a vascular network to provide additional nutrients and oxygen for growth (angiogenesis)
- Recruited tumor vasculature is different from normal vasculature, measurable with contrast-enhanced MRI

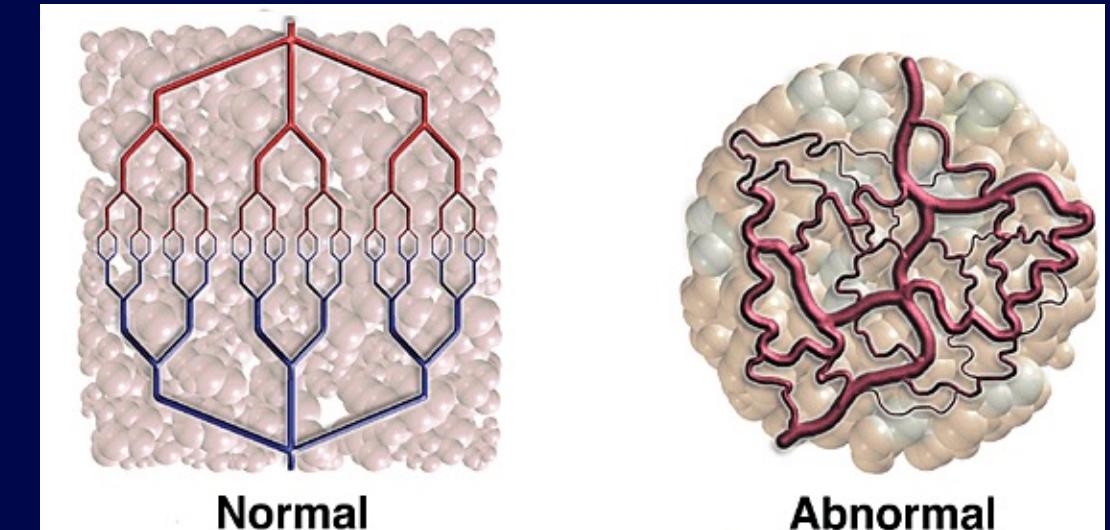


David Geffen  
School of Medicine

**UCLA**  
Radiology

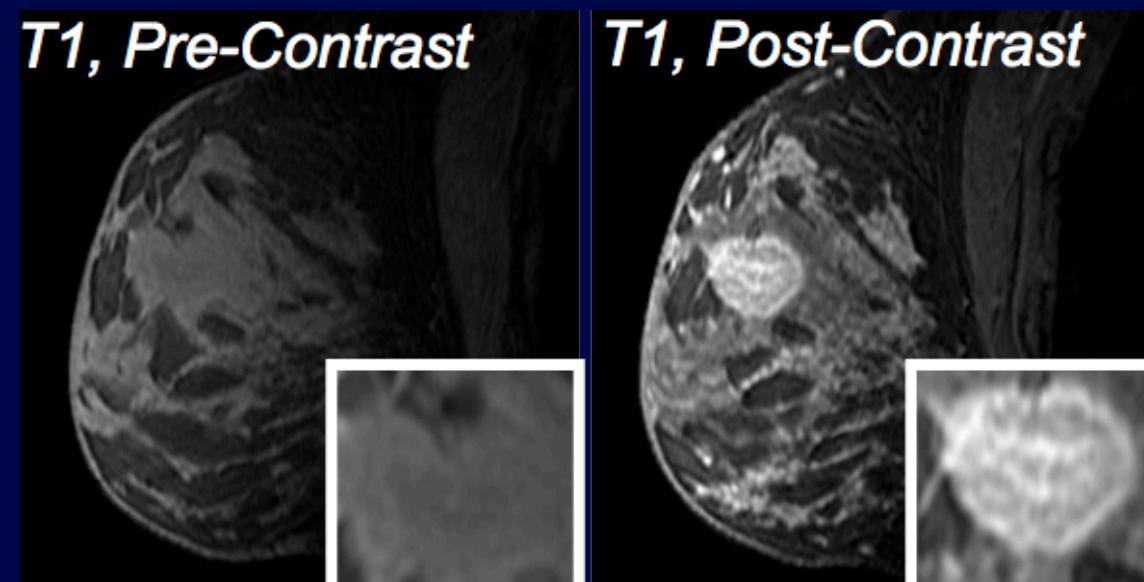
# Tumor Vasculation and Enhancement

- Cancer has many traits different from surrounding tissue:
  - Unchecked cell proliferation
  - Cannot grow beyond a certain size without developing a vascular network



*Jain R, Nat. Medicine 2001*

- MRI has great potential to detect cancer and vascular abnormalities

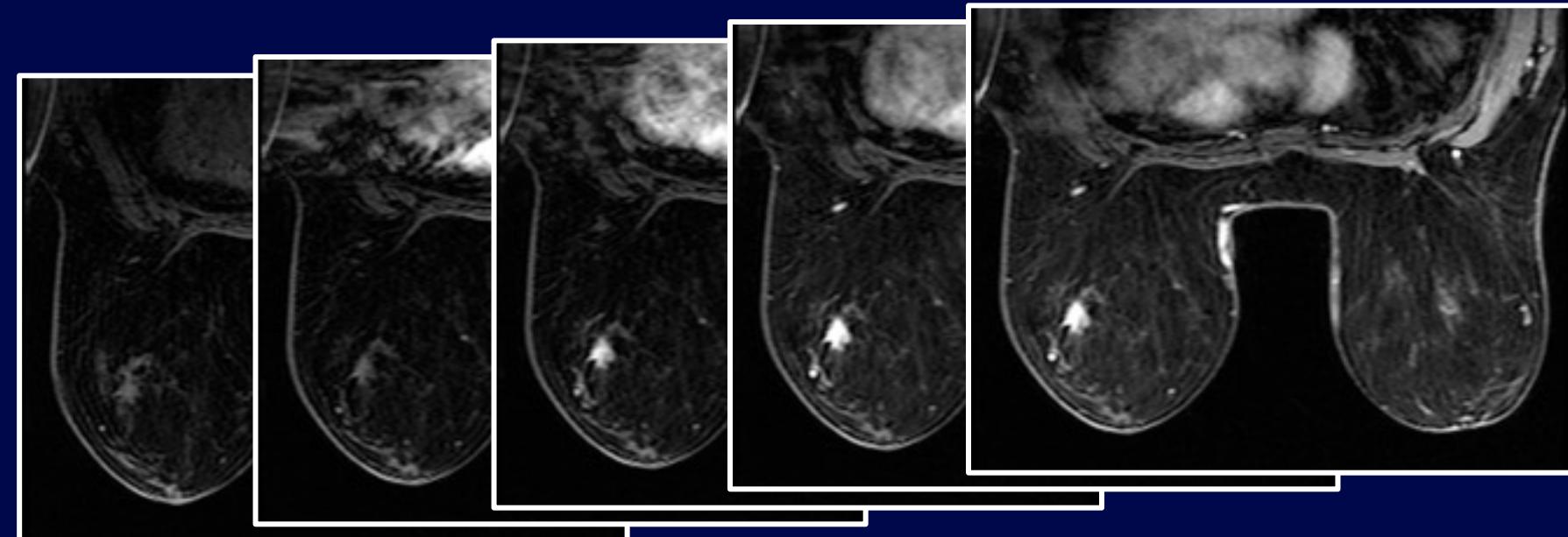


David Geffen  
School of Medicine

**UCLA**  
Radiology

# Contrast Enhanced MRI

- One post-contrast image
- Pre- and post-contrast image
- “Slow” dynamic acquisition (~ minutes)
- “Fast” dynamic acquisition (~ seconds)

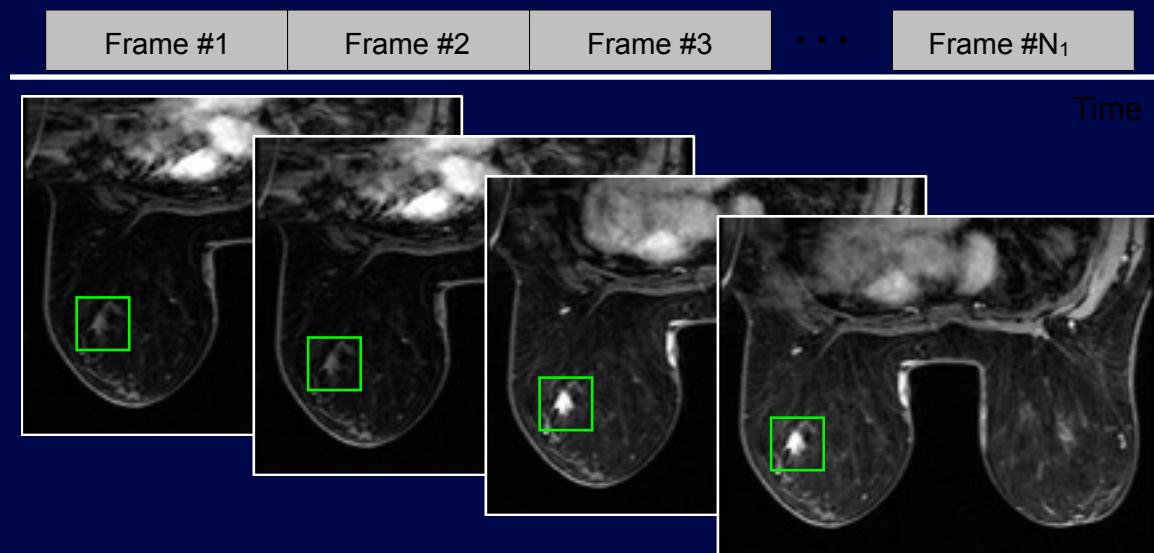


David Geffen  
School of Medicine

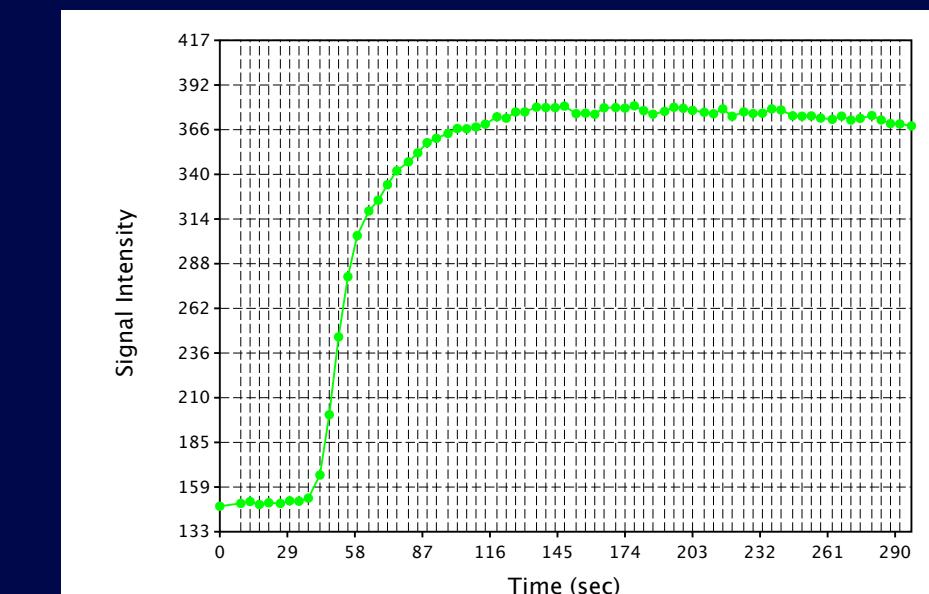
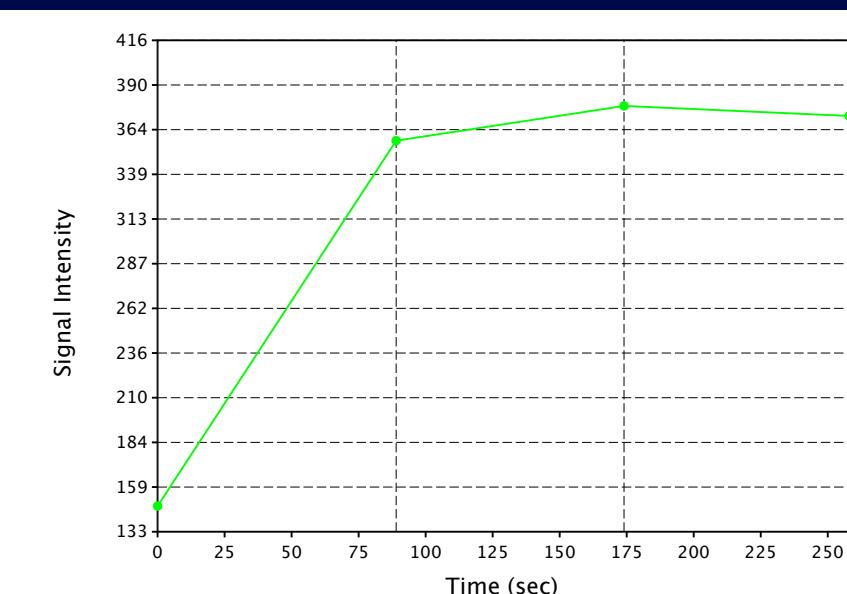
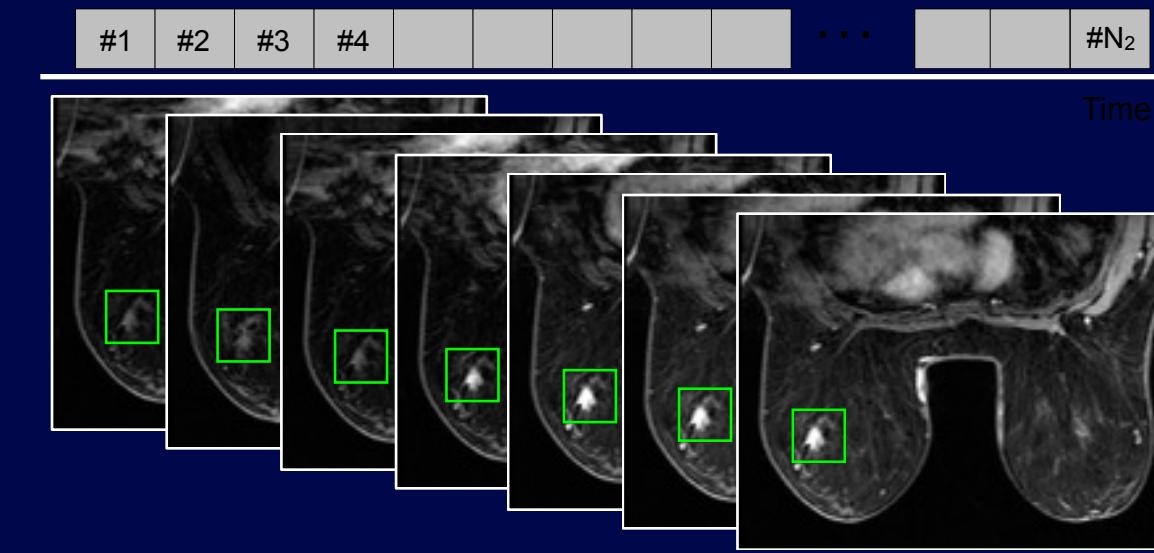
**UCLA**  
Radiology

# Dynamic Contrast-Enhanced (DCE) MRI

Conventional DCE-MRI



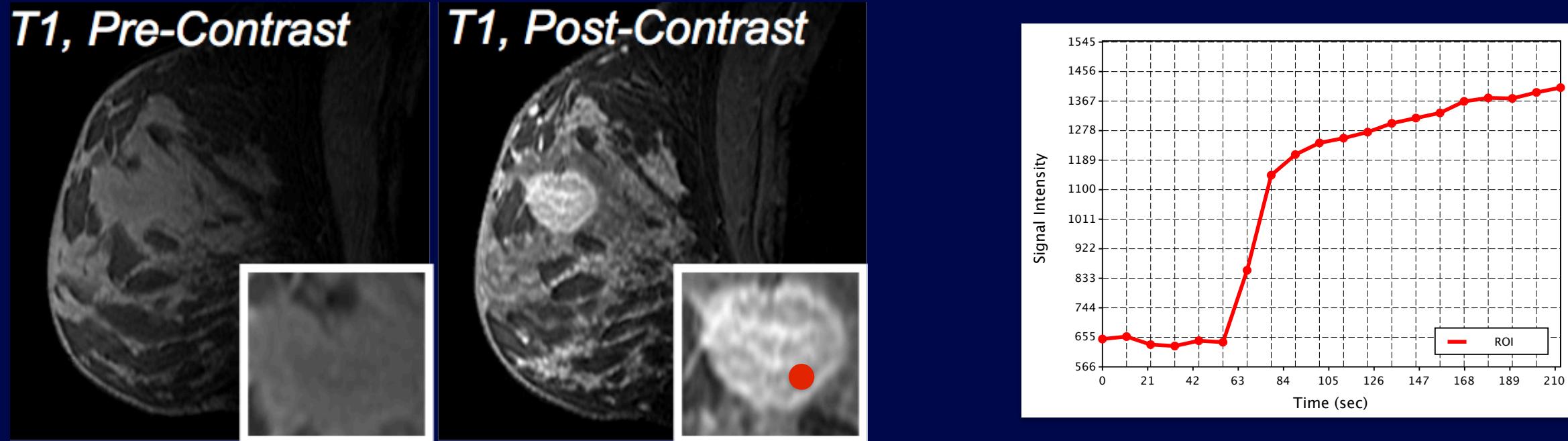
High Frame-Rate DCE-MRI



David Geffen  
School of Medicine

**UCLA**  
Radiology

# DCE-MRI: Temporal Resolution



- High spatial and temporal resolution is desirable for DCE-MRI applications, especially for better quantitative analysis
- Many k-space data sharing schemes (e.g., TWIST and DISCO) become popular

*Madhuranthakam AJ, et al. MRM 2006  
Herrmann KH, et al. JMRI 2011*

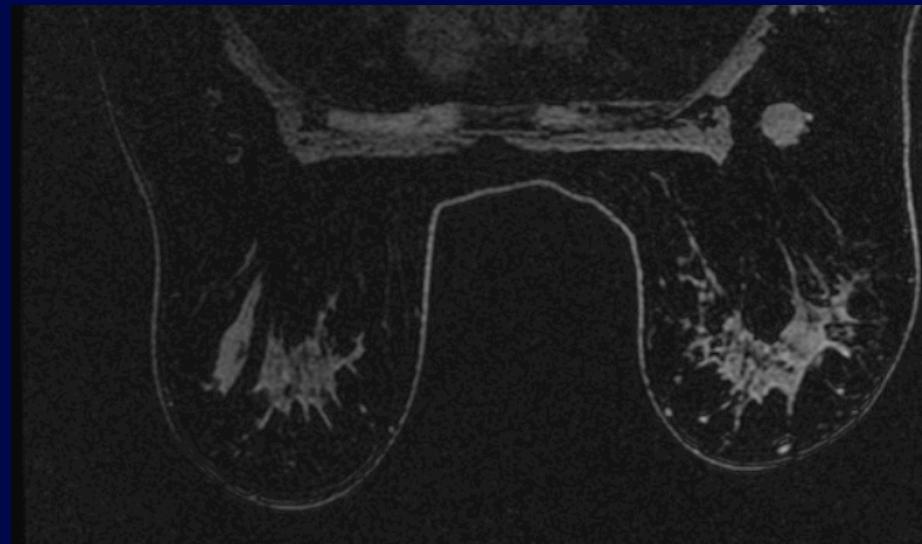


David Geffen  
School of Medicine

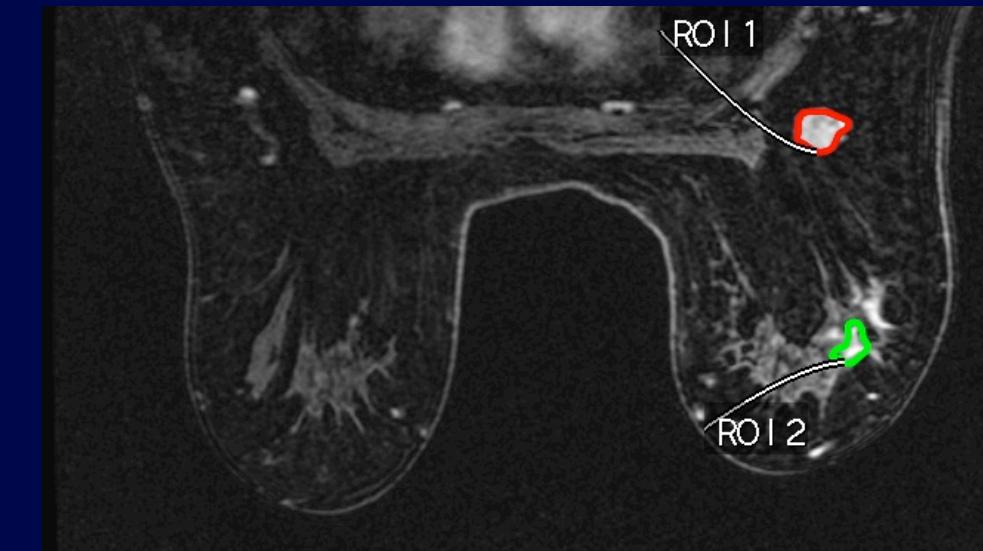
**UCLA**  
Radiology

# Dynamic Contrast Enhanced (DCE) MRI

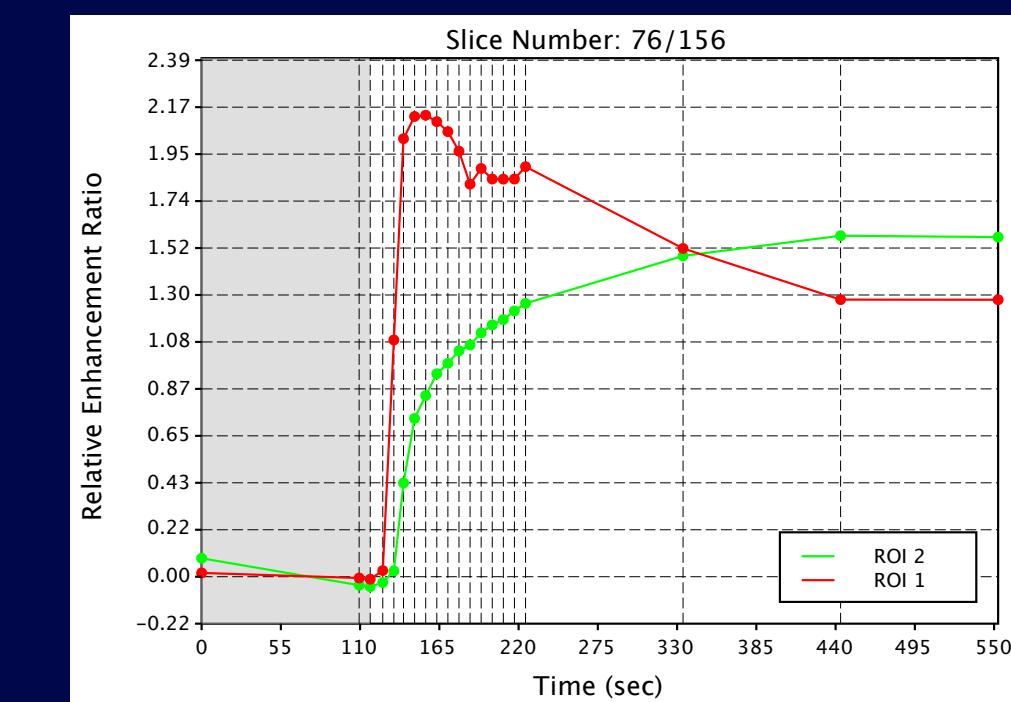
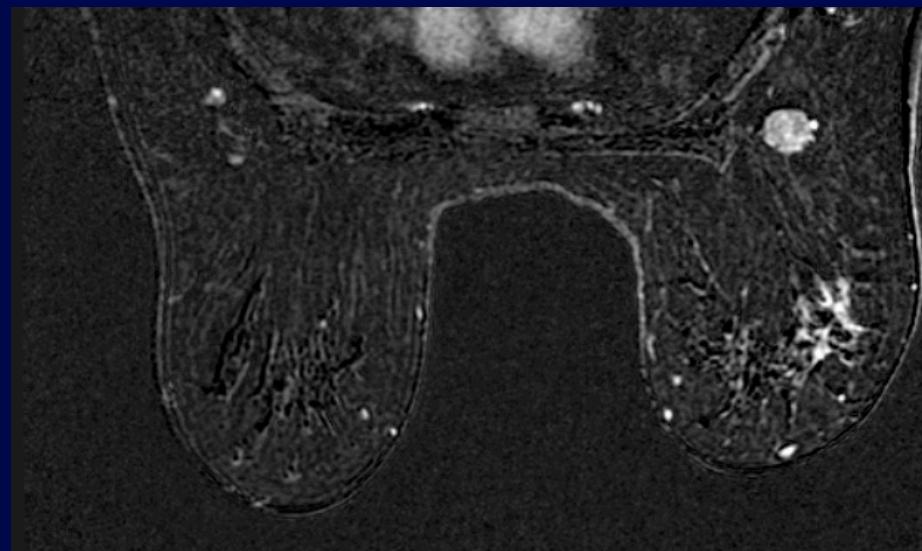
Pre-contrast



Peak-contrast



Subtraction

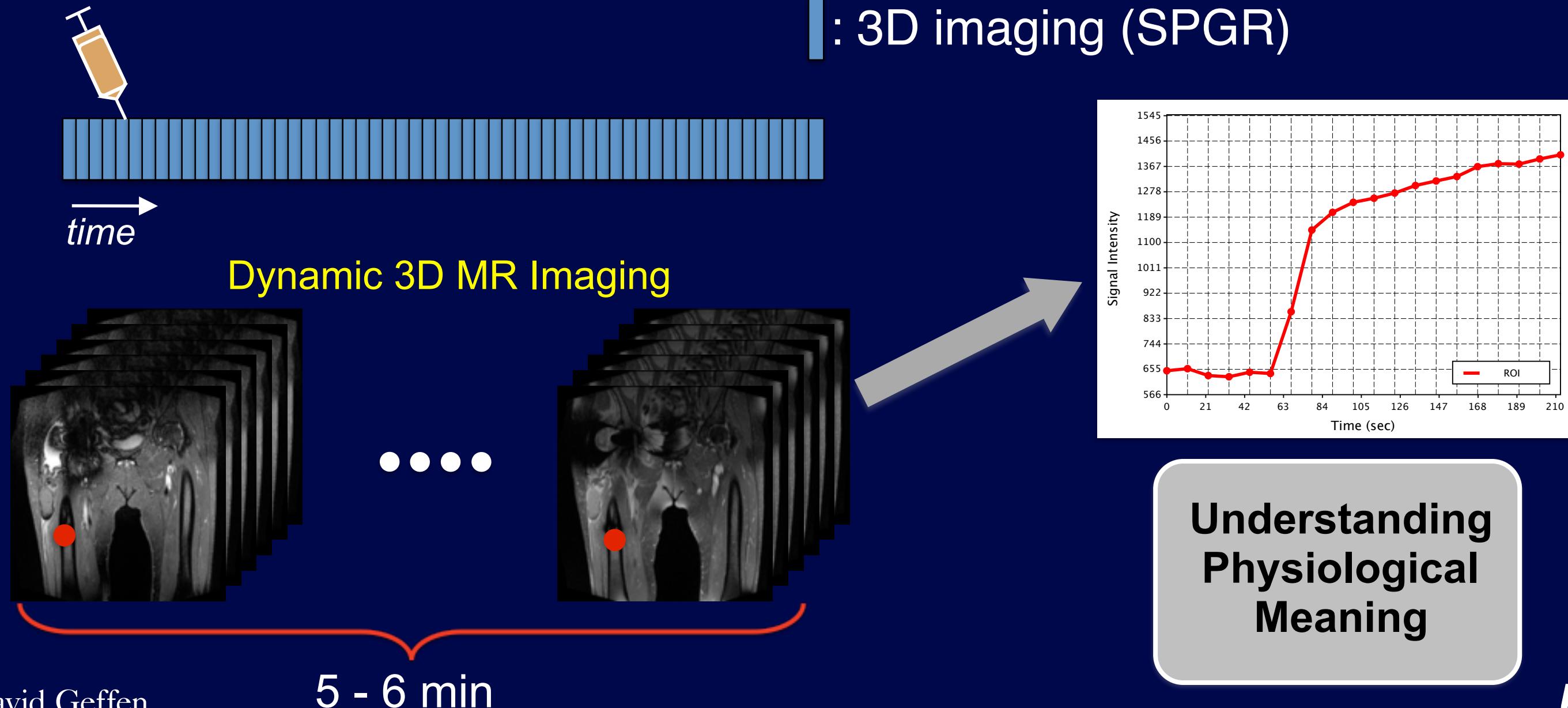


David Geffen  
School of Medicine

**UCLA**  
Radiology

# T1-weighted DCE-MRI

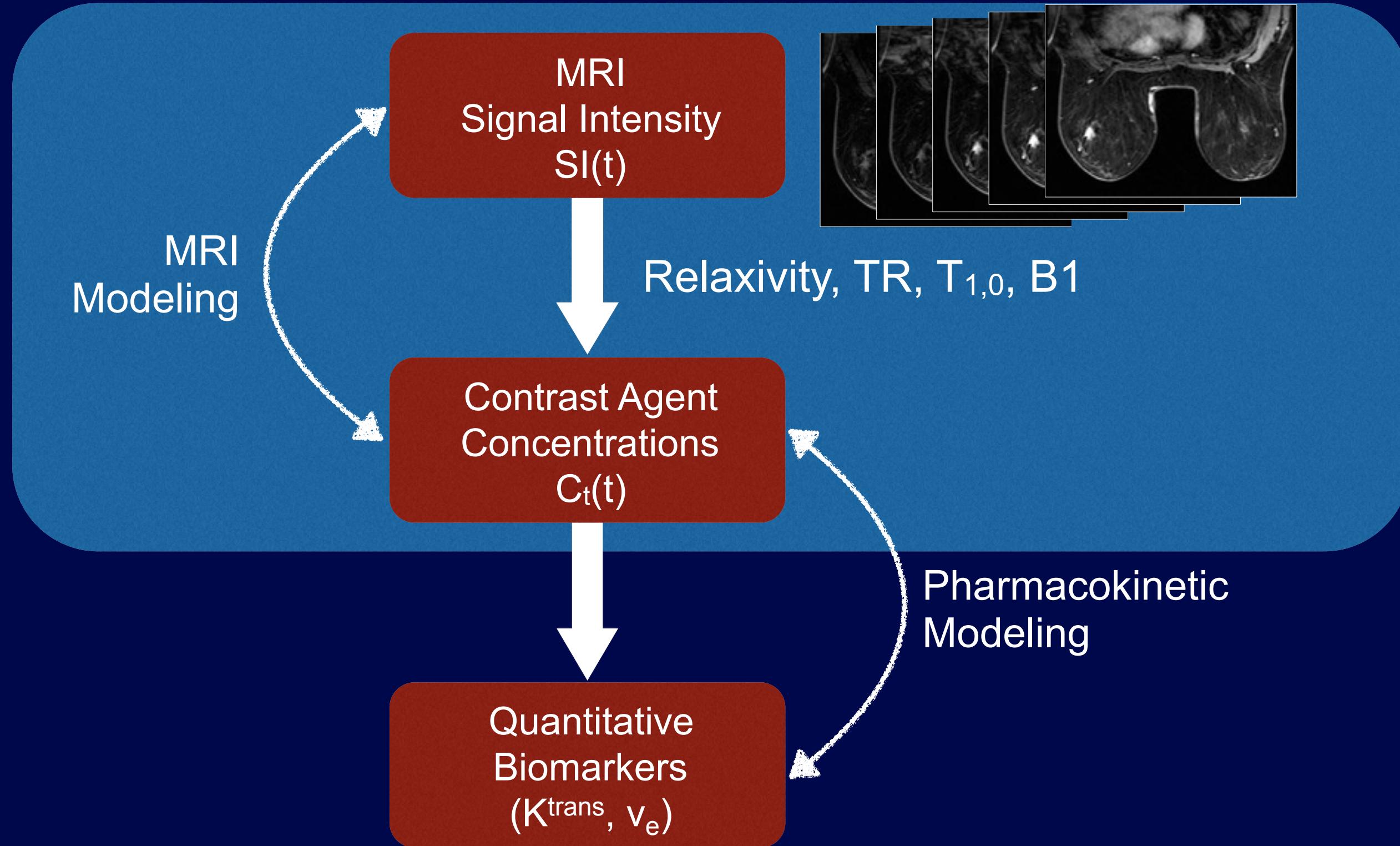
- DCE-MRI continuously monitors enhancement of tissue before and after injection of contrast agent



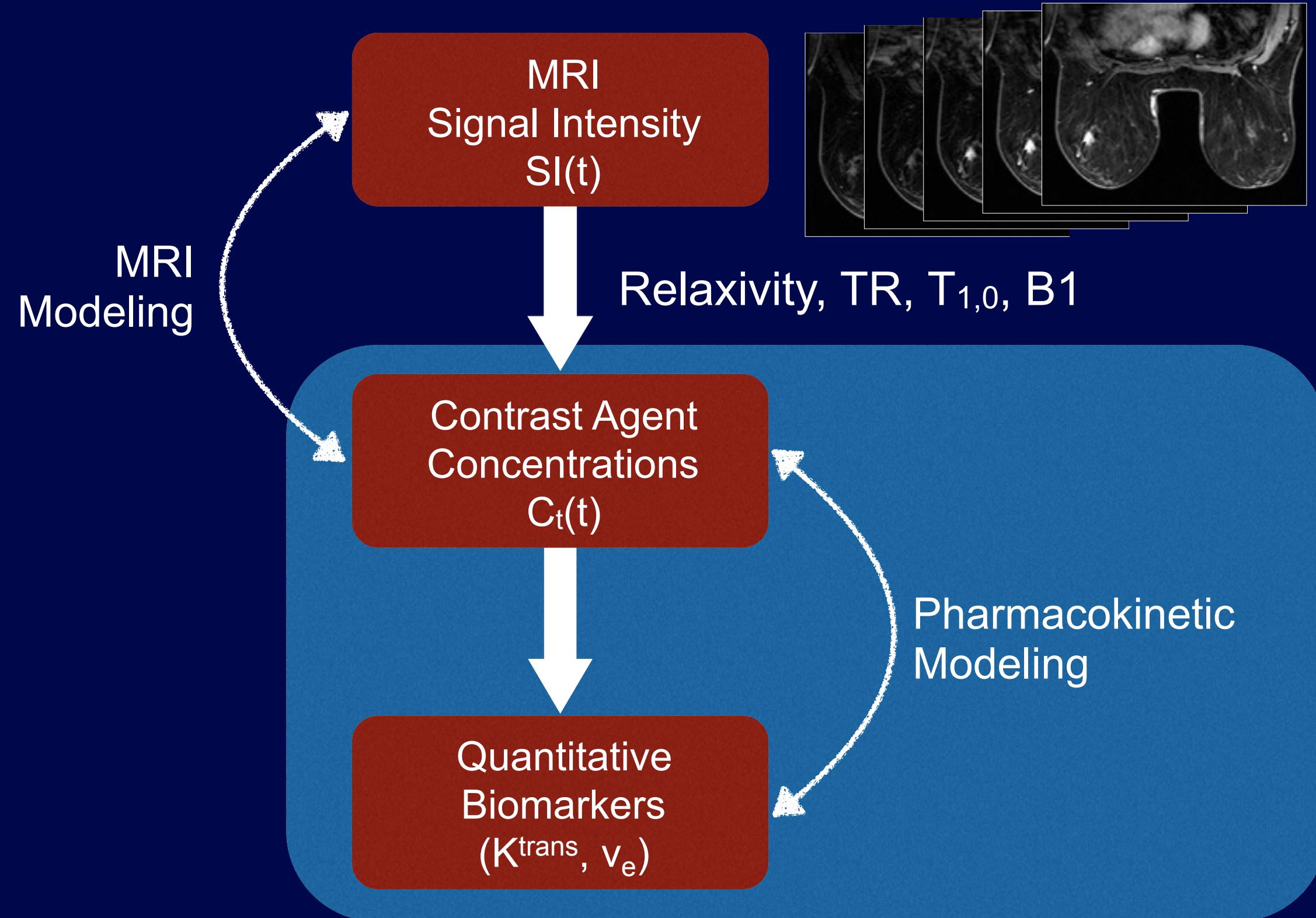
David Geffen  
School of Medicine

**UCLA**  
Radiology

# Quantitative DCE-MRI



# Quantitative DCE-MRI



# Outline of Topics

---

- Conversion from MR signal to concentration
  - T1 measurements
  - B1 inhomogeneity
- Conversion from concentration to quantitative biomarkers (pharmacokinetic modeling)
  - Standard Tofts (two-compartment) model
  - Arterial input function
  - Dispersion modeling
- DCE-MRI data analysis (post-processing option)



# MRI Modeling: MR Signal → Concentration

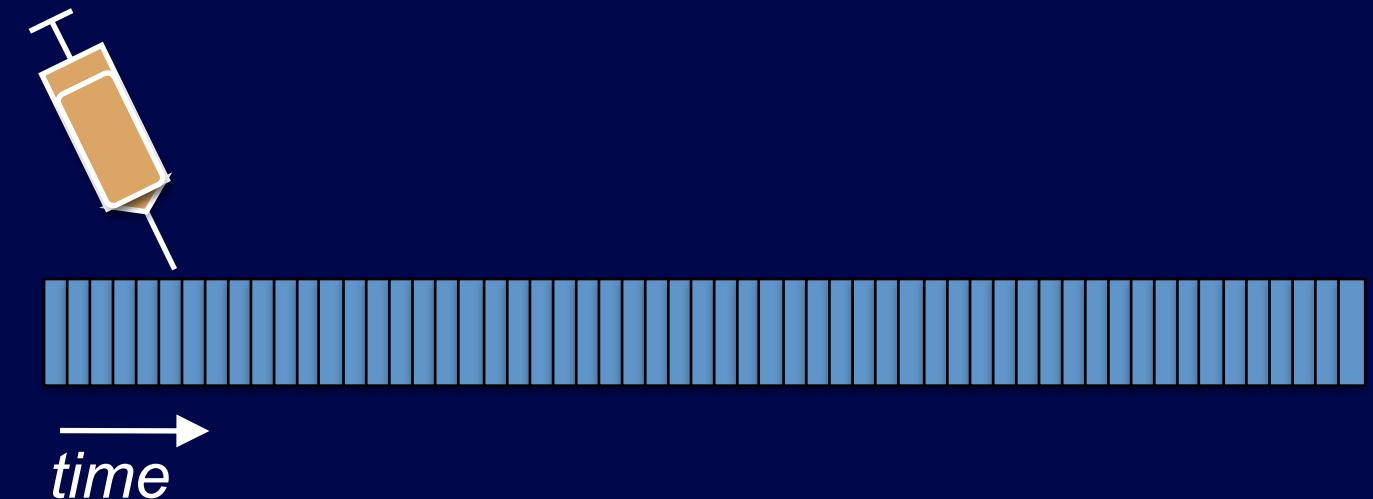
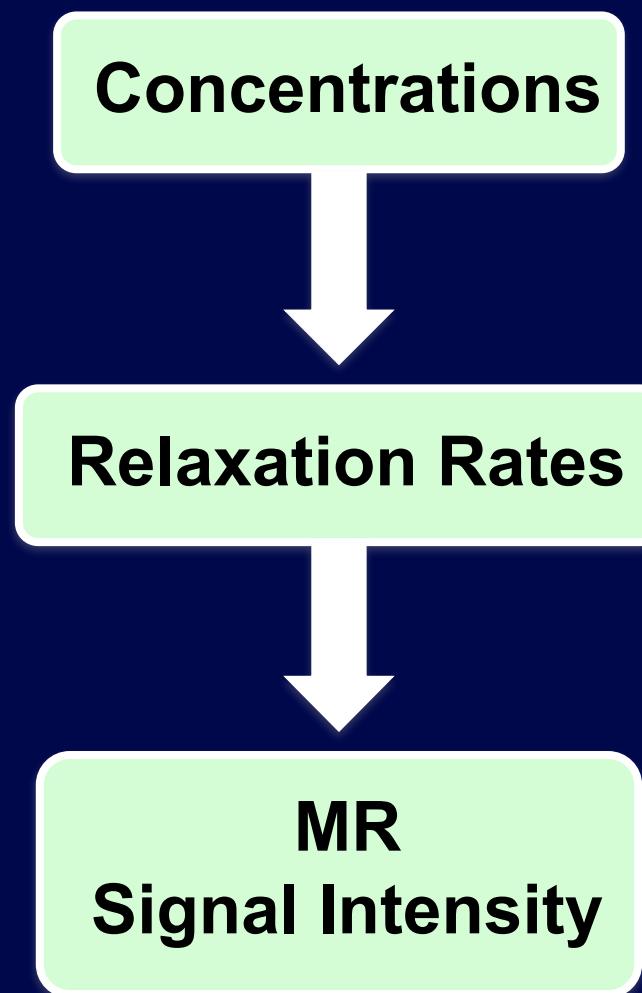
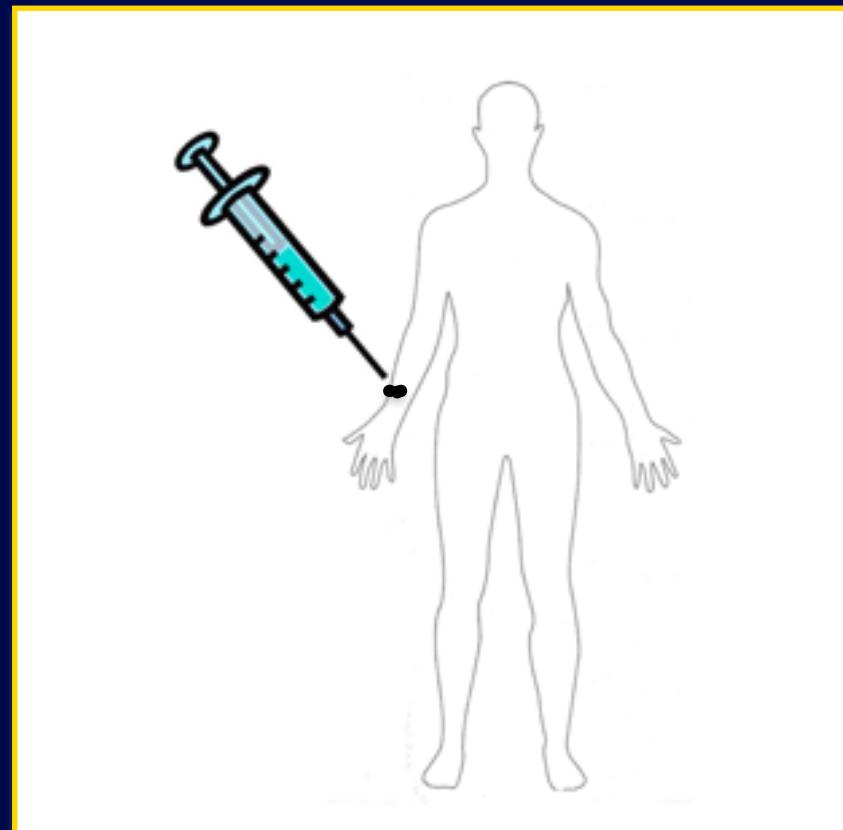


David Geffen  
School of Medicine

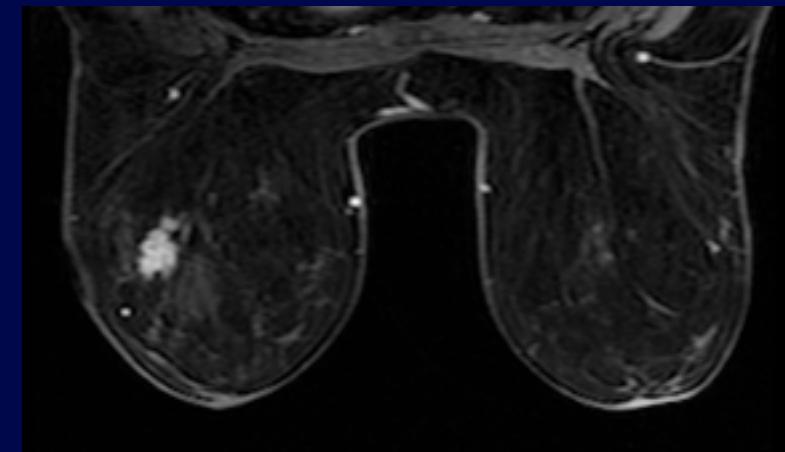
**UCLA**  
Radiology

# T1-weighted DCE-MRI

- DCE-MRI continuously monitors enhancement of tissue before and after injection of contrast agent



Dynamic 3D MR Imaging



David Geffen  
School of Medicine

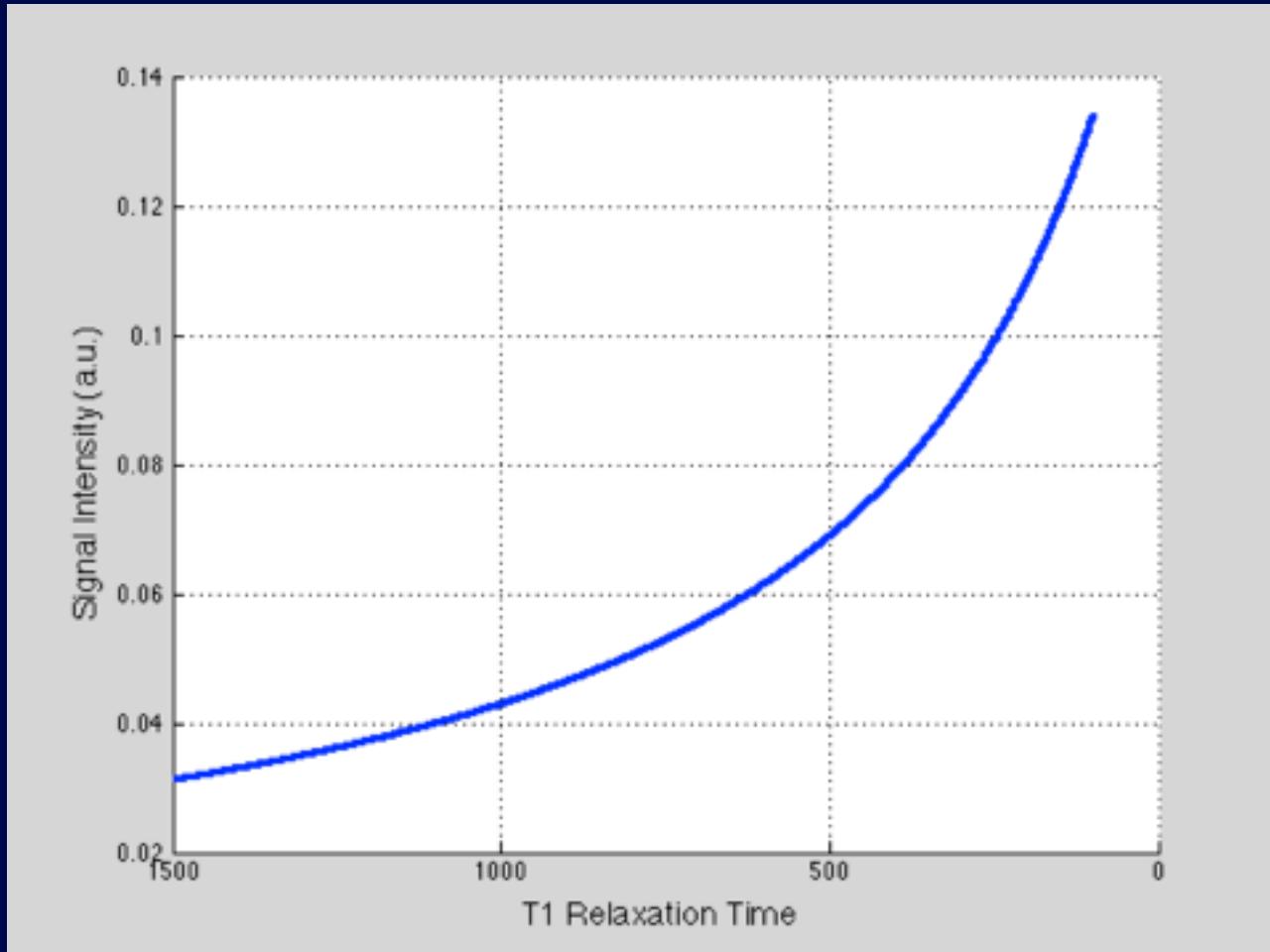
**UCLA**  
Radiology

# MR Signal Intensity

- Signal equation for RF-spoiled gradient echo (T1-weighted) sequence:

$$S \propto \frac{(1 - e^{-TR/T1}) \sin \theta}{1 - e^{-TR/T1} \cos \theta}$$

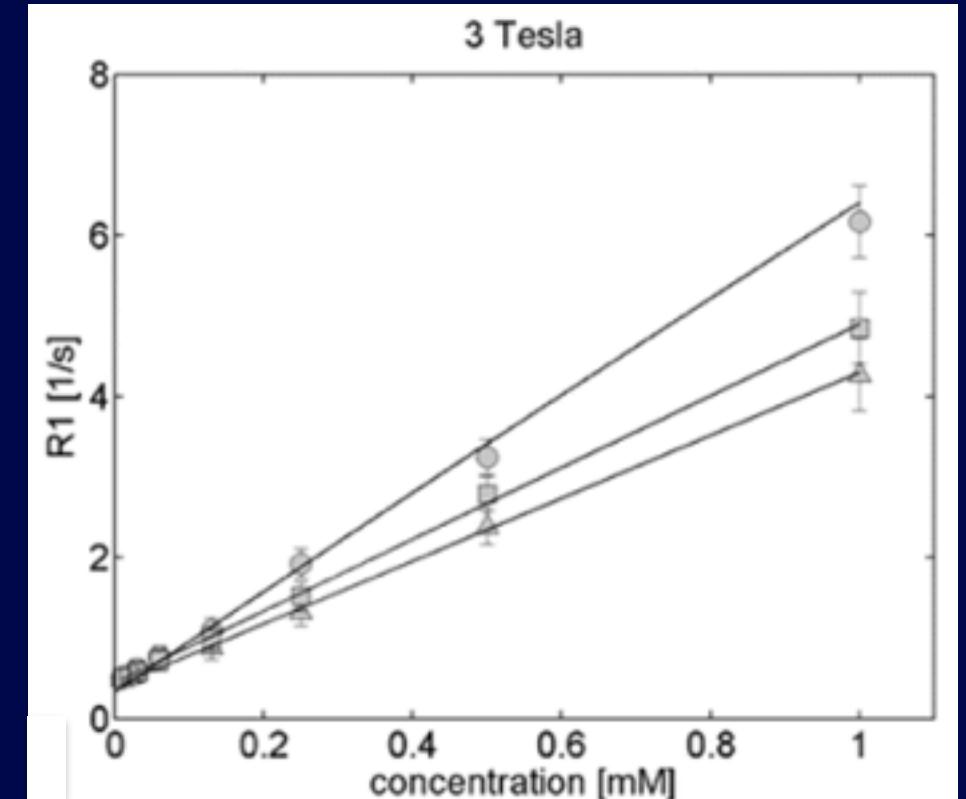
- MR signal intensity is **not linearly proportional** to T1 relaxation time



# Relaxivity of Contrast Agent

- $1/T_1 (R_1)$  is linearly proportional to concentration
  - Relaxivities ( $r_1$ ) of the contrast agent determine the slopes

Gadolinium Chelate	$r_1$ relaxivities at 3T ( $L \text{ mmol}^{-1} \text{ s}^{-1}$ )
Magnevist (Gd-DTPA)	3.3
Gadovist (Gd-BT-DO3A)	3.6
MultiHance (Gd-BOPTA)	6.3



Pintaske J. Investigative Radiology 2006



David Geffen  
School of Medicine

**UCLA**  
Radiology

# Quantitative DCE MRI

- Measurement of baseline relaxation time ( $T_{1,0}$ ) is required to monitor concentration  $C(t)$  from MR signal intensity

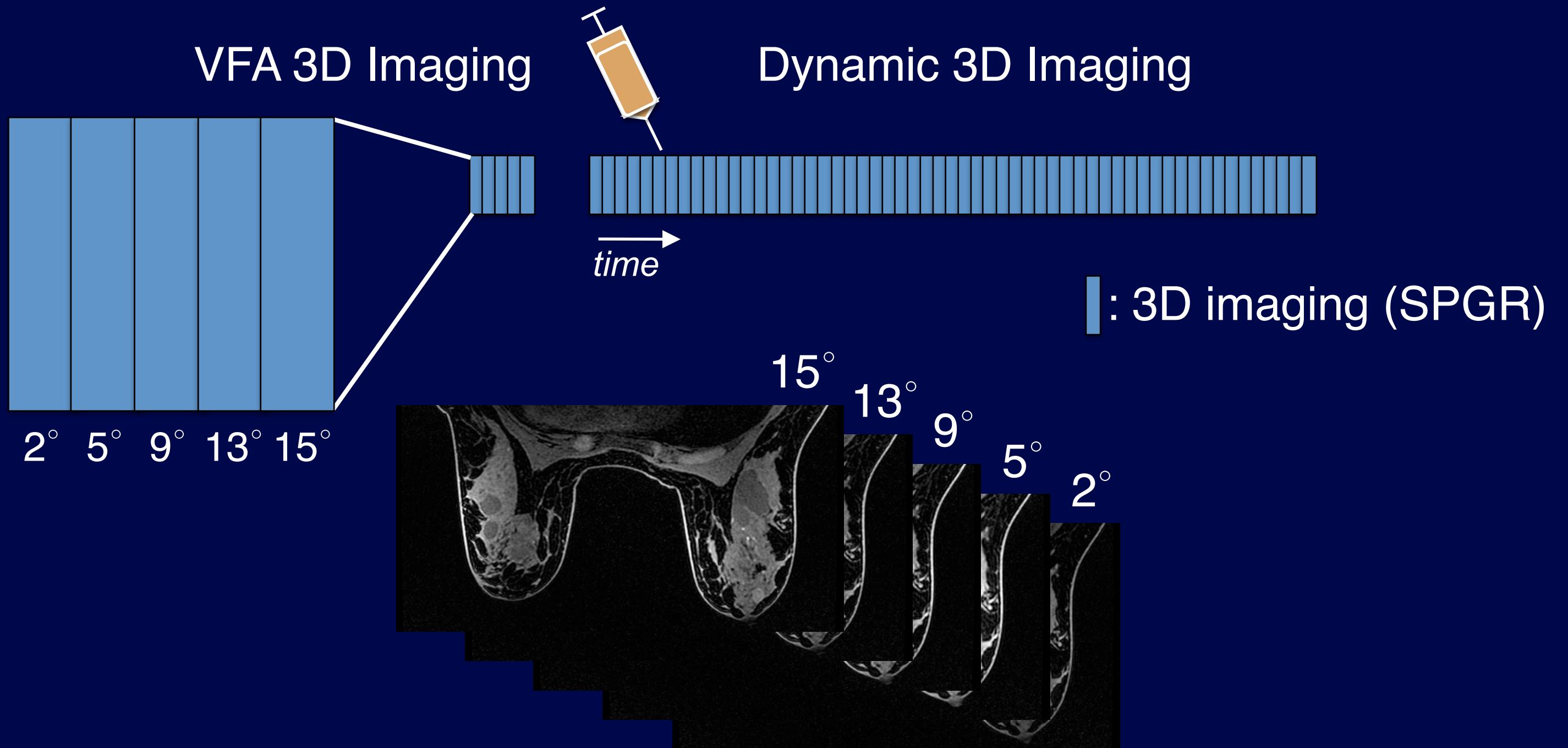
$$\frac{1}{\overline{T_1(t)}} = \frac{1}{\overline{T_{1,0}}} + \gamma \cdot C_t(t)$$

Relaxation time              Baseline relaxation time              Contrast agent concentration

- Assume  $T_{1,0}$  vs. Measure  $T_{1,0}$
- Variable flip angle (VFA) approach, often called DESPOT1, is a common choice for fast 3D volumetric  $T_{1,0}$  mapping



# VFA $T_{1,0}$ Measurements



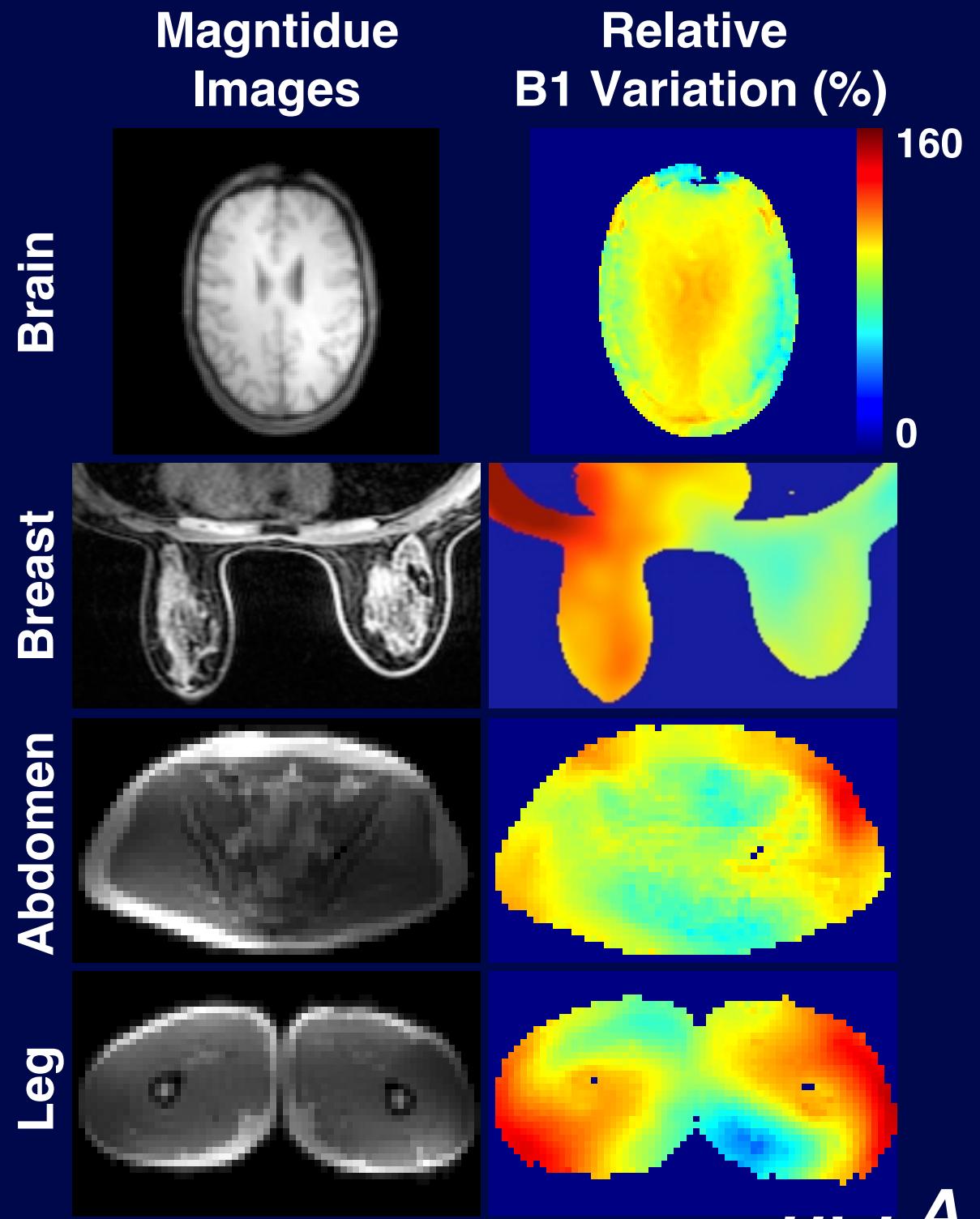
David Geffen  
School of Medicine

**UCLA**  
Radiology

# B1 inhomogeneity at 3T

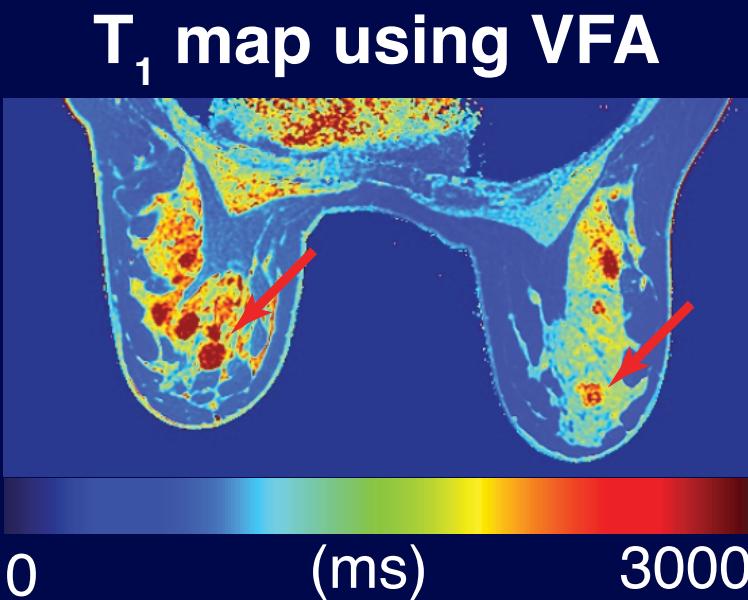
- VFA  $T_{1,0}$  mapping is sensitive to B1 inhomogeneity
- Transmit RF (B1) field inhomogeneity can create 30 – 50 % flip angle variation across the body at 3T

*Sung K, et al. JMRI 2008  
Azlan C, et al. JMRI 2010  
Hancu I, et al. ISMRM 2010 p.2470  
Sung K, et al. JMRI 2013*



# Compensating for B1 inhomogeneity at 3T

- Additional B1 measurements / B1 shimming may be needed to compensate for B1 inhomogeneity
- There exist other ways to compensate for B1 inhomogeneity



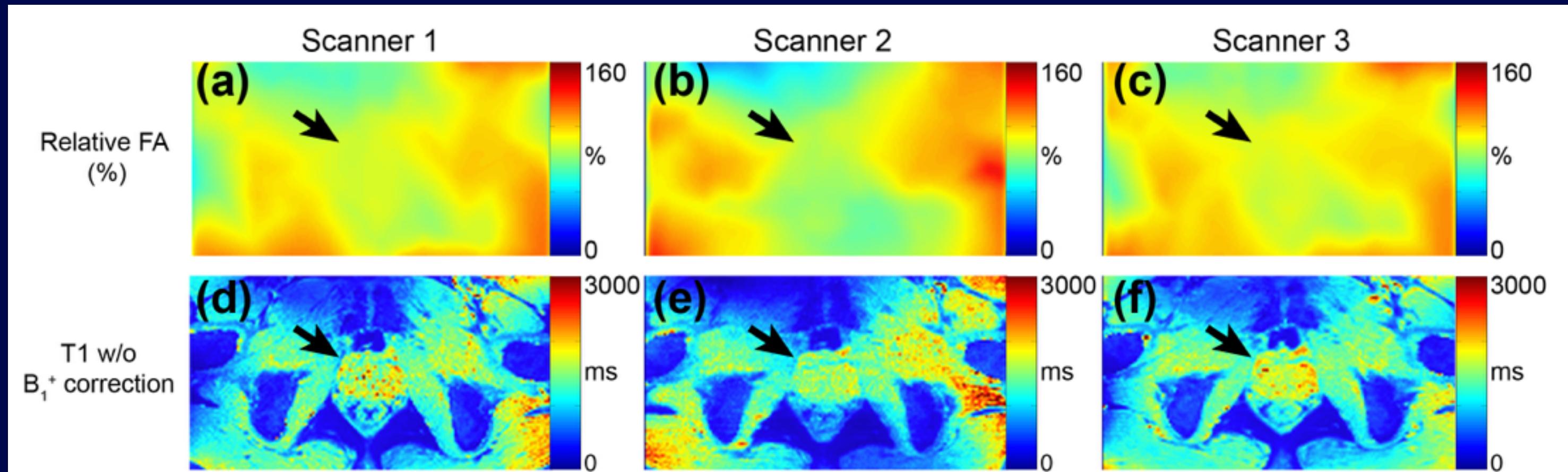
Sung K, MRM 2013



David Geffen  
School of Medicine

**UCLA**  
Radiology

# Challenges: Inter- and Intra-scanner Variability



*K Sung, et. al., MRM 2013  
N Rangwala, et. al., JMRI 2016*



David Geffen  
School of Medicine

**UCLA**  
Radiology

# Summary

---

- Pre-contrast T1 ( $T_{1,0}$ ) information is needed for conversion from MR signal to concentration
  - Assume  $T_{1,0}$  from literature
  - Measure  $T_{1,0}$  using VFA
- VFA  $T_{1,0}$  mapping requires
  - Careful selection of a set of flip angles
  - Sufficient SNR (e.g., multiple measurements)
  - Compensation for B1 inhomogeneity (for  $\geq 3T$  applications)



# Pharmacokinetic Modeling: Concentration → Quantitative Biomarkers



David Geffen  
School of Medicine

**UCLA**  
Radiology

# Pharmacokinetics

---

- Pharmacokinetics
  - What the body does to the drug (or contrast agent)
  - Related “doses of drug” to “concentrations of drug at various locations in the body”
- Although pharmacokinetics is a leap from the molecular and cellular analyses,
  - We are interested in kinetic phenomena that occur at the level of the whole body



# Compartment Models

---

- The body is divided into compartments
  - Vascular plasma space
  - Extracellular extravascular space (EES) or interstitial space
  - Intracellular space
- Each compartment is assumed to be well-mixed
  - Uniform concentration in each compartment
  - Want to know how the average concentration of the drug varies with time in the compartment
  - Mass can be transferred between different compartments
  - Inputs for drug entering the body / Outputs for drug clearance



# Compartment Models

---

- Each compartment has:
  - Volume
  - Average concentration of drug
- Principles
  - Mass conservation
  - Rate constants for transfer between compartments
- Compartment models are not mechanistic
  - Several processes are lumped in black boxes



# Drug Administration and Clearance

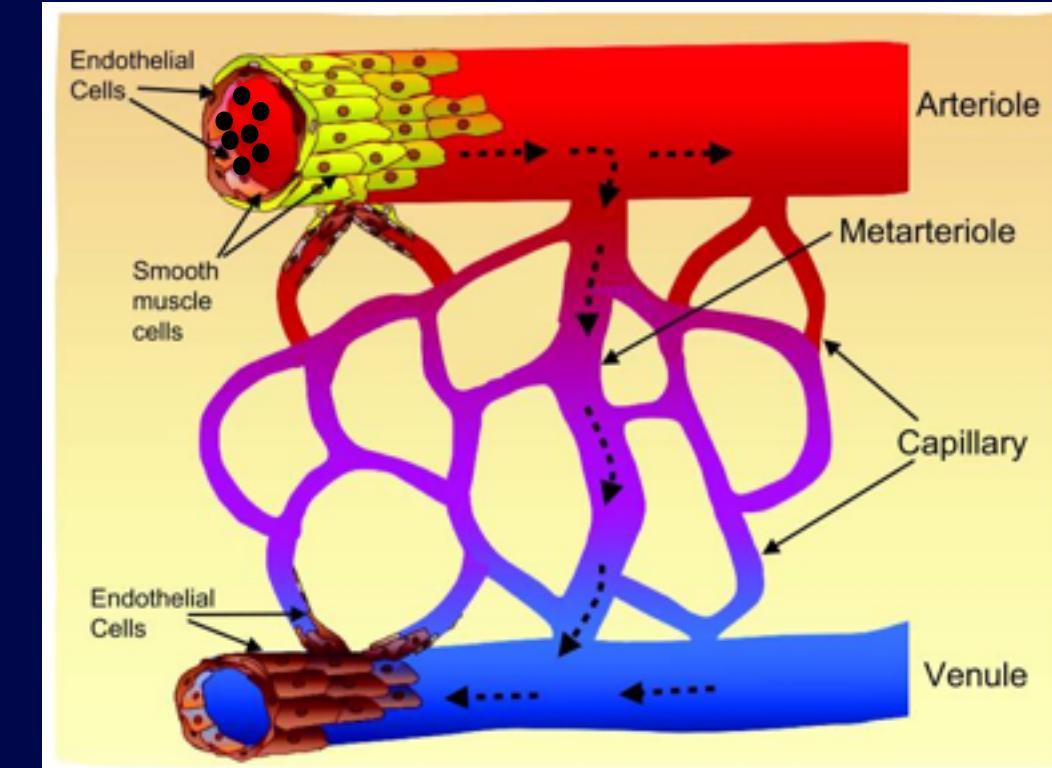
---

- Drug administration
  - Controlled release from devices
  - Intravenous injection
- Drug Clearance
  - Renal excretion
  - Renal and liver excretion



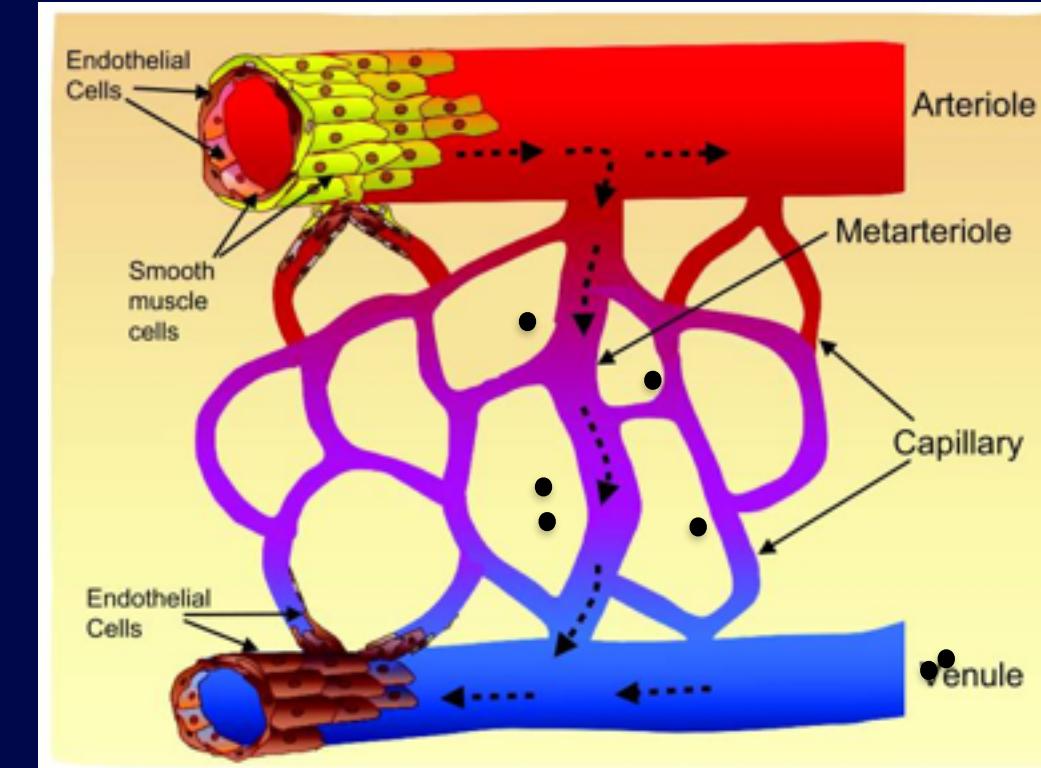
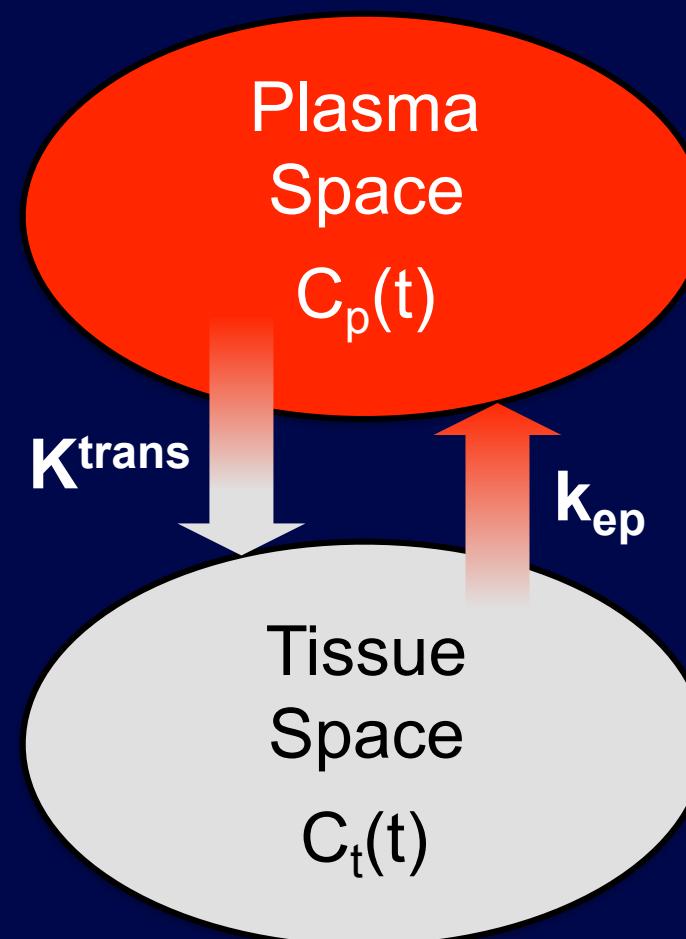
# Pharmacokinetic Modeling

- Three tissue compartments
  - Vascular plasma space
  - Extracellular extravascular space (EES)
  - Intracellular space

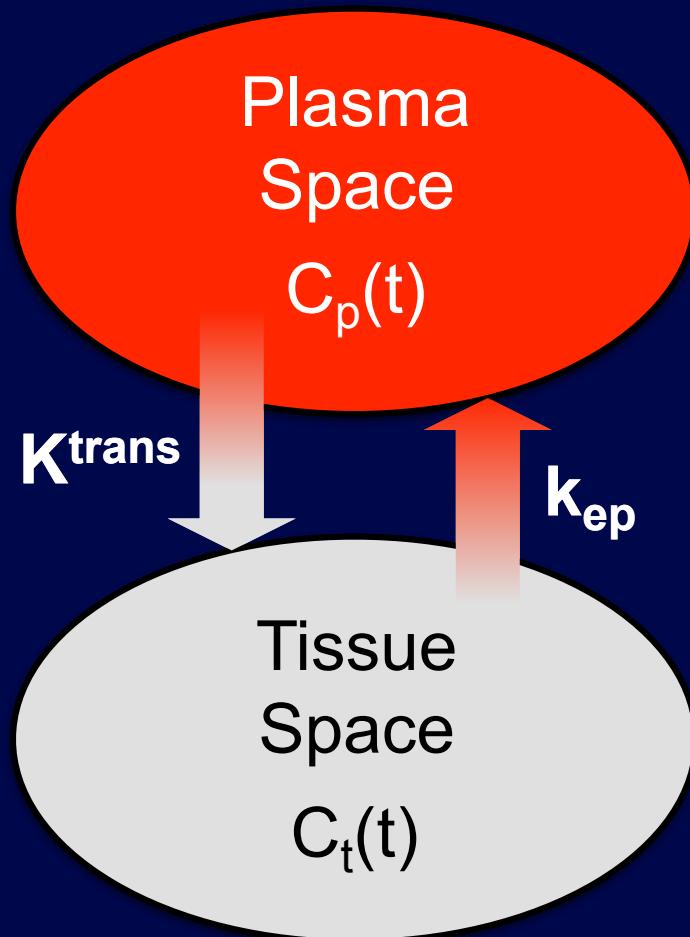


# Pharmacokinetic Modeling

- Three tissue compartments
  - Vascular plasma space
  - Extracellular extravascular space (EES)
  - Intracellular space



# Fick's First Law of Diffusion



- Fick's first law relates **diffusive flux** to the concentration field (flux from high to low concentration) with magnitude that is **proportional to the concentration gradient**

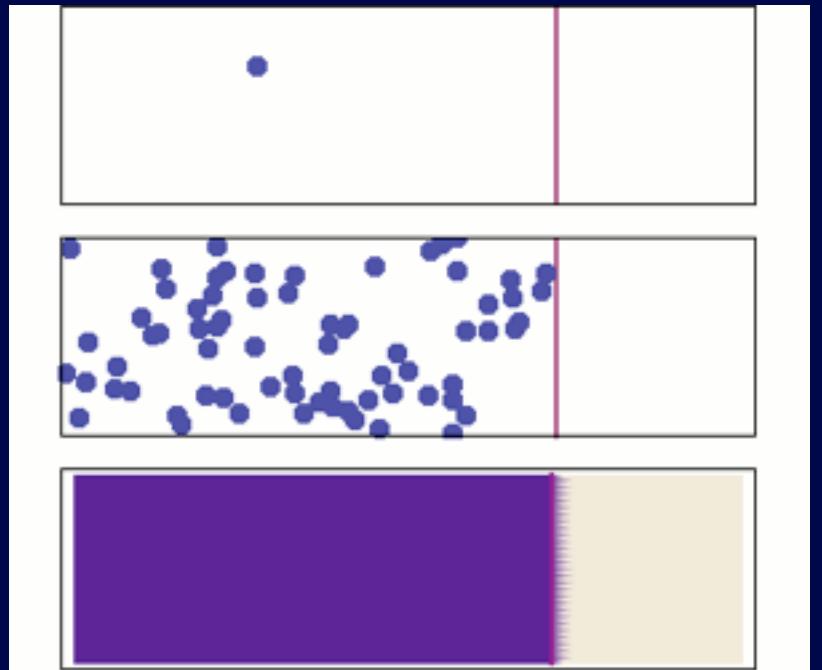
- Fick's first law gives:

$$\Phi_d = PA(C_1 - C_2)$$

Diffusive flux

Transfer constant

Concentrations on each side of membrane



$$\frac{dC_t}{dt} = K^{trans} (C_p - C_t/v_e)$$

Volume of EES  
per unit volume of tissue

Kety SS, Pharmacol Rev 1951

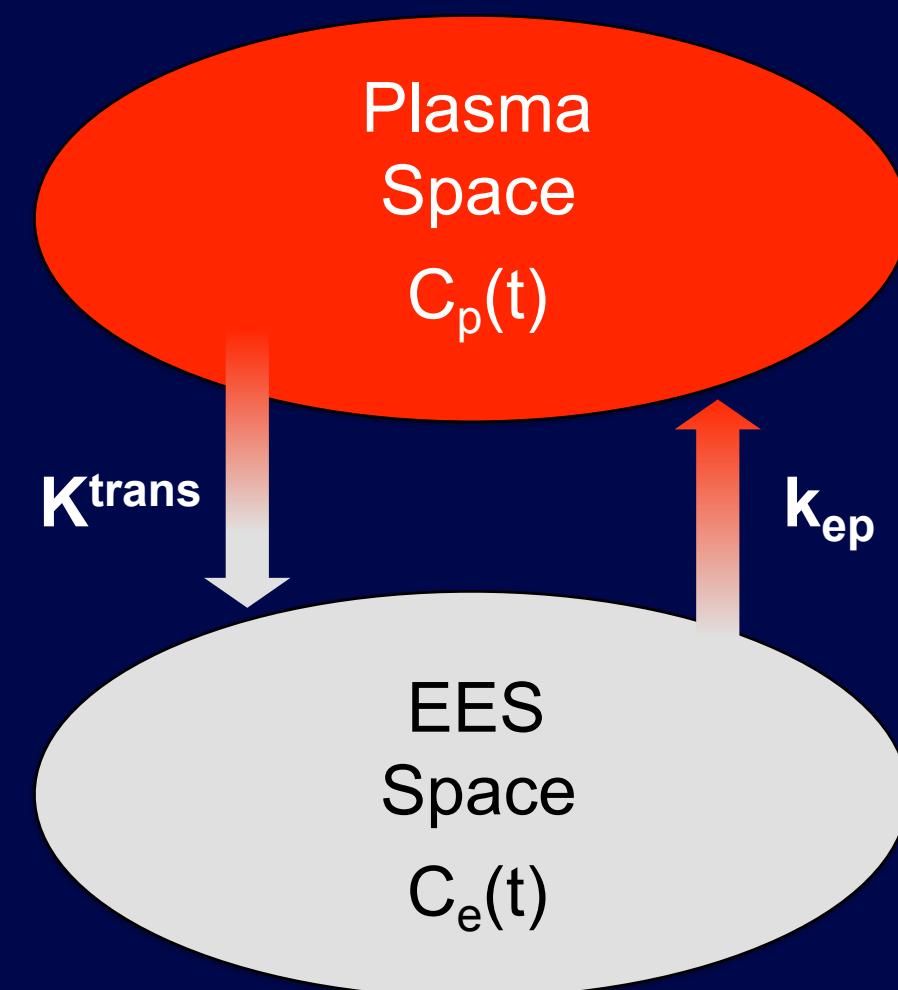
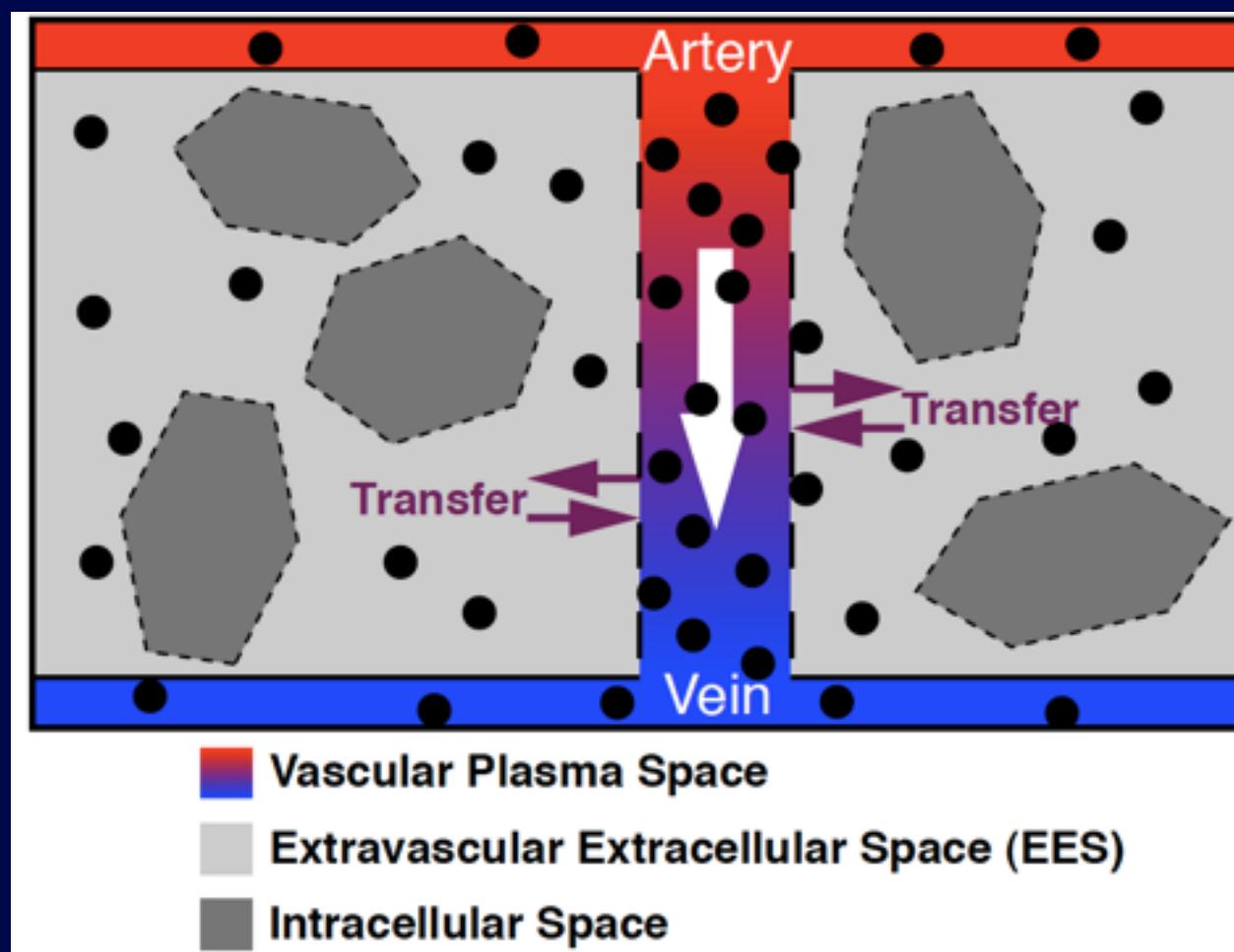


David Geffen  
School of Medicine

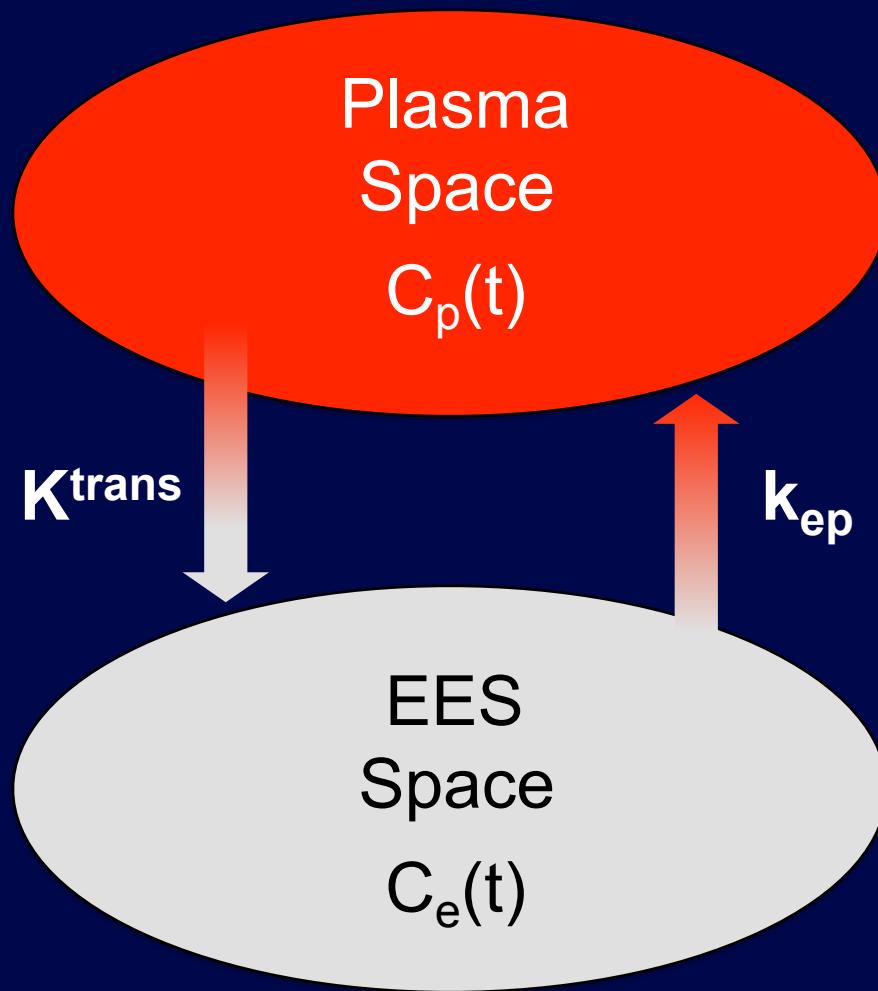
**UCLA**  
Radiology

# Pharmacokinetic Modeling

- Two tissue compartments
  - Vascular plasma space
  - Extracellular extravascular space (EES)



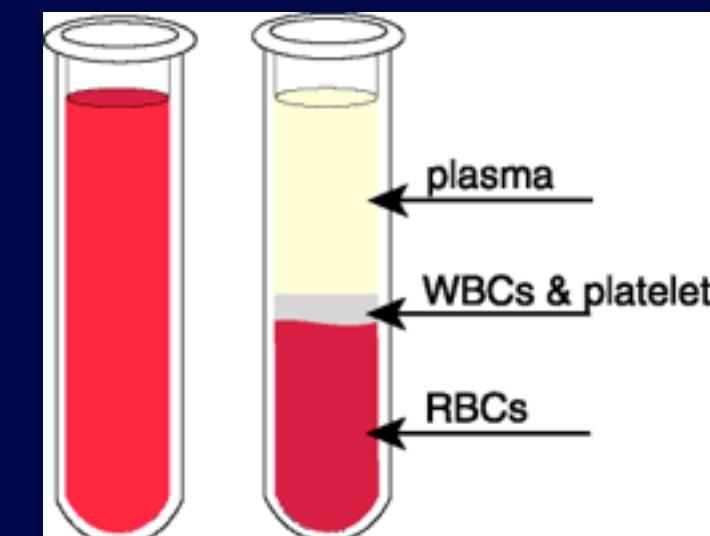
# Standard Tofts Model



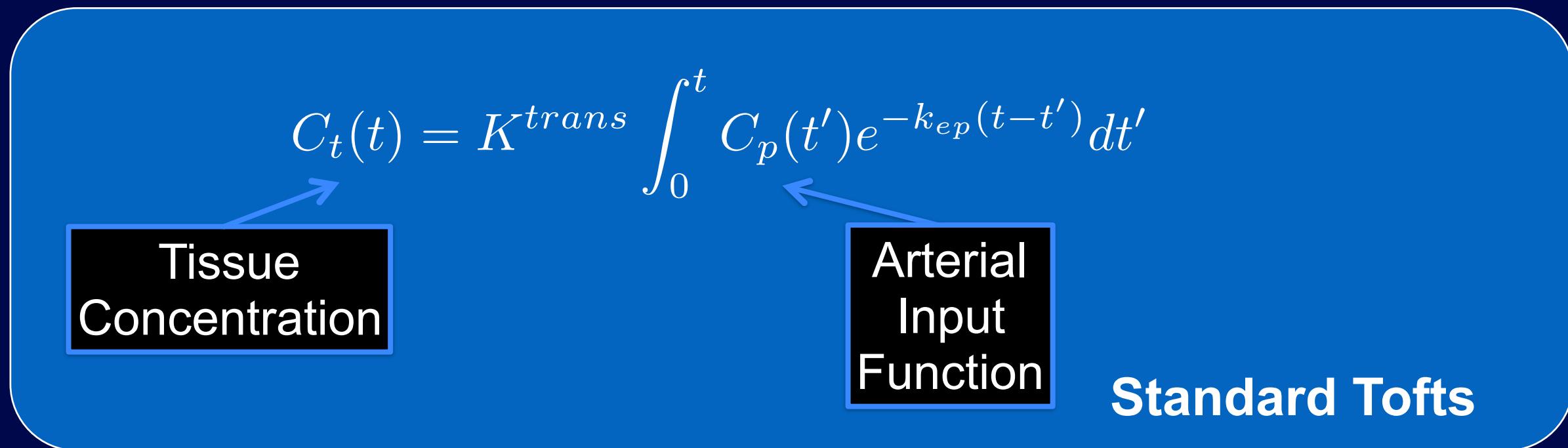
$$\frac{dC_t}{dt} = K^{trans}(C_p - C_t/v_e)$$

- Tissue concentration  $\neq$  EES concentration
  - $C_t = v_e \cdot C_e$
- Plasma concentration  $\neq$  Blood concentration
  - $C_p = C_b/(1-Hct)$

*Matsuzawa T. Comp Haematol Int 1996*



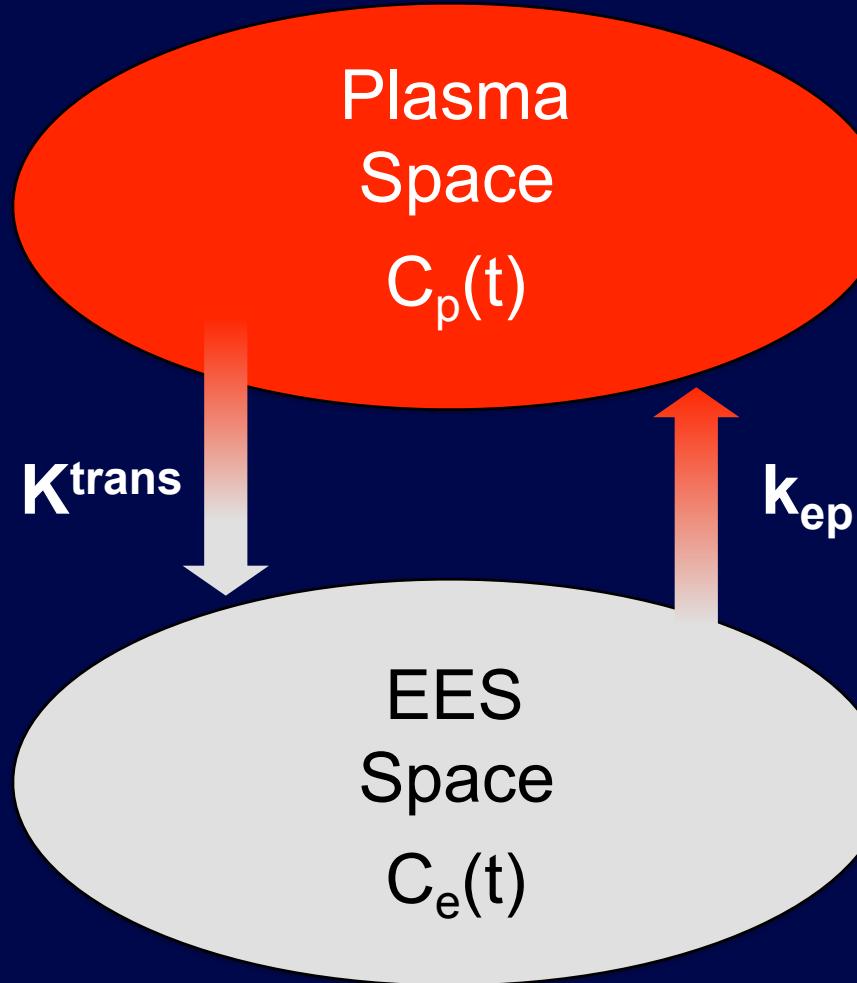
# Standard Tofts Model



Symbol	Preferred short name	Units	Full name
$K^{trans}$	Transfer constant <sup>a</sup>	$\text{min}^{-1}$	Volume transfer constant between blood plasma and EES
$k_{ep}$	Rate constant	$\text{min}^{-1}$	Rate constant between EES and blood plasma
$v_e$	EES <sup>d</sup>	None	Volume of extravascular extracellular space per unit volume of tissue <sup>e</sup>



# Arterial Input Function (AIF)



- Population-averaged AIF:
  - Bi-exponential model
  - Bi-exponential + linear upslope model
  - Single Gaussian + exponential model
  - Dual Gaussian + exponential model

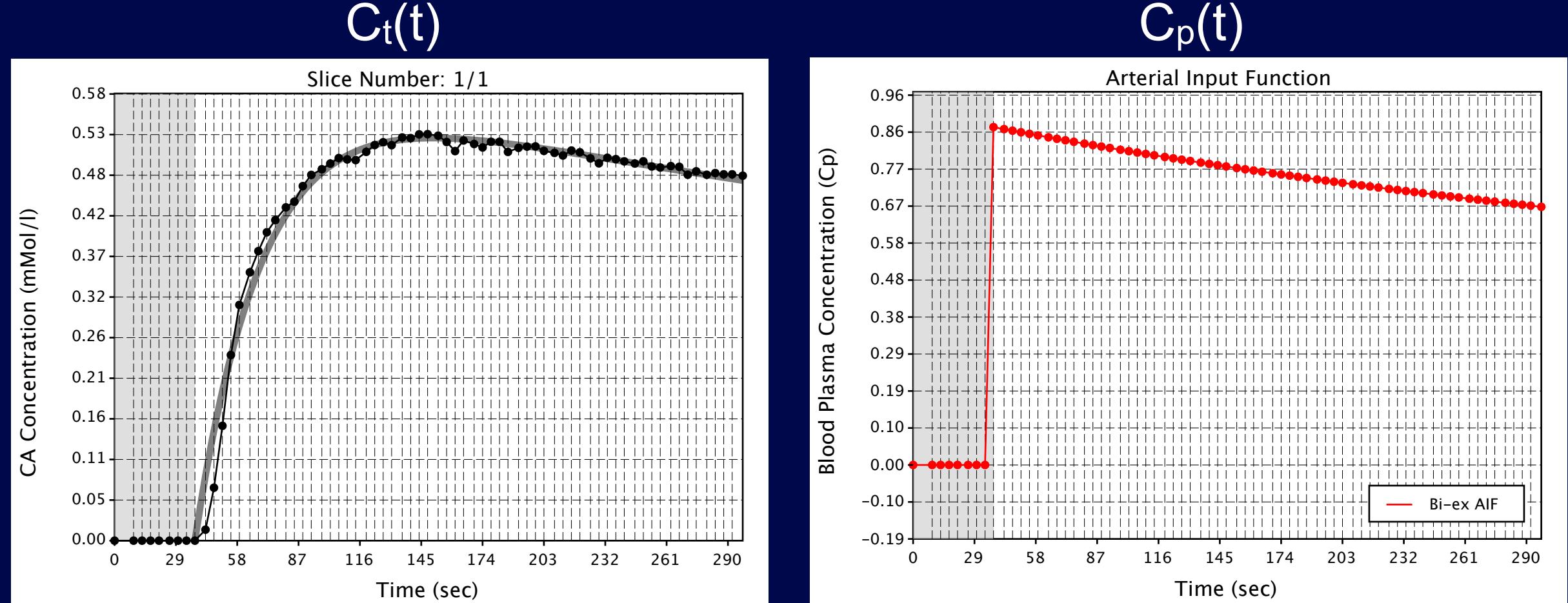
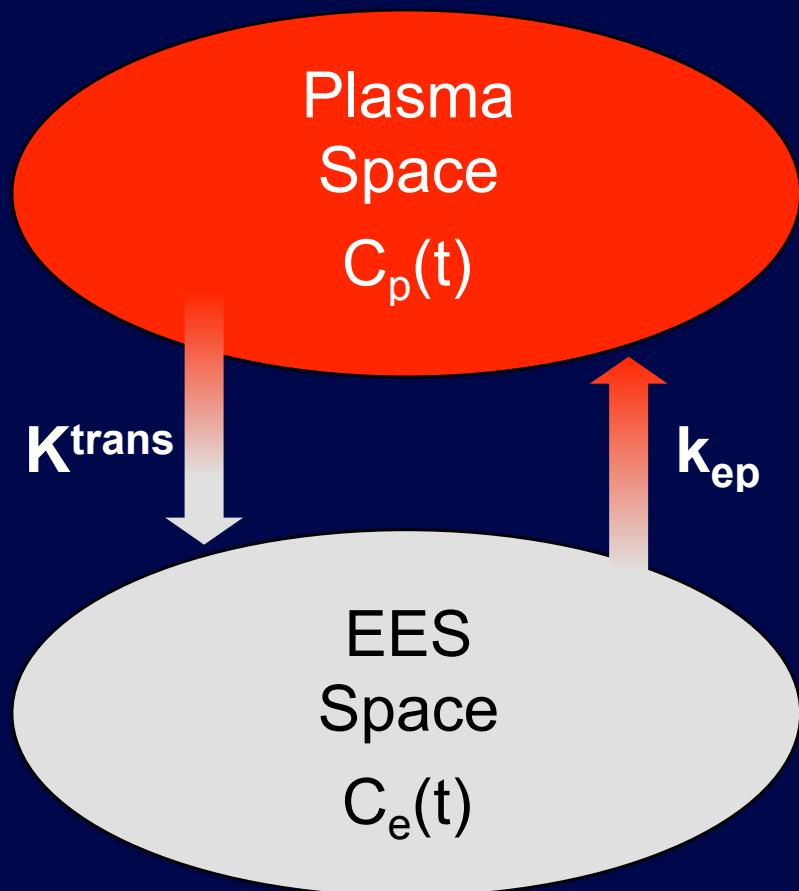
*McGrath DM, MRM 2009*

- Subject-based AIF requires
  - High temporal and spatial resolution
  - Compensation for flow-enhancement



# Bi-exponential Model: Weimann AIF

$$C_t(t) = K^{trans} \int_0^t C_p(t') \exp\left(\frac{-K^{trans}(t-t')}{v_e}\right) dt'$$



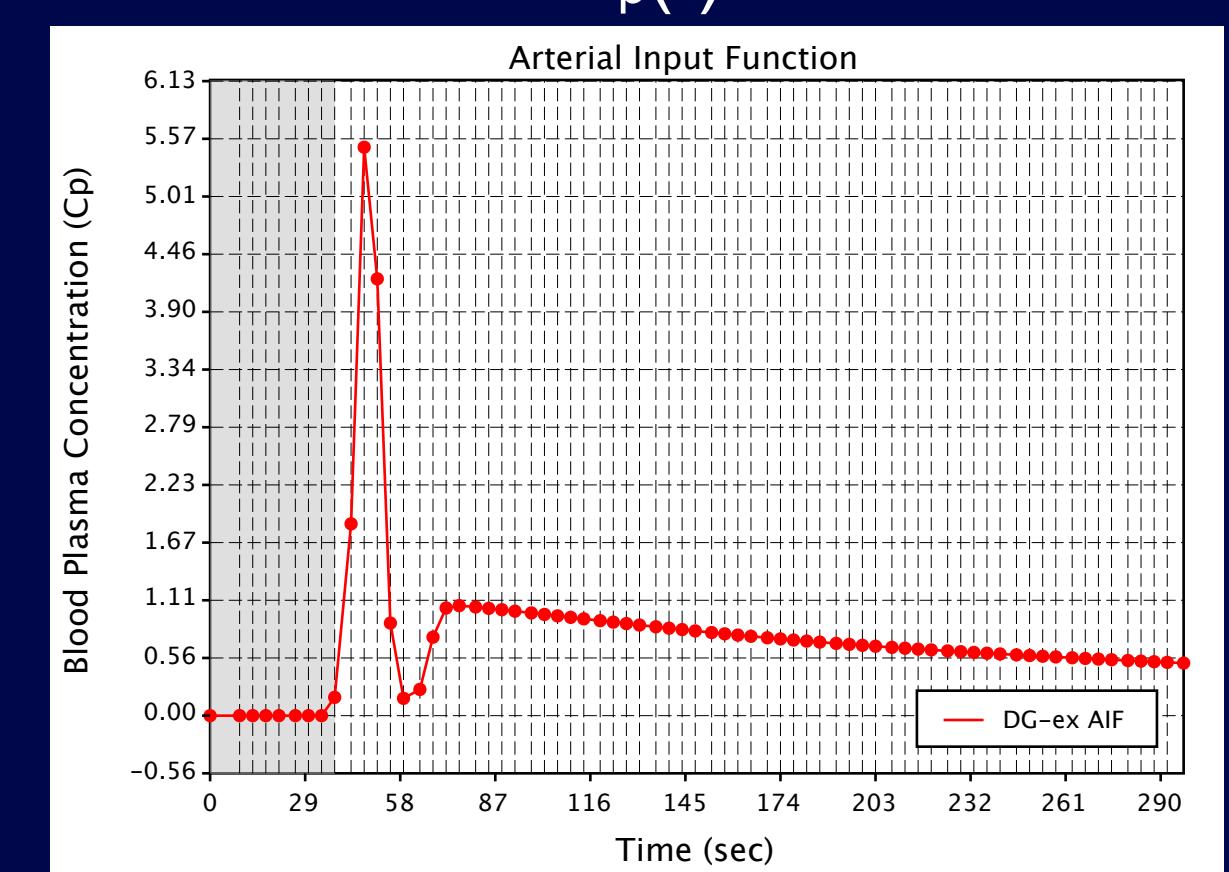
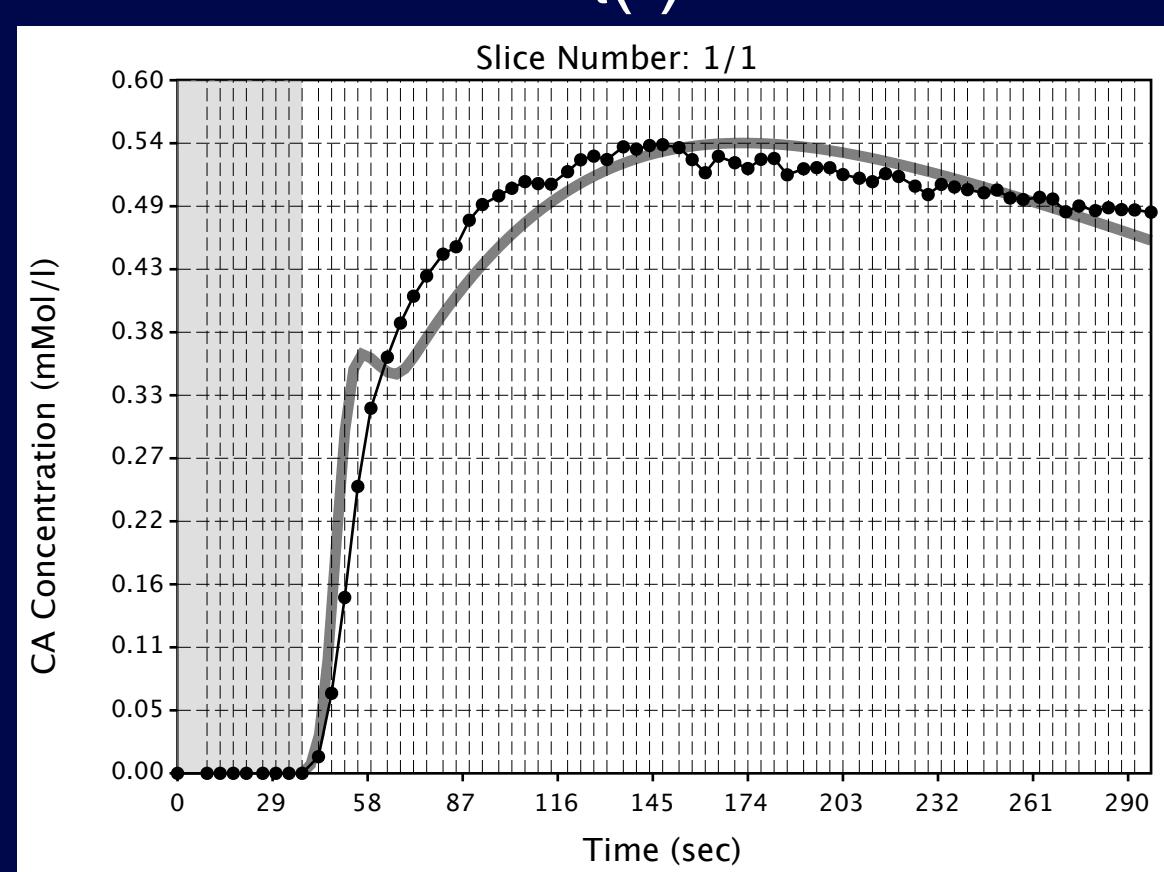
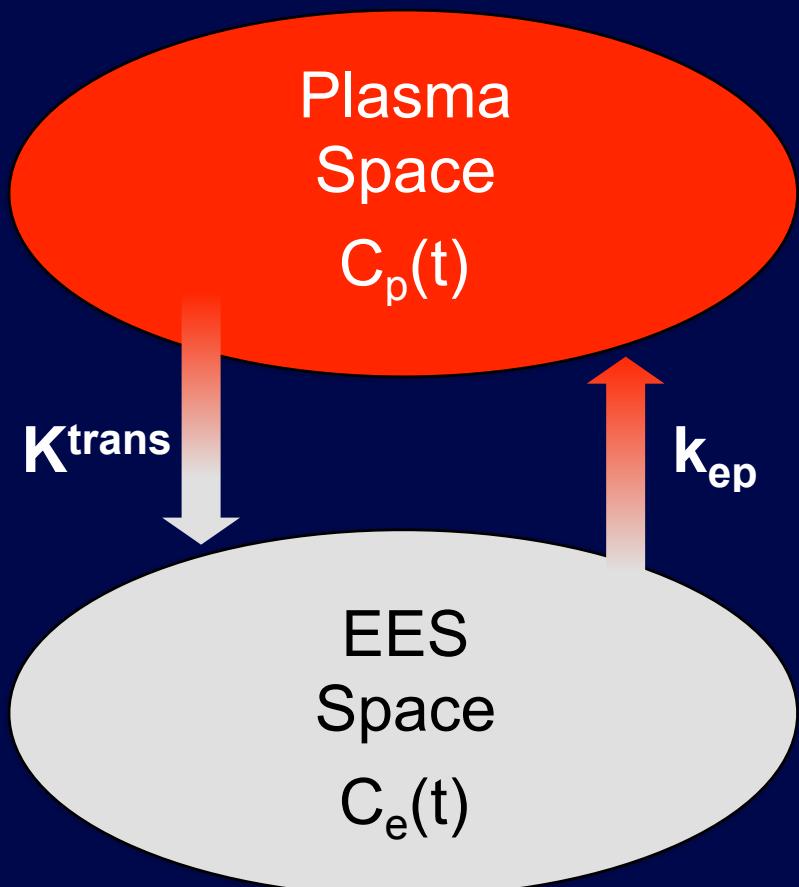
$$K^{trans} = 1.32 \text{ min}^{-1}$$

$$k_{ep} = 1.91 \text{ min}^{-1}$$



# Dual-Gaussian+Exponential Model: Parker AIF

$$C_t(t) = K^{trans} \int_0^t C_p(t') \exp\left(\frac{-K^{trans}(t-t')}{v_e}\right) dt'$$



$$K^{trans} = 0.47 \text{ min}^{-1}$$

$$k_{ep} = 0.65 \text{ min}^{-1}$$

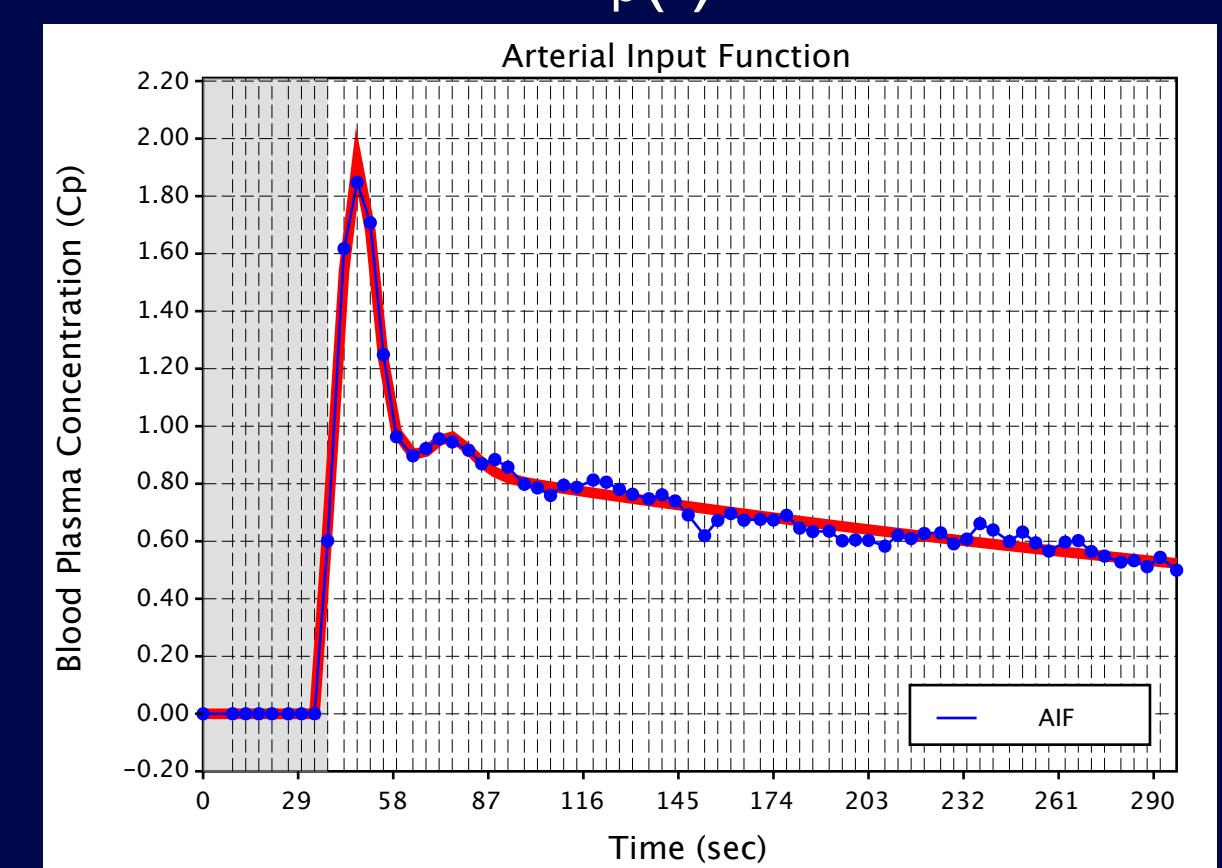
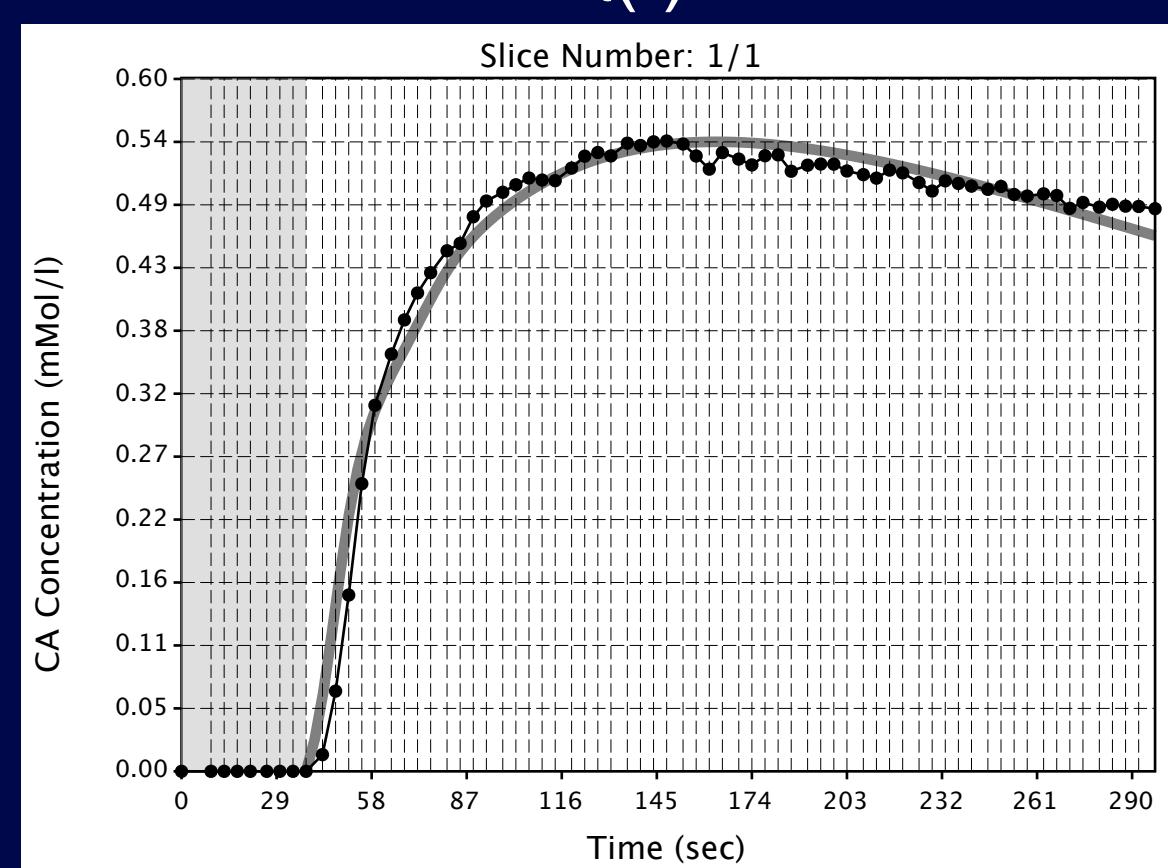
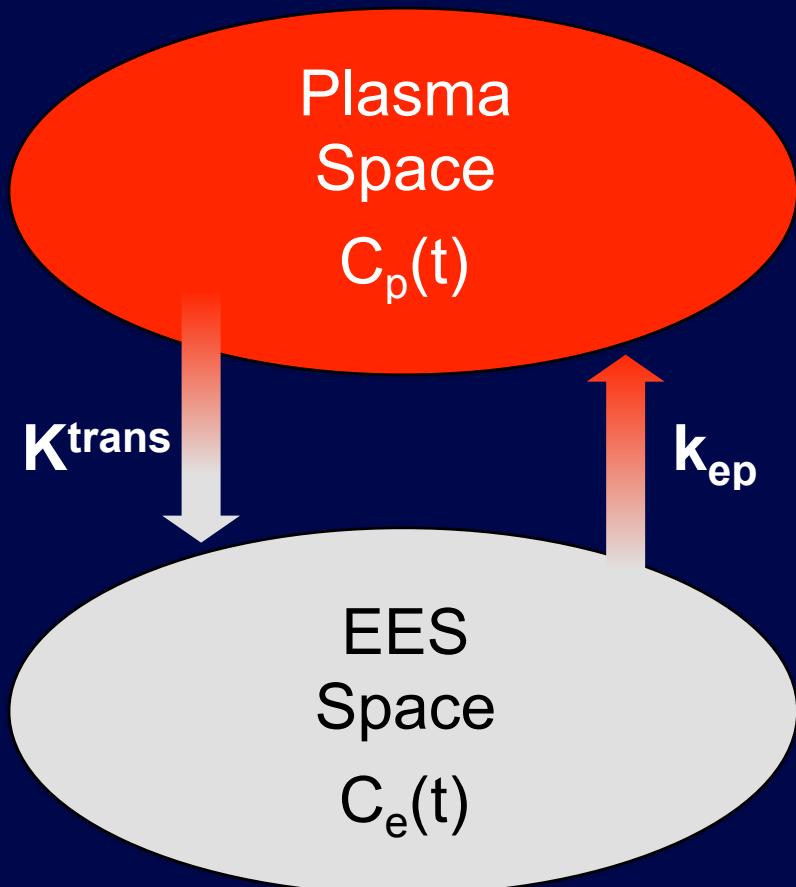


David Geffen  
School of Medicine

**UCLA**  
Radiology

# Subject-based AIF

$$C_t(t) = K^{trans} \int_0^t C_p(t') \exp\left(\frac{-K^{trans}(t-t')}{v_e}\right) dt'$$



$$K^{trans} = 0.35 \text{ min}^{-1}$$

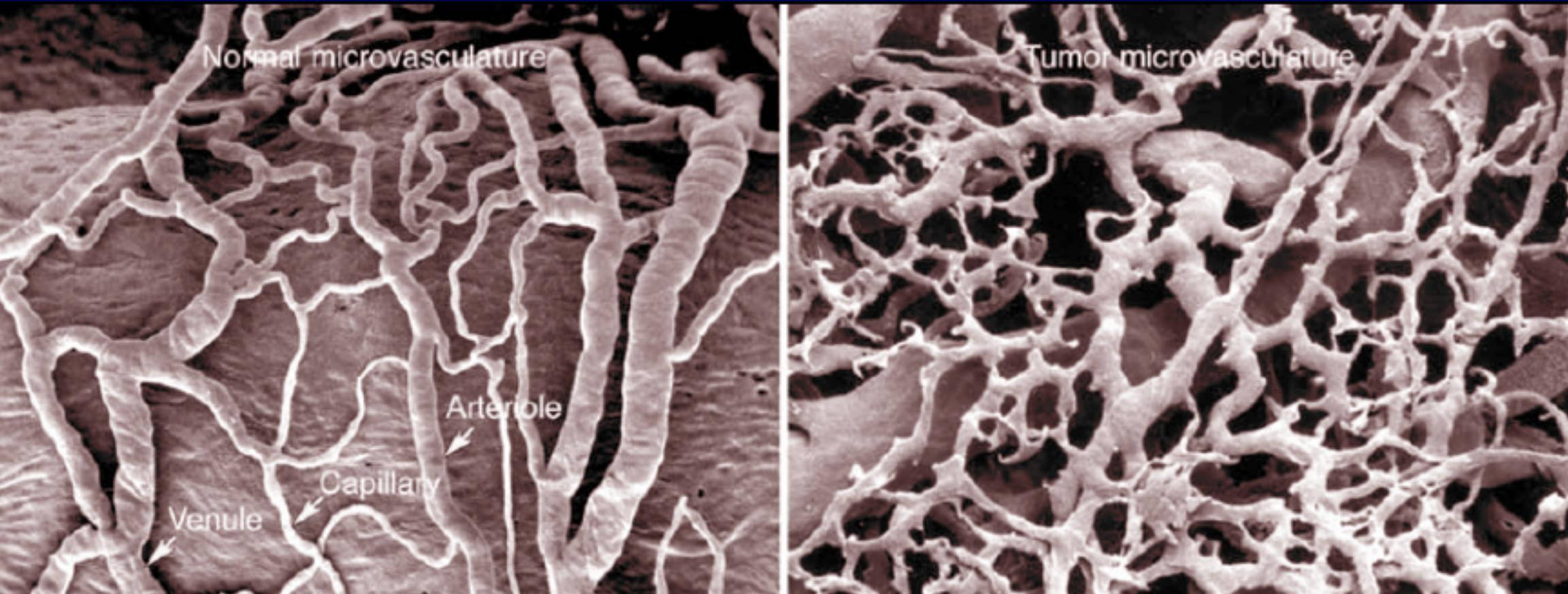
$$k_{ep} = 0.87 \text{ min}^{-1}$$



David Geffen  
School of Medicine

**UCLA**  
Radiology

# Delay and Dispersion Model



- Recruited vasculature is characterized by irregular vessels with increased permeability
- Delay and dispersion model offers another quantitative measure of vasculature

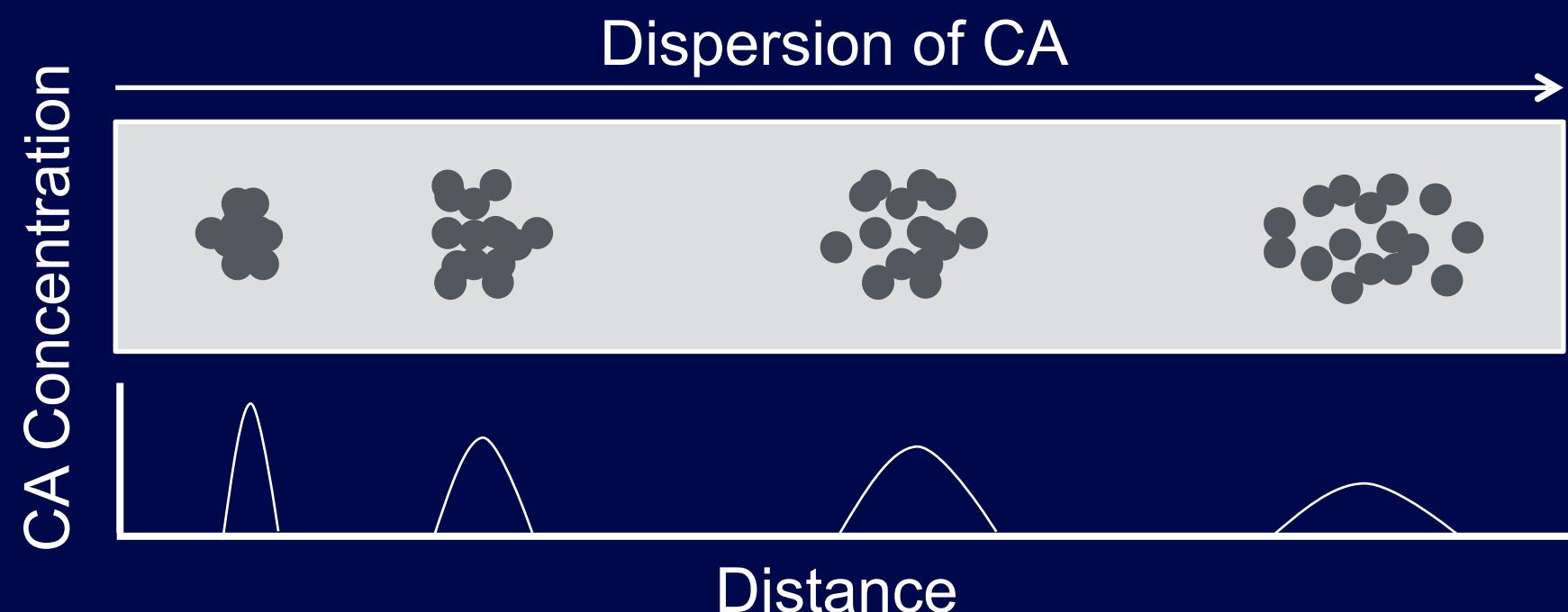
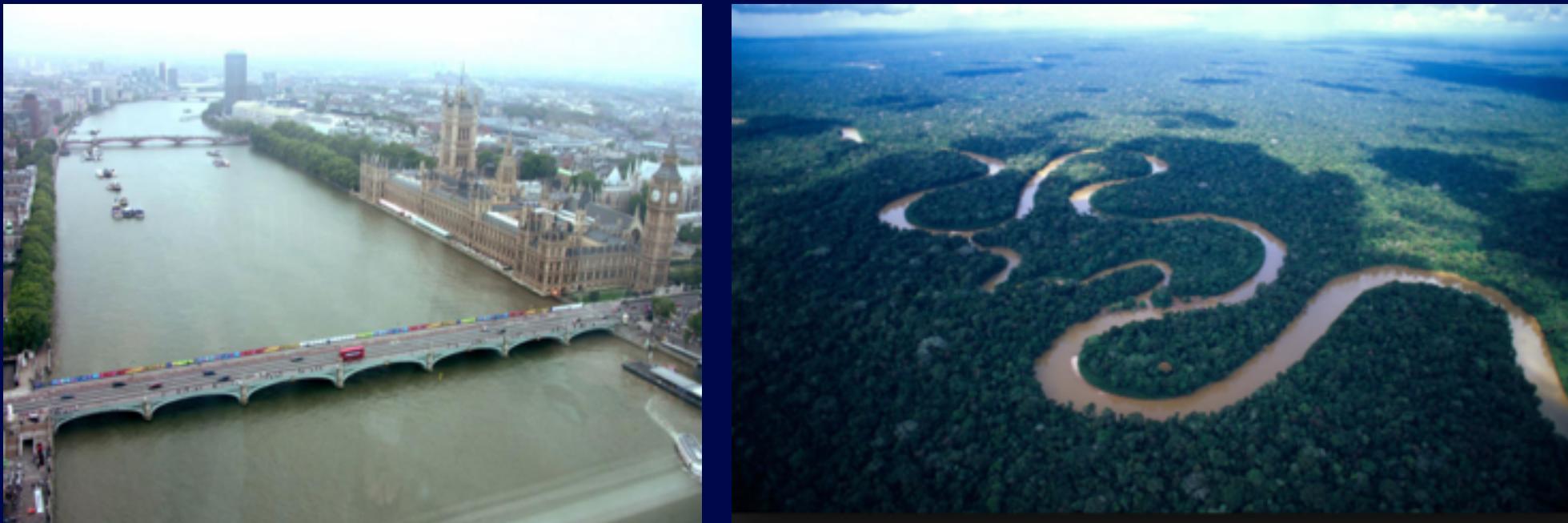


David Geffen  
School of Medicine

**UCLA**  
Radiology

# Delay and Dispersion Model

- Contrast agent will disperse as it travels through the vasculature



# Dispersion Model History

Magnetic Resonance in Medicine 44:466–473 (2000)

**Delay and Dispersion Effects in Dynamic Susceptibility Contrast MRI: Simulations Using Singular Value Decomposition**

Fernando Calamante,\* David G. Gadian, and Alan Connelly

**Contrast-ultrasound diffusion imaging for localization of prostate cancer.**

Authors: M. Kuenen, M. Mischi, H. Wijkstra

 View research catalog entry for this paper

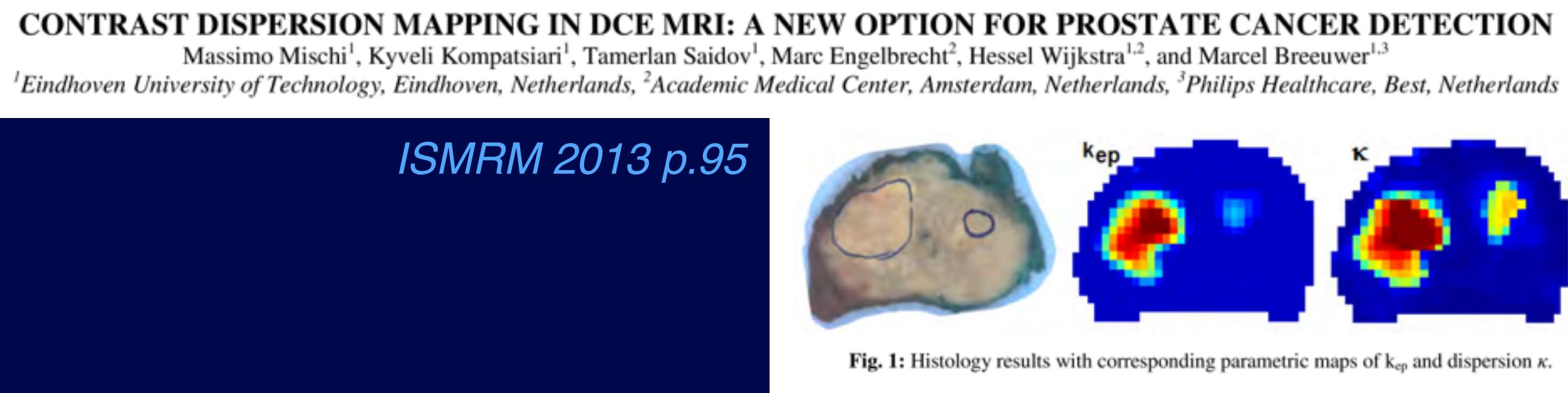
Journal: *IEEE transactions on medical imagi...*

Year: 2011

Volume: 30

Issue:

Pages: 1493–1502



David Geffen  
School of Medicine

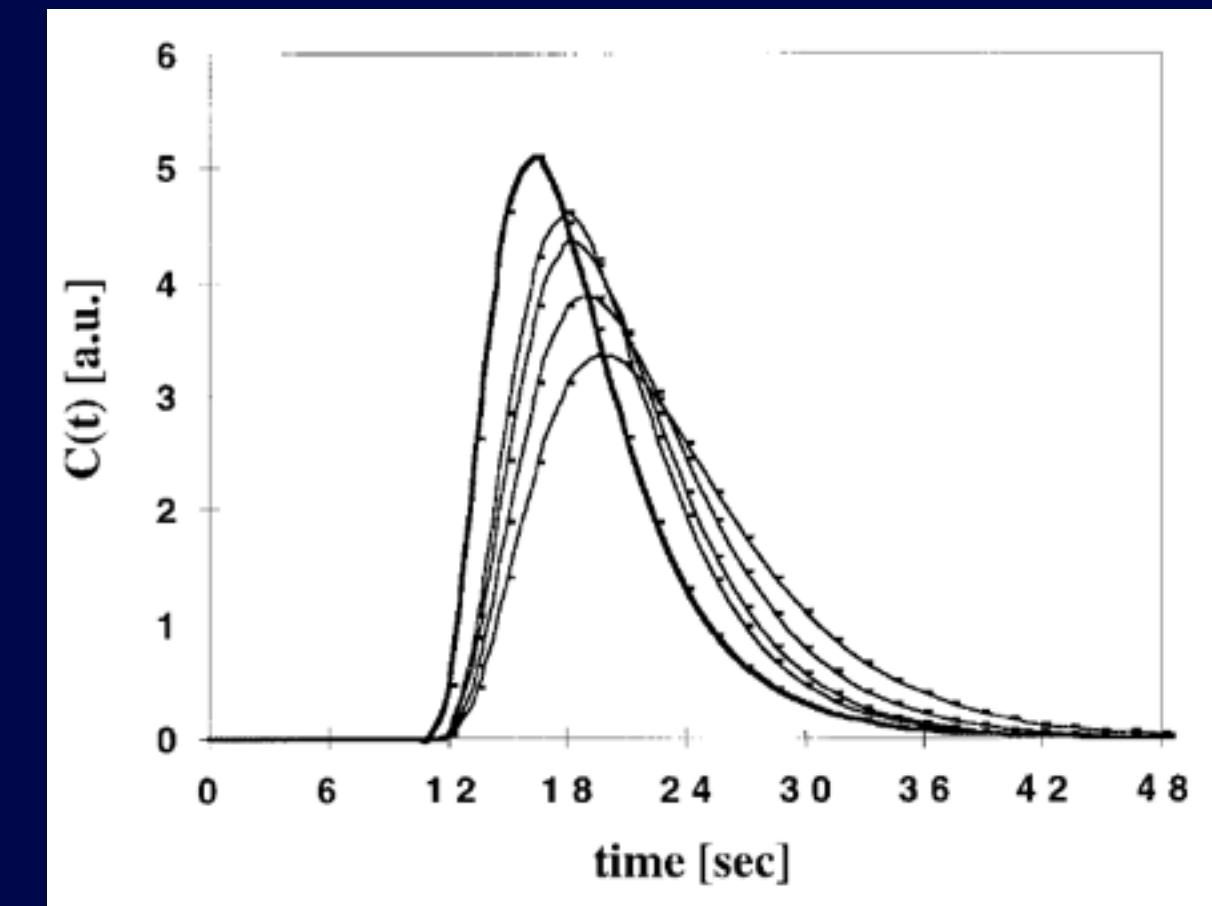
**UCLA**  
Radiology

# Delay and Dispersion Effects in Dynamic Susceptibility Contrast MRI: Simulations Using Singular Value Decomposition

Fernando Calamante,\* David G. Gadian, and Alan Connelly

$$C_a(t) = C_a^{(est)}(t) \otimes h^*(t)$$

$$h^*(t) = -\frac{dR^*(t)}{dt} = \beta \cdot e^{-\beta t}$$



## Standard Tofts

$$C_t(t) = K^{trans} \int_0^t C_p(t') e^{-k_{ep}(t-t')} dt'$$

Population Averaged AIFs ( $C_p(t)$ ):  
Weimann, Fritz-Hans, Parker

## Standard Tofts

$$C_t(t) = \boxed{K^{trans}} \int_0^t C_p(t') e^{-k_{ep}(t-t')} dt'$$

Population Averaged AIFs ( $C_p(t)$ ):  
Weimann, Fritz-Hans, Parker

$$C_p(t) = \alpha \sqrt{\frac{\kappa}{2\pi t}} \cdot e^{\frac{-\kappa(t-\mu)^2}{2t}}$$

Dispersion

$$C_t(t) = \boxed{\beta} \int_0^t \sqrt{\frac{\boxed{\kappa}}{2\pi t}} \cdot e^{\frac{-\kappa(t-\boxed{\mu})^2}{2t}} \cdot e^{-k_{ep}(t-t')} dt'$$

## Standard Tofts

$$C_t(t) = \boxed{K^{trans}} \int_0^t C_p(t') e^{-k_{ep}(t-t')} dt'$$

Population Averaged AIFs ( $C_p(t)$ ):  
Weimann, Fritz-Hans, Parker

$$C_p(t) = \alpha \sqrt{\frac{\kappa}{2\pi t}} \cdot e^{\frac{-\kappa(t-\mu)^2}{2t}}$$

Dispersion

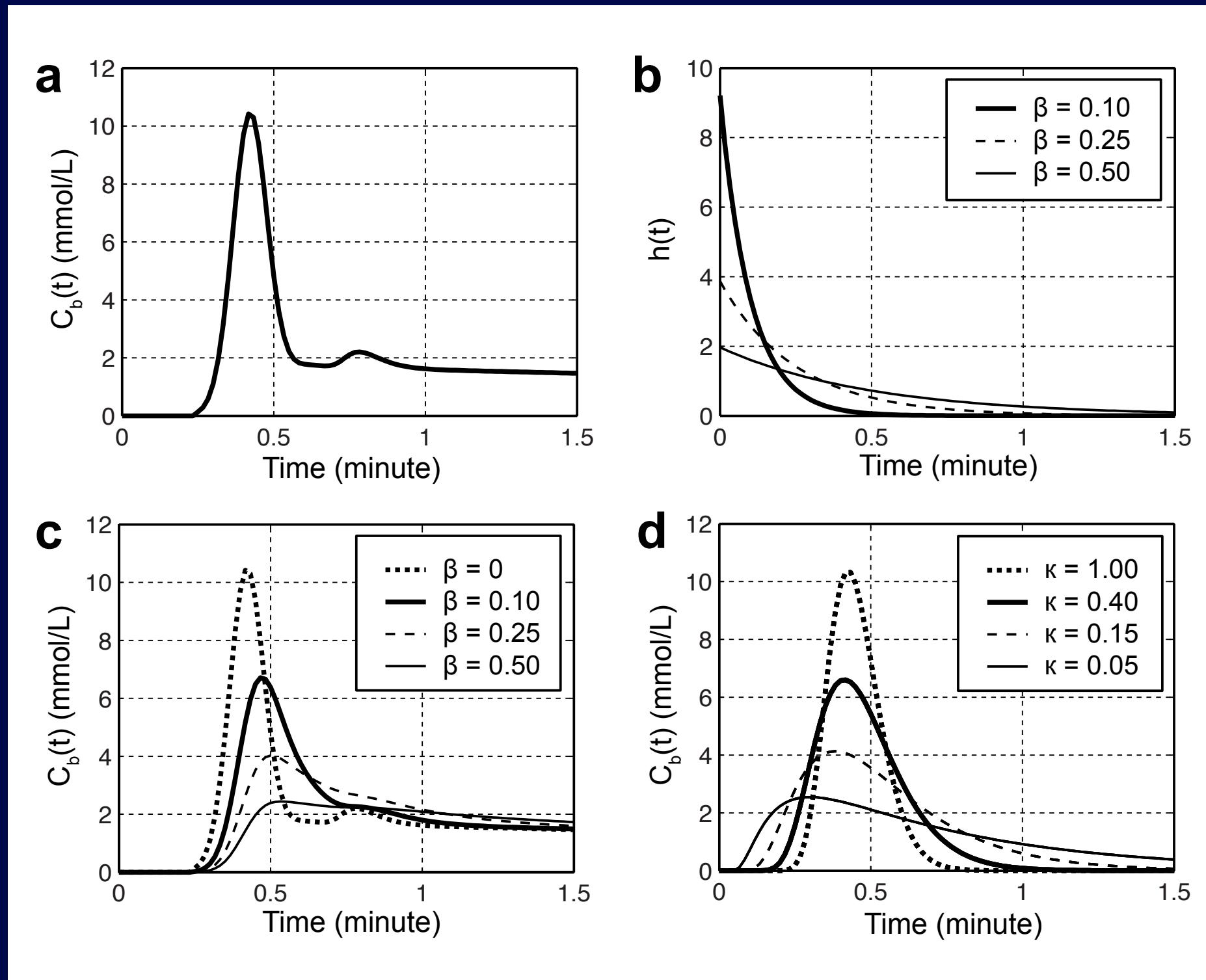
$$C_t(t) = \boxed{\beta} \int_0^t \sqrt{\frac{\boxed{\kappa}}{2\pi t}} \cdot e^{\frac{-\kappa(t-\boxed{\mu})^2}{2t}} \cdot e^{-k_{ep}(t-t')} dt'$$

$$C_t(t) = \boxed{K^{trans}} \int_0^t C_p(t') e^{-k_{ep}(t-t')} dt'$$

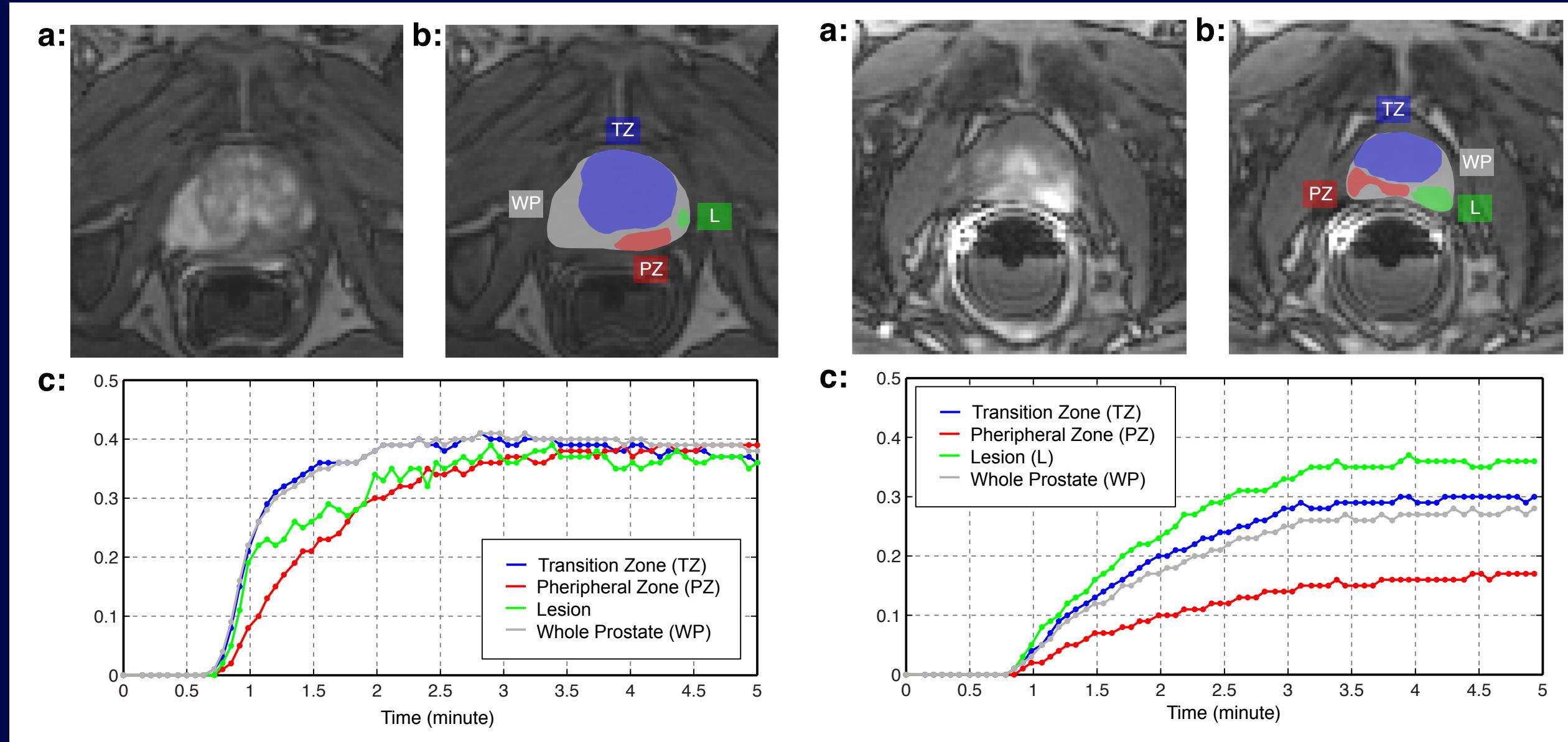
Modified Dispersion

$$C_p^{dispersed} = C_p(t) \star h(t) \quad h(r) = \frac{1}{\boxed{\beta}} e^{-t/\beta}$$

# Dispersion vs. Modified Dispersion



# GS 4+4 vs. GS 3+4 (PZ)



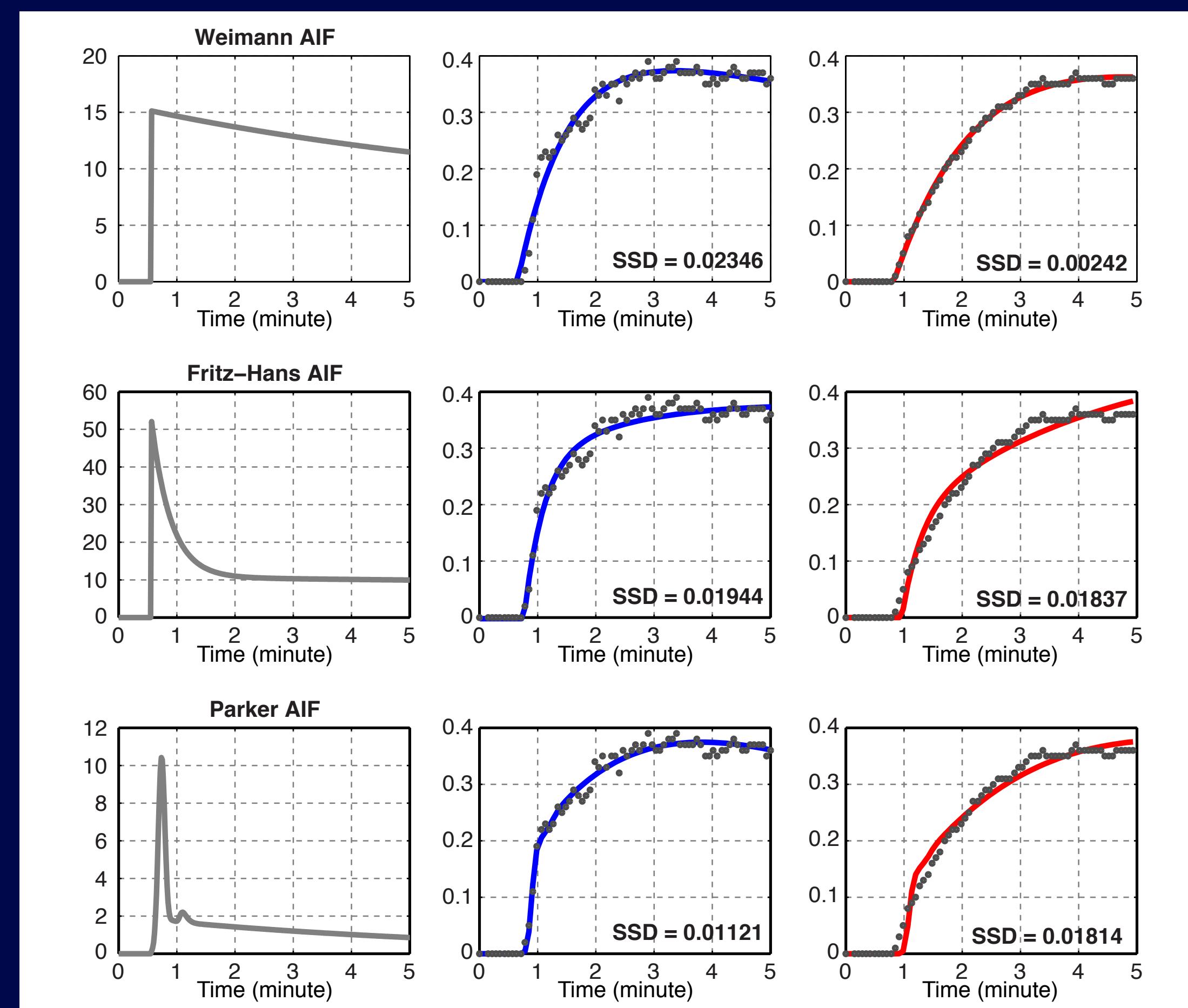
Low Dispersion



David Geffen  
School of Medicine

High Dispersion

**UCLA**  
Radiology

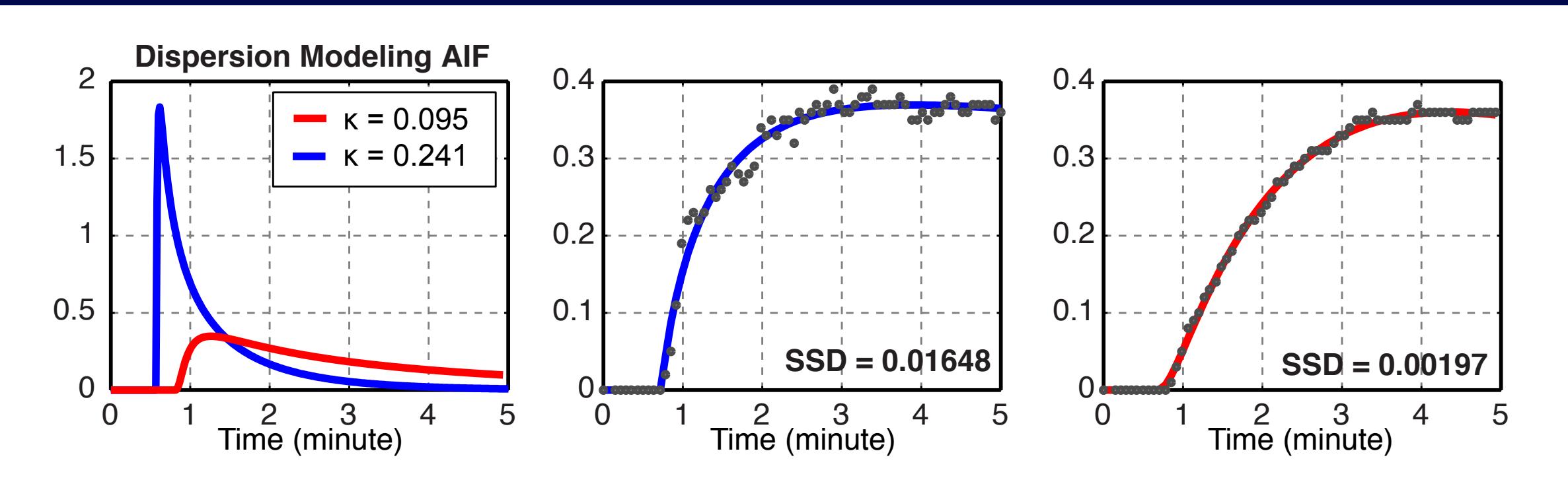


# Dispersion Modeling

$$C_p(t) = \alpha \sqrt{\frac{\kappa}{2\pi t}} \cdot e^{\frac{-\kappa(t-\mu)^2}{2t}}$$

Dispersion

$$C_t(t) = \beta \int_0^t \sqrt{\frac{\kappa}{2\pi t}} \cdot e^{\frac{-\kappa(t-\mu)^2}{2t}} \cdot e^{-k_{ep}(t-t')} dt'$$



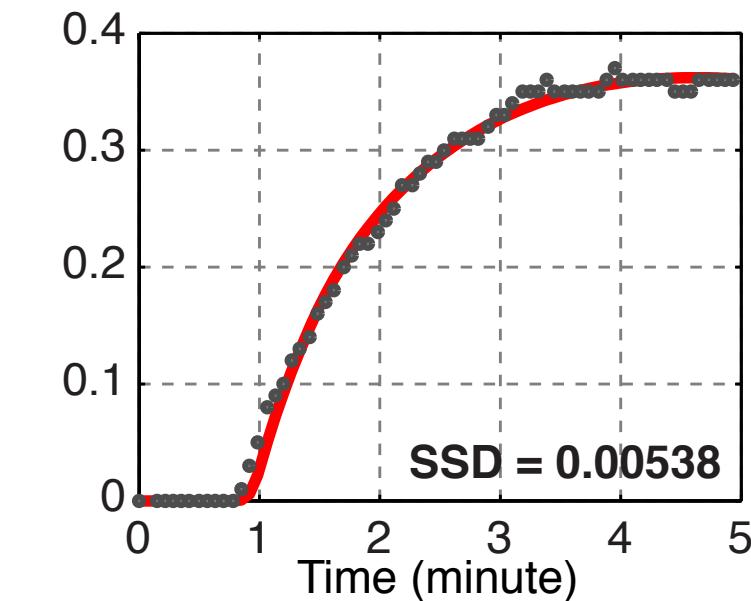
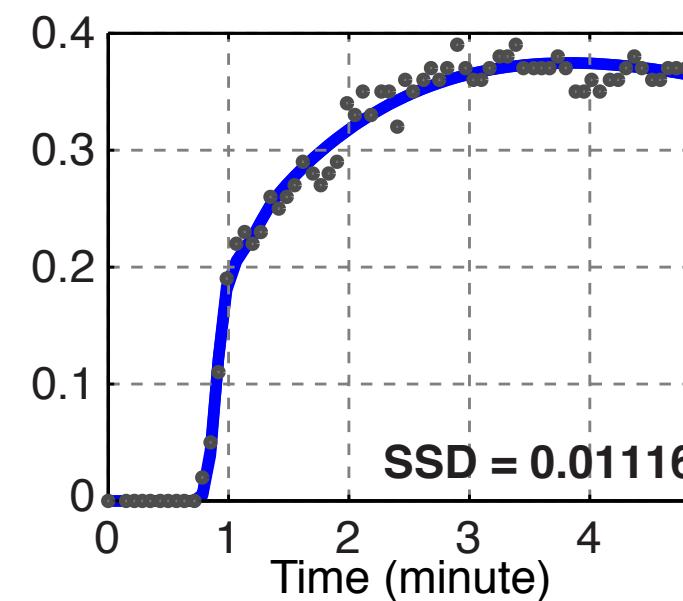
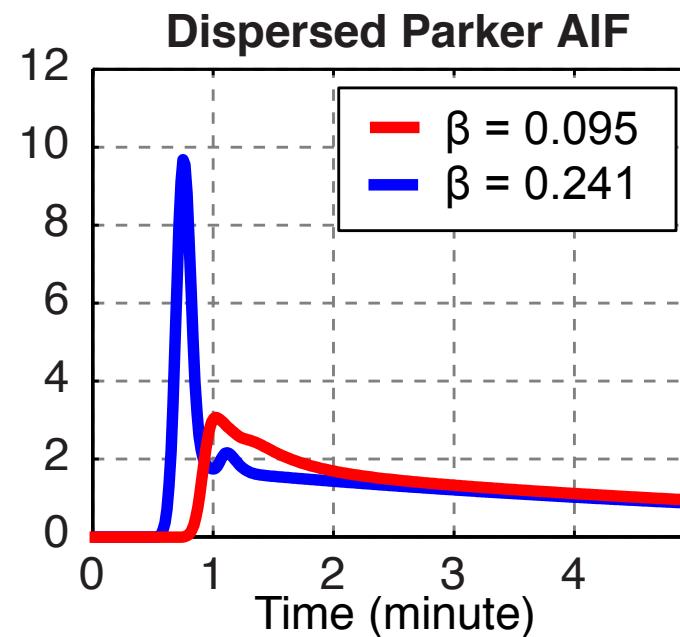
# Modified Dispersion Modeling

$$C_t(t) = K^{trans} \int_0^t C_p(t') e^{-k_{ep}(t-t')} dt'$$

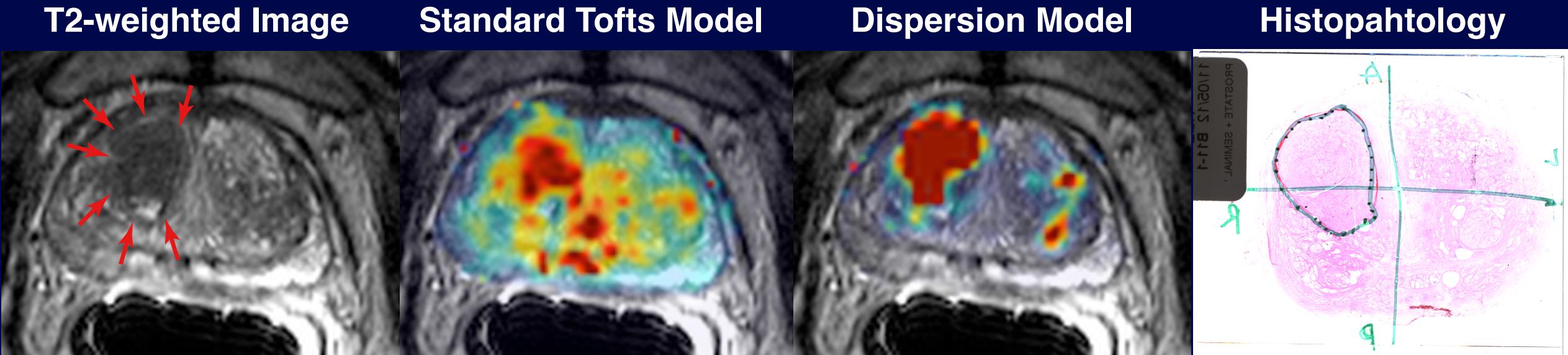
$$C_p^{dispersed} = C_p(t) \star h(t)$$

$$h(r) = \frac{1}{\beta} e^{-t/\beta}$$

**Modified  
Dispersion**



# Dispersion vs. Tofts model



Gleason 3+4

*Dispersion model shows the clearest delineation  
between tumor and normal tissue*



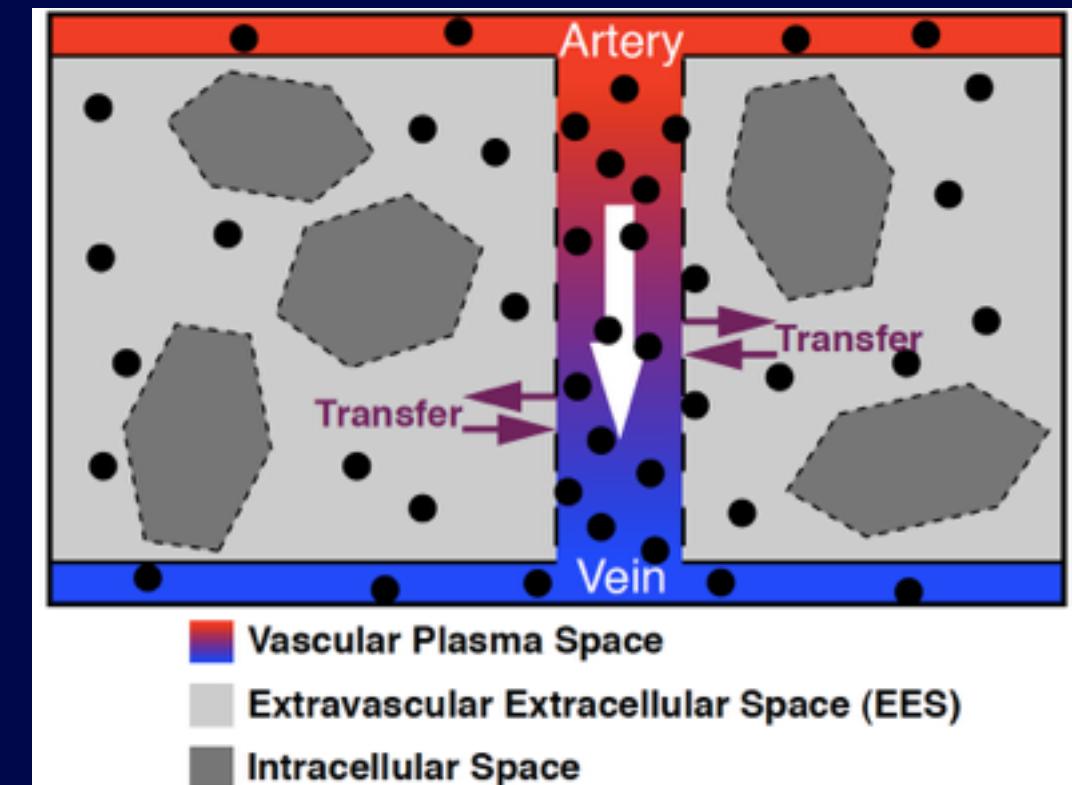
David Geffen  
School of Medicine

**UCLA**  
Radiology

# Physiological Understanding

- PK parameters are sensitive to a choice of the AIF model
- PK parameters can have different physiological meaning
  - High-permeability case
  - Low-permeability case
  - Mixed case
- Extended Tofts model

$$C_t(t) = v_p C_p + K^{trans} \int_0^t C_p(t') \exp \left( \frac{-K^{trans}(t - t')}{v_e} \right) dt'$$



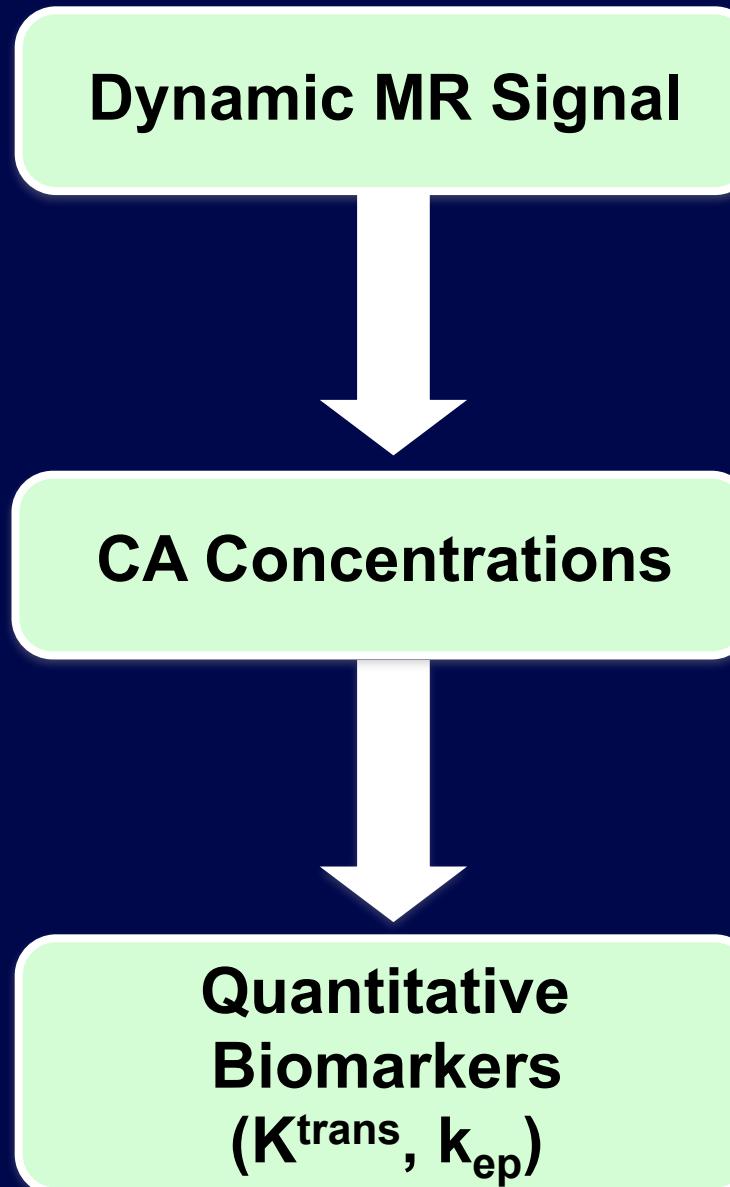
# Post-processing Option: DCE-MRI Data Analysis



David Geffen  
School of Medicine

**UCLA**  
Radiology

# Quantitative Data Analysis



- Software tools should facilitate:
  - $T_{1,0}$  map generation
  - Conversion from MR signal to CA concentration
  - Regions of interest (ROIs) plots
  - PK parameter calculation
- Software tools should also be able to:
  - Handle large 4D (3D + time) data
  - Manage DICOM databases
  - Locate regions of interests
  - Export back to DICOM databases



# OsiriX Plug-in: DCE Tool

- DCE-MRI analysis software (DCE Tool)
  - Plug-in to OsiriX (open-source medical image processing software)



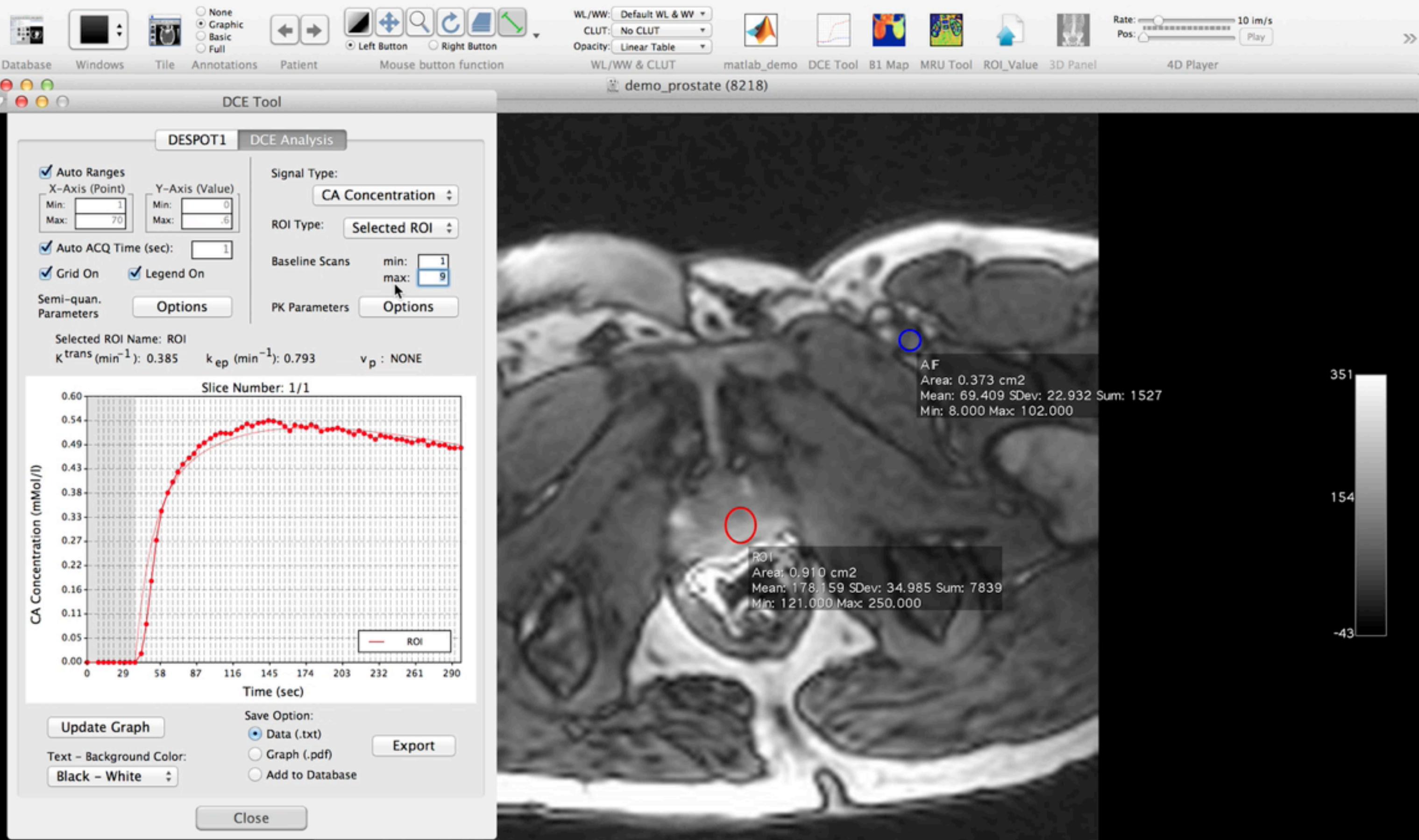
*A Rosset et al, J of Digital Imaging 2004*

- Selected features for DCE Tool:
  - $T_{1,0}$  map calculation (with an option for B1 compensation)
  - Supports for several AIF functions
    - PK parameter calculation (standard Tofts / extended Tofts models)
    - Semi-quantitative parameter calculation (initial slope, area under the curve, etc)

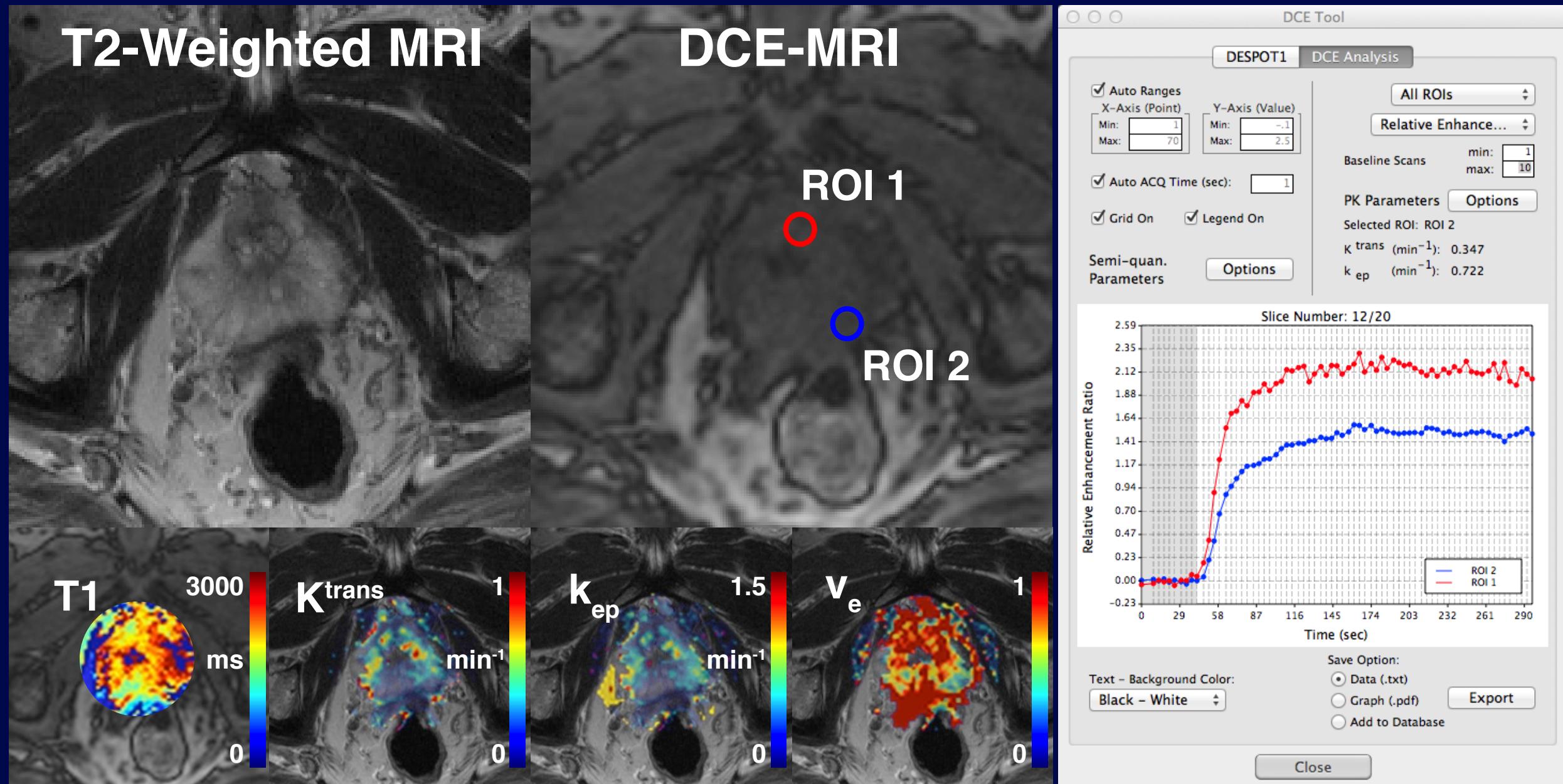


David Geffen  
School of Medicine

**UCLA**  
Radiology



# Quantitative DCE-MRI Software



*Sung K, RSNA 2011*

[http://kyungs.bol.ucla.edu/software/DCE\\_tool/DCE\\_tool.html](http://kyungs.bol.ucla.edu/software/DCE_tool/DCE_tool.html)



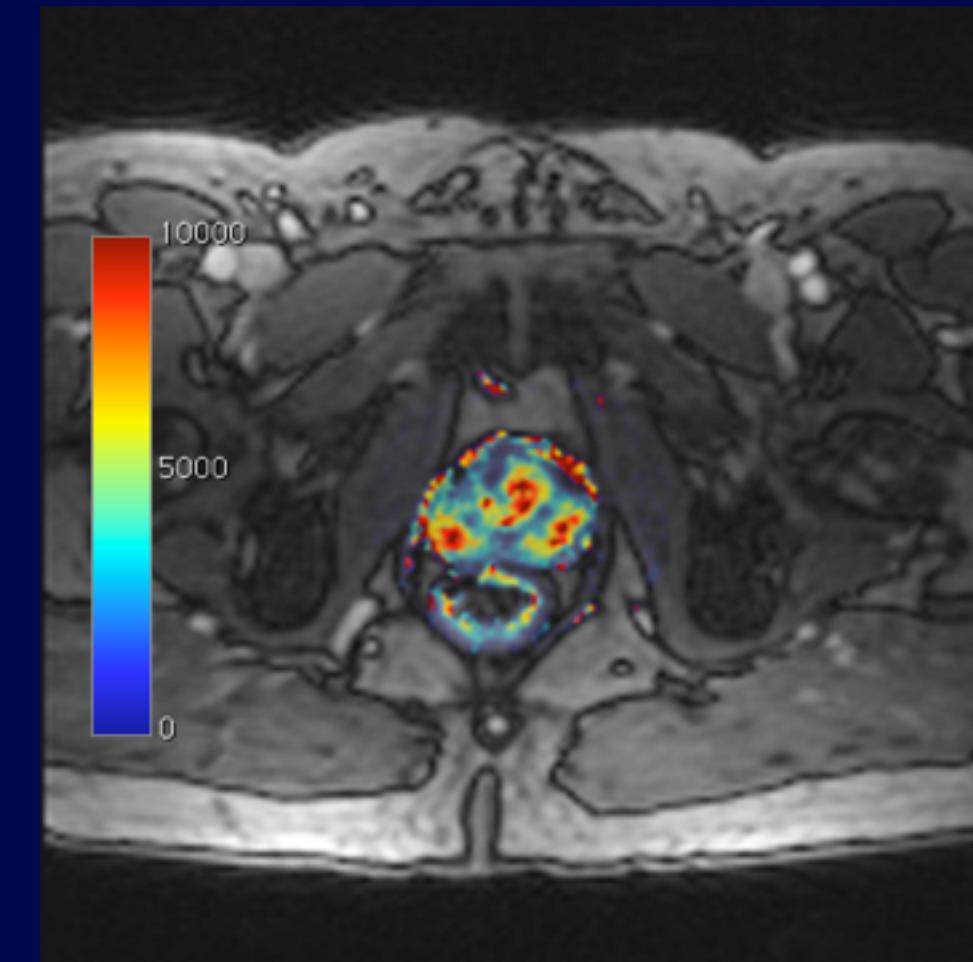
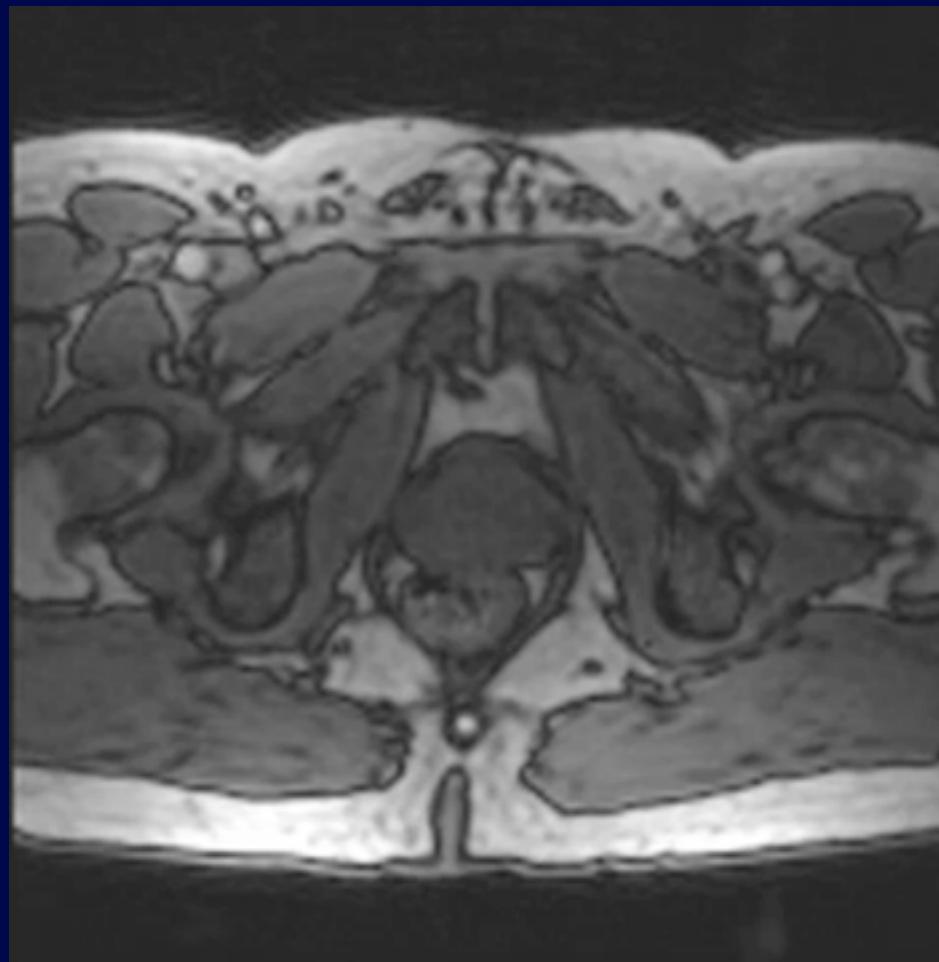
David Geffen  
School of Medicine

**UCLA**  
Radiology

# Prostate DCE-MRI

- Prostate DCE-MRI

$K^{trans}$  ( $\text{min}^{-1} \times 10000$ )



Temporal resolution ~ 4sec  
Spatial resolution = 1.6 X 1.6 X 3.6 mm



David Geffen  
School of Medicine

**UCLA**  
Radiology

# Overall Summary

---

- DCE-MRI has great potential to accurately produce quantitative biomarkers for cancer imaging
- PK parameters can represent different meanings depending on various assumptions
- Understanding possible sources of errors is critical for accuracy and precision
- Standard imaging protocol and image analysis are important for reproducible results



# Thank You!



David Geffen  
School of Medicine



Kyung Sung, PhD

[ksung@mednet.ucla.edu](mailto:ksung@mednet.ucla.edu)

<http://kyungs.bol.ucla.edu>



David Geffen  
School of Medicine

**UCLA**  
Radiology